

# Anisotropy in phonon and electron transport in $\text{Sb}_2\text{Se}_3$ from machine learning foundation models

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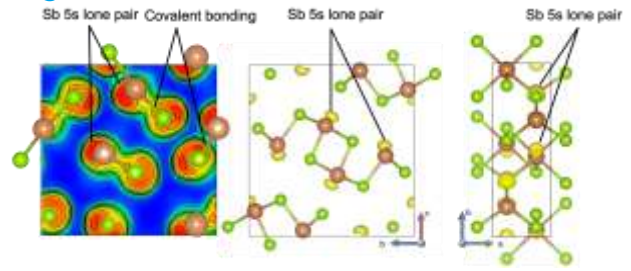
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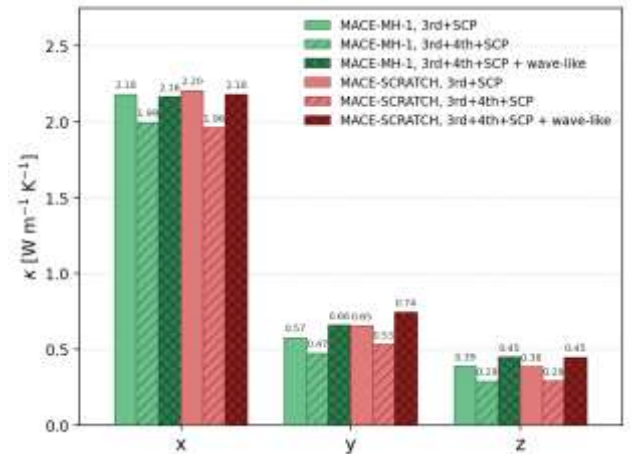
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The comprehensive evaluation of phonon and electron transport has long been hindered by the fundamental trade-off between *ab initio* accuracy and computational efficiency. The success of machine learning foundation models in mapping potential energy surfaces and electronic Hamiltonian raised the question: can they be extended to predict complex transport properties with high efficiency without sacrificing *ab initio* accuracy? To answer this question, in this work, we develop a computational workflow integrating state-of-the-art machine learning interatomic potential MACE-MH-1 [1] and Hamiltonian foundation models Uni-HamGNN [2] to investigate the electron and phonon transport properties in  $\text{Sb}_2\text{Se}_3$ . Our results reveal both significant phonon and electron transport anisotropy in  $\text{Sb}_2\text{Se}_3$ : the lattice thermal conductivity exhibits a  $\sim 4.8$ -fold anisotropy, reaching  $\sim 2.16$  W/mK along the ribbon axis (*x*-axis) and dropping to  $\sim 0.66$  (*y*-axis) and  $\sim 0.45$  W/mK (*z*-axis) across layers. The pronounced anisotropy in phonon transport originates from the spatial distribution of lone-pair electrons. More specifically, the lone-pair electrons are predominantly distributed within the *yz*-plane, which induces highly asymmetric interatomic forces. This large force asymmetry triggers the highest anharmonic phonon scattering rates, ultimately leading to the ultralow thermal conductivity along the *z*-direction. Furthermore, the carrier mobilities also exhibit remarkable anisotropy. The electron mobility demonstrates a staggering  $\sim 48.0$ -fold contrast between the *x* and *z* directions, while the hole mobility shows a  $\sim 5.1$ -fold variation between the *y* and *z* axes. These electronic anisotropies are primarily driven by significant directional variations in electron-phonon coupling strength and carrier effective mass. This work successfully demonstrates the capability of foundation models to predict complex transport properties with *ab initio* accuracy and remarkable efficiency in  $\text{Sb}_2\text{Se}_3$ .

## Figure and Table



**Figure 1.** Crystal structure and electronic localization function (ELF) of  $\text{Sb}_2\text{Se}_3$ . Left: ELF plot showing the distribution of Sb 5s lone pairs and covalent bonding regions. Middle and Right: 3D ELF plot of the lone-pair electron density (yellow) relative to the Sb (brown) and Se (green) atomic framework.



**Figure 2.** Calculated lattice thermal conductivity along different crystallographic axes. The bar chart compares values calculated using MACE-MH-1 and MACE-SCRATCH models across various levels of theory (3rd order, 4th order, SCP, and wave-like corrections).

**Table 1.** Directional carrier mobilities and effective masses  $m^*$  for electrons and holes, where polar denotes the contribution from polar optical phonon scattering and rmp represents the remaining scattering mechanisms.

$\text{cm}^2\text{V}^{-1}\text{s}^{-1}$	dir	polar	rmp	total	$m^*(m_0)$
Electron	x	99.64	407.24	79.24	0.15
	y	17.92	75.99	14.30	0.89
	Z	2.03	9.65	1.65	7.92
Hole	x	10.94	52.02	8.98	0.97
	y	19.50	97.30	16.13	0.56
	z	3.79	20.33	3.17	2.53

## References

- [1] Batatia et al, <https://arxiv.org/pdf/2510.25380>
- [2] Zhong *et al*, Nature Machine Intelligence, 8, 403–414 (2026)