

Exploring Ground States of Fermi-Hubbard Model on Honeycomb Lattices with Counterdiabaticity

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The ground state of Fermi-Hubbard model is of relevance to essential material characteristics in the systems such as artificial graphene and high-temperature superconductors [1-2]. In this talk, we present the exploration of the ground state properties of this model on a honeycomb lattice structure using quantum counterdiabatic (CD) algorithms with shallower circuit depth and fewer qubit numbers [3]. Our study focuses on variational quantum algorithms, specifically leveraging CD algorithms to design shallow quantum circuits capable of simulating larger honeycomb lattices, shown in Fig. 1.

We demonstrate the efficacy of the CD algorithm through a comparative analysis of its performance against Hamiltonian variational ansatz (HVA) on a triangular honeycomb lattice with 26 qubits, as depicted in Fig. 2. Moreover, we introduce noise into the quantum circuits. Notably, our findings indicate that the counterdiabatic-inspired ansatz outperforms in accurately determining the ground energy.

This study sheds light on the potential of variational quantum algorithms in probing quantum materials, particularly within the complex landscape of noisy intermediate-scale quantum computing.

References

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Figures

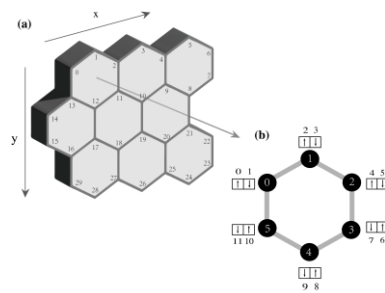


Figure 1. A schematic diagram of the Fermi-Hubbard model: regular hexagonal honeycomb structure is used to describe the lattices.

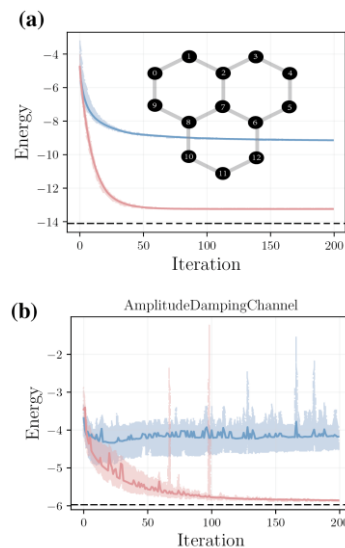


Figure 2. Energy as a function of iteration. (a): The blue solid line is HV ansatz, the red solid line is CD inspired ansatz. The black dash line shows the exact ground energy. Shaded regions present the upper quartile and lower quartile of ten instances. (b): System energy corresponding to 1x1 honeycomb lattice structure with amplitude damping noise.