

Topology between one and two dimensions

Cristiane Morais Smith

Institute for Theoretical Physics, Utrecht Univ., the Netherlands

C.deMoraisSmith@uu.nl

Abstract

We know how topological insulators behave in 1,2,3 dimensions, but what happens in between? In this talk, I will first present theoretical and experimental results on the behavior of ultranarrow germanene nanoribbons. We found that a phase transition from 1D topological edge states to 0D end states occurs as the width of the nanoribbons is reduced below 2 nm [1], see Fig. 1. Then, I will discuss the topological properties of electrons in self-formed single-layer bismuth fractals with dimension $d = 1.58$ [2], see Fig. 2. Finally, I will present theoretical results on the Hubbard model in a fractal geometry [3] and discuss ongoing studies on a fractal made of Rydberg atoms with long-range interactions (in preparation).

References

- [1] D. J. Klaassen, L. Eek et al., Nature Communications **16** (2025) 2059.
- [2] R. Canyellas, C. Liu et al., Nature Physics **20** (2024) 1421.
- [3] M. Conte, V. Zampronio, M. Rontgen, and C. Morais Smith, Quantum **8** (2024) 1469.

Figures

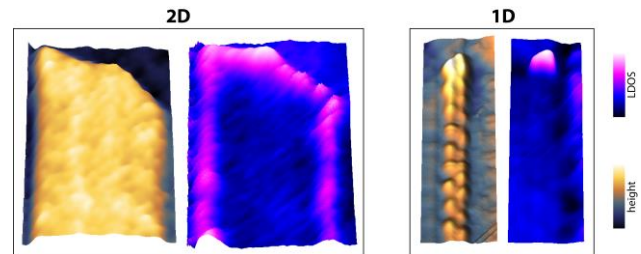


Figure 1: Topographic view (left) and local density of states (LDOS) (right) for broad (2D) and ultranarrow (1D) germanene nanoribbons. The topological states are visible in pink (high LDOS).

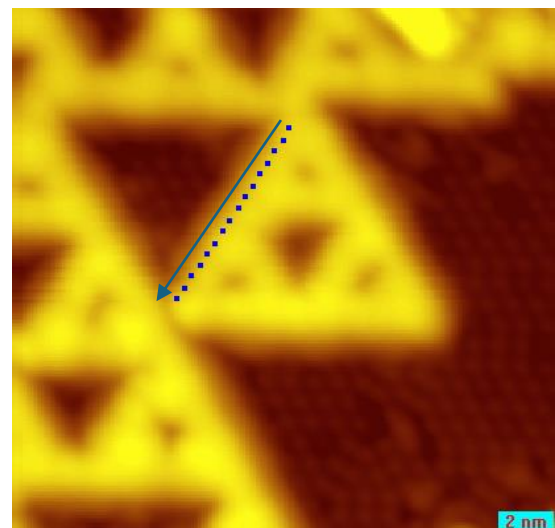


Figure 2: Topographic image of the single-layer bismuth Sierpinski fractals spontaneously formed in InSb substrates. The fractals have a Hausdorff dimension $d = 1.58$ and exhibit both, 1D edge states and 0D corner states.
