



Gradient-index electron optics in graphene pn junctions

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Motivation

- Study the ballistic transport on graphene pn junctions.
- Generate the pn junctions on graphene with backgate-voltages.
- Describe the current flow by analogies of the gradient-index geometrical optics.
- Propose several nanodevices in graphene.

NEGF method

Tight-binding model External electrostatic potential

$$G = (E - H - V - \Sigma)^{-1}$$

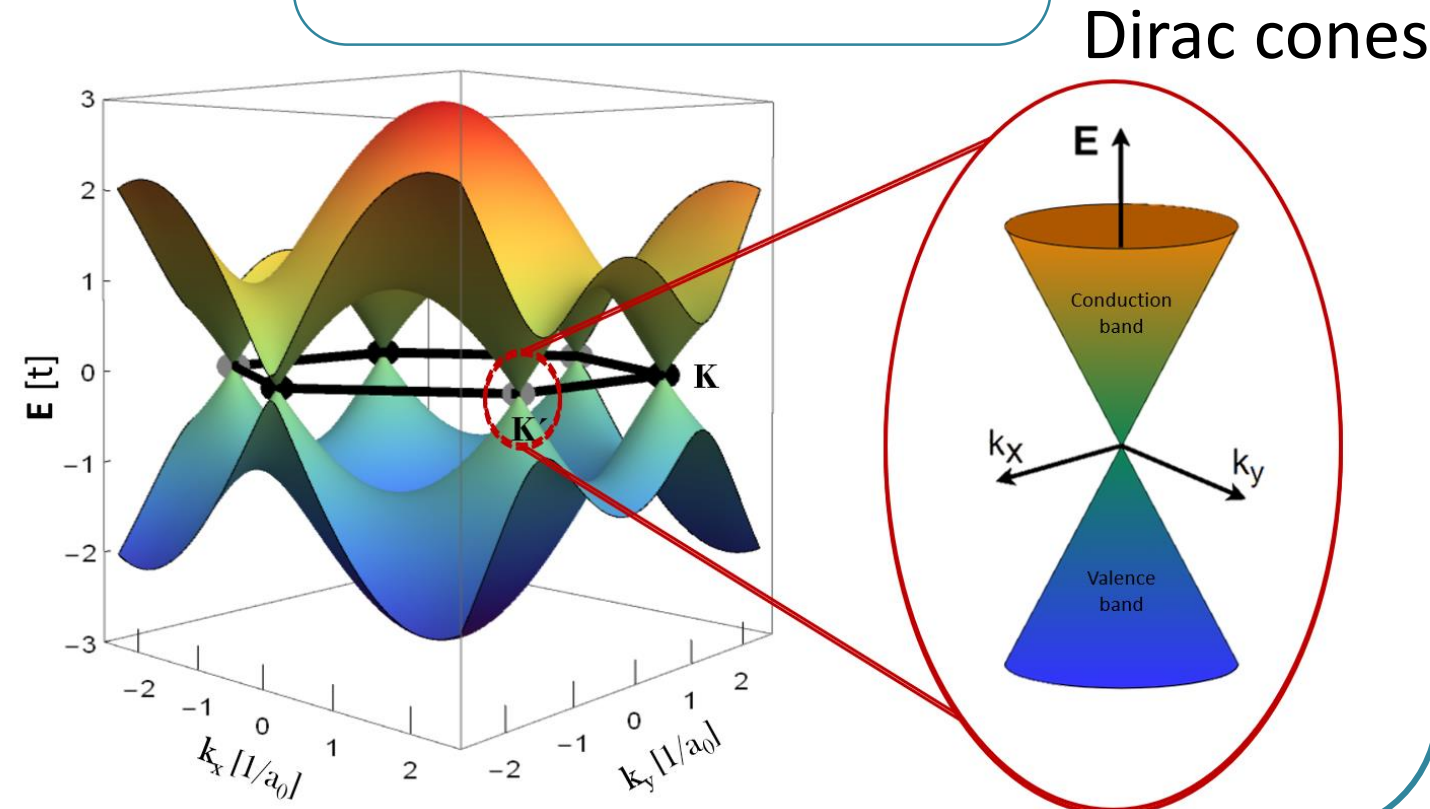
$$G^< = G \Sigma^in G^>$$

Electrons' Inscattering function

$$I_{ij}^{OP} = \frac{2e}{h} \text{Im}(t_{ij}^* G_{ij}^<)$$

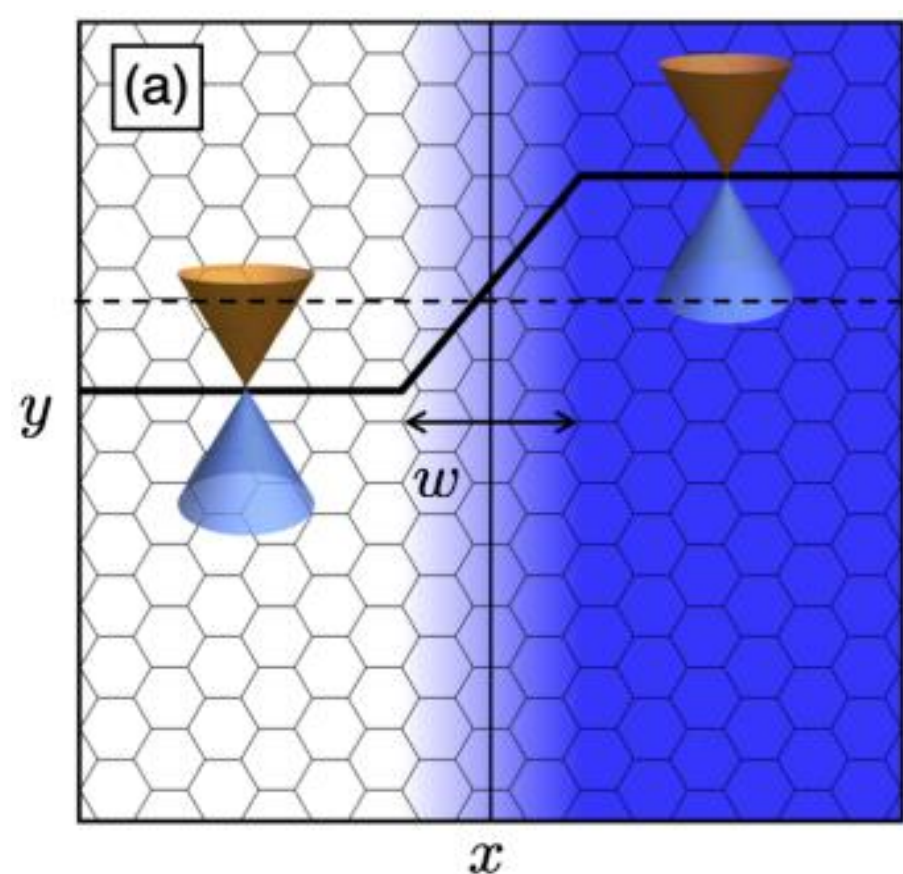
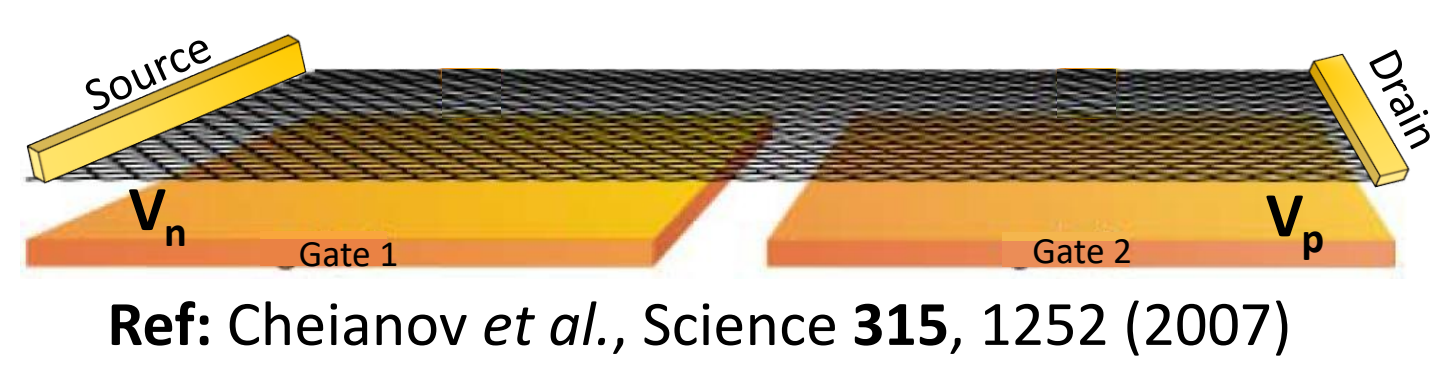
Local current on the system

Graphene band structure

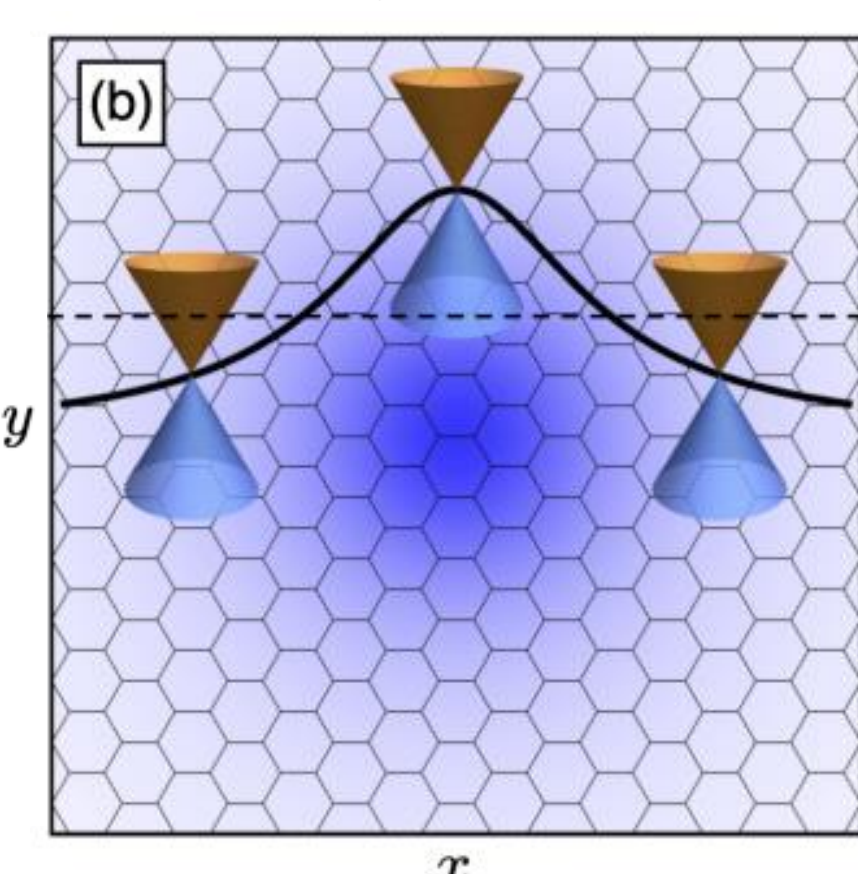
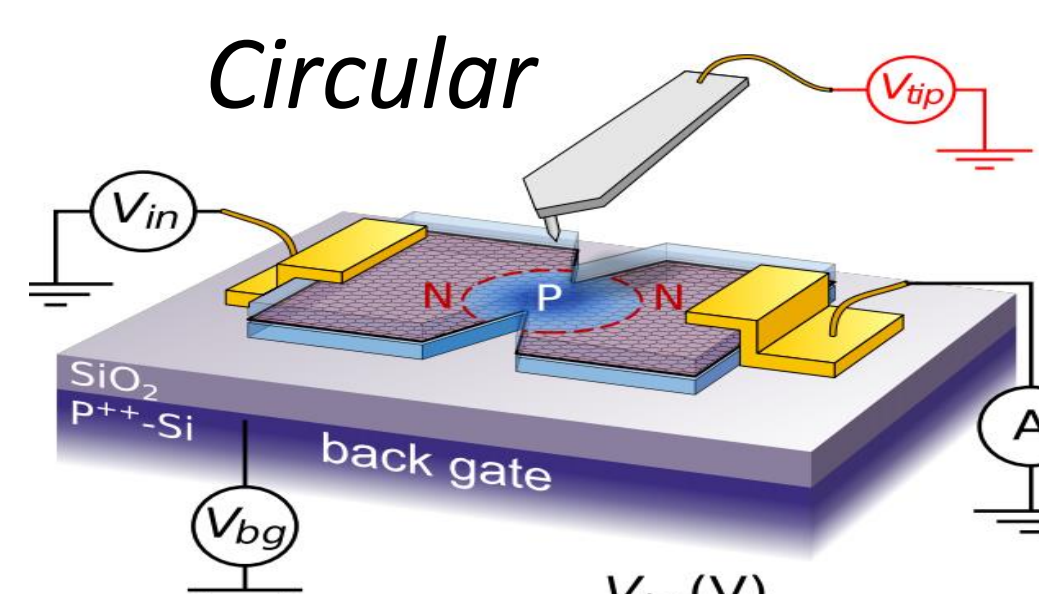


Graphene pn junctions

Straight



Circular



Gradient-index optics

Effective refractive index: $n(r) \equiv \frac{E - V(r)}{v_F}$

The index dependence of the position of the medium/region of system.

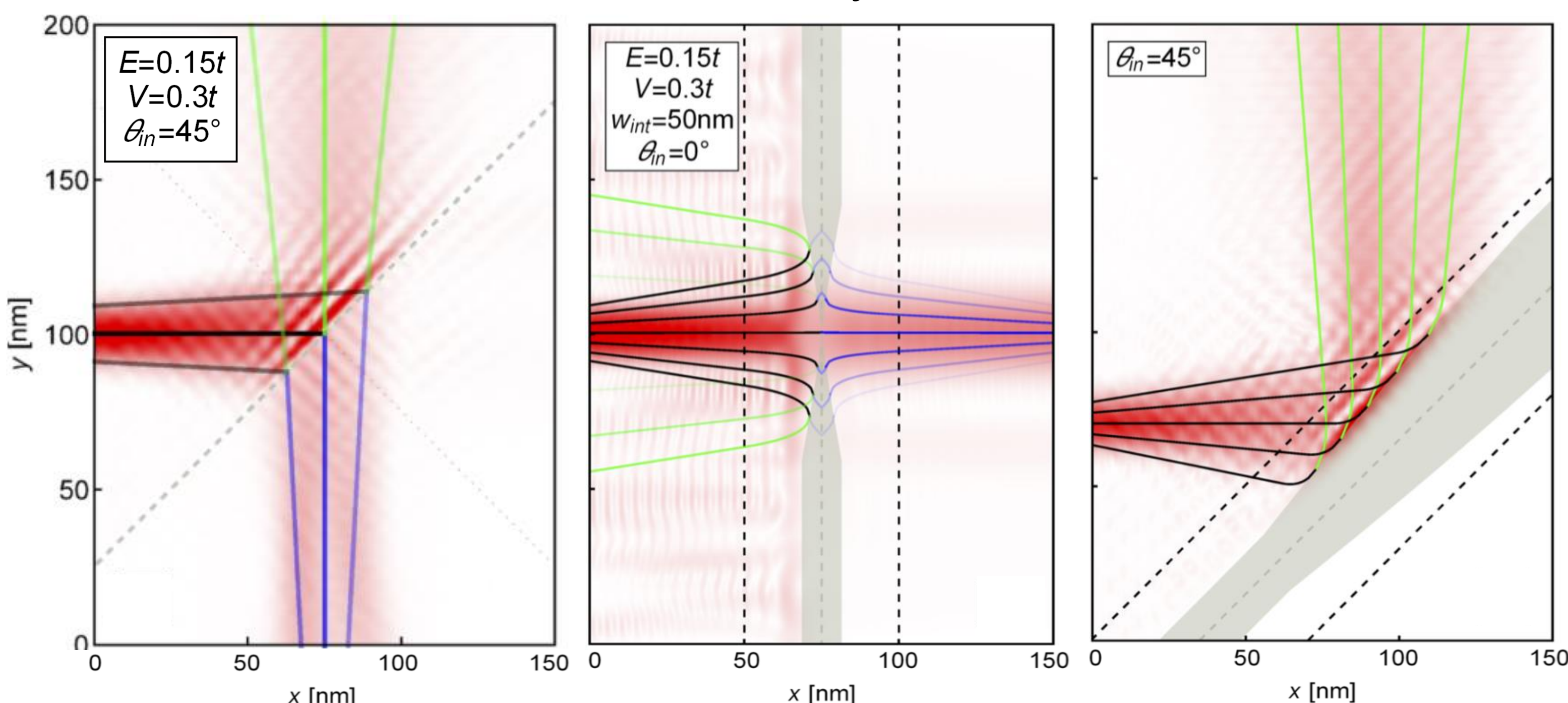
Straight pn junctions

Semiclassical trajectories: $y(x) = y_0 + p_y \int_{x_0}^x \frac{s(x') dx'}{\sqrt{n^2(x') - p_y^2}}$

Gradient-index optics!

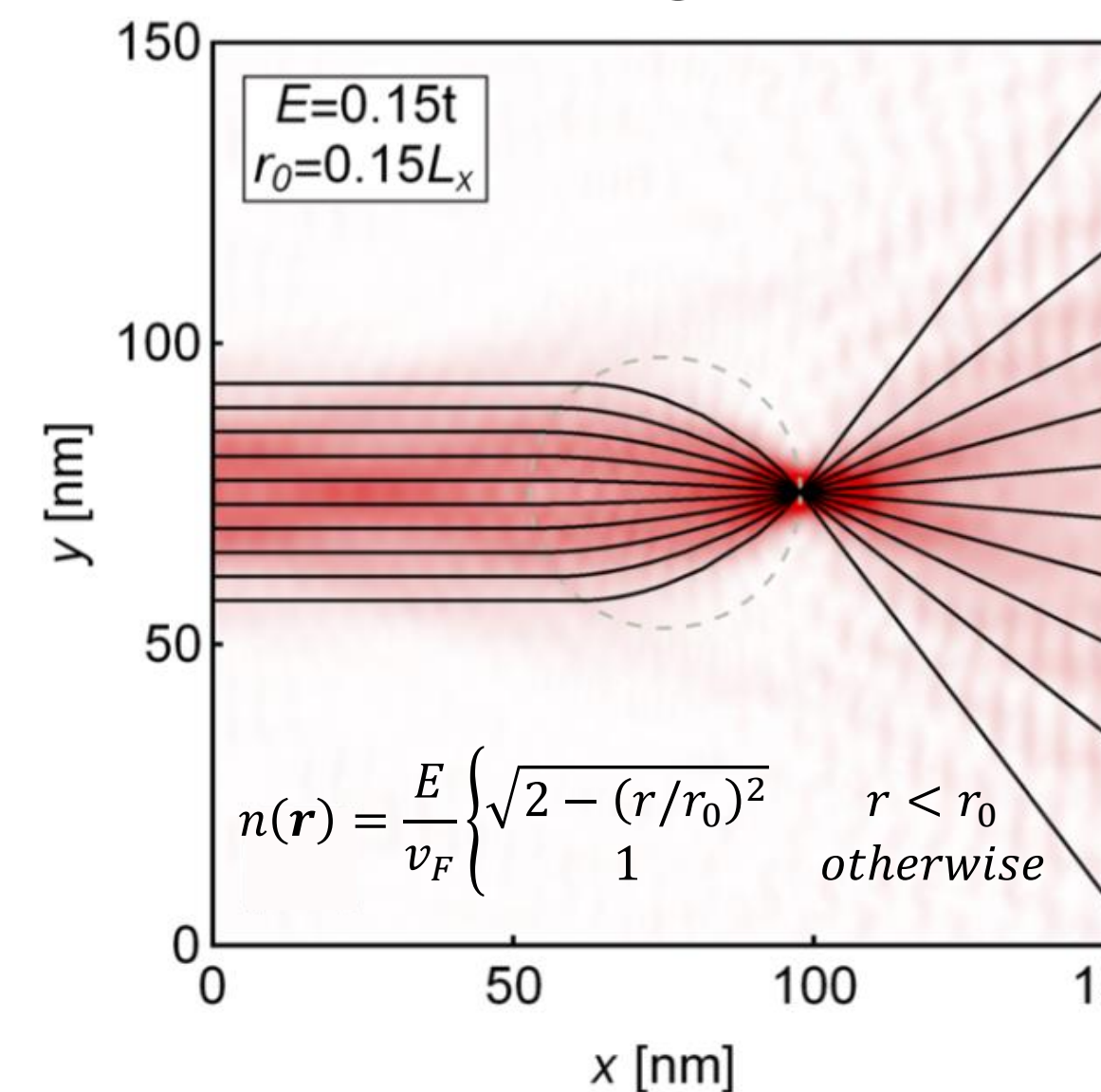
Step junction: negative refraction and Snell's law for electrons.

Smooth junction: classical forbidden zone

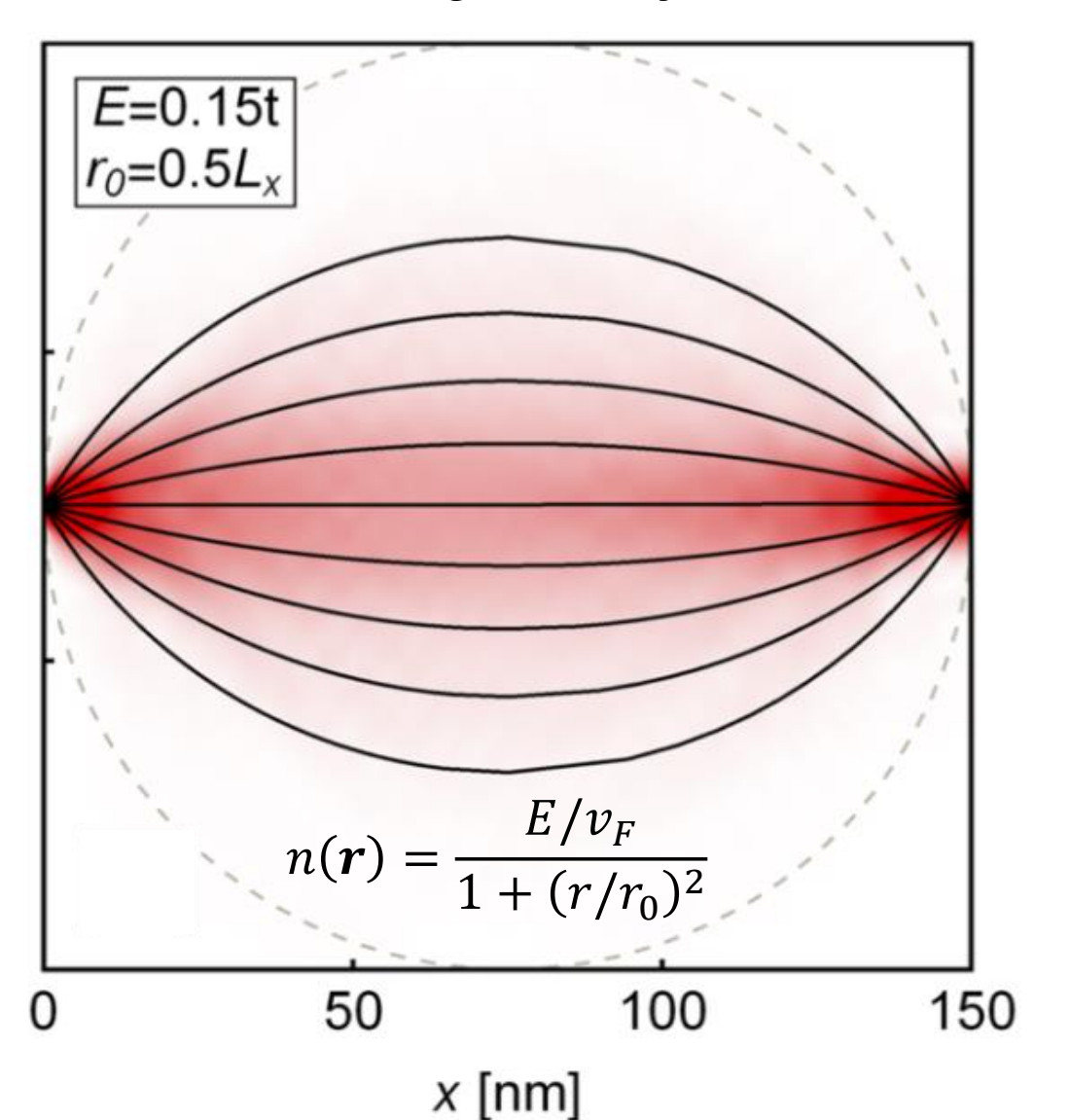


Optical lenses in graphene

Luneburg lens



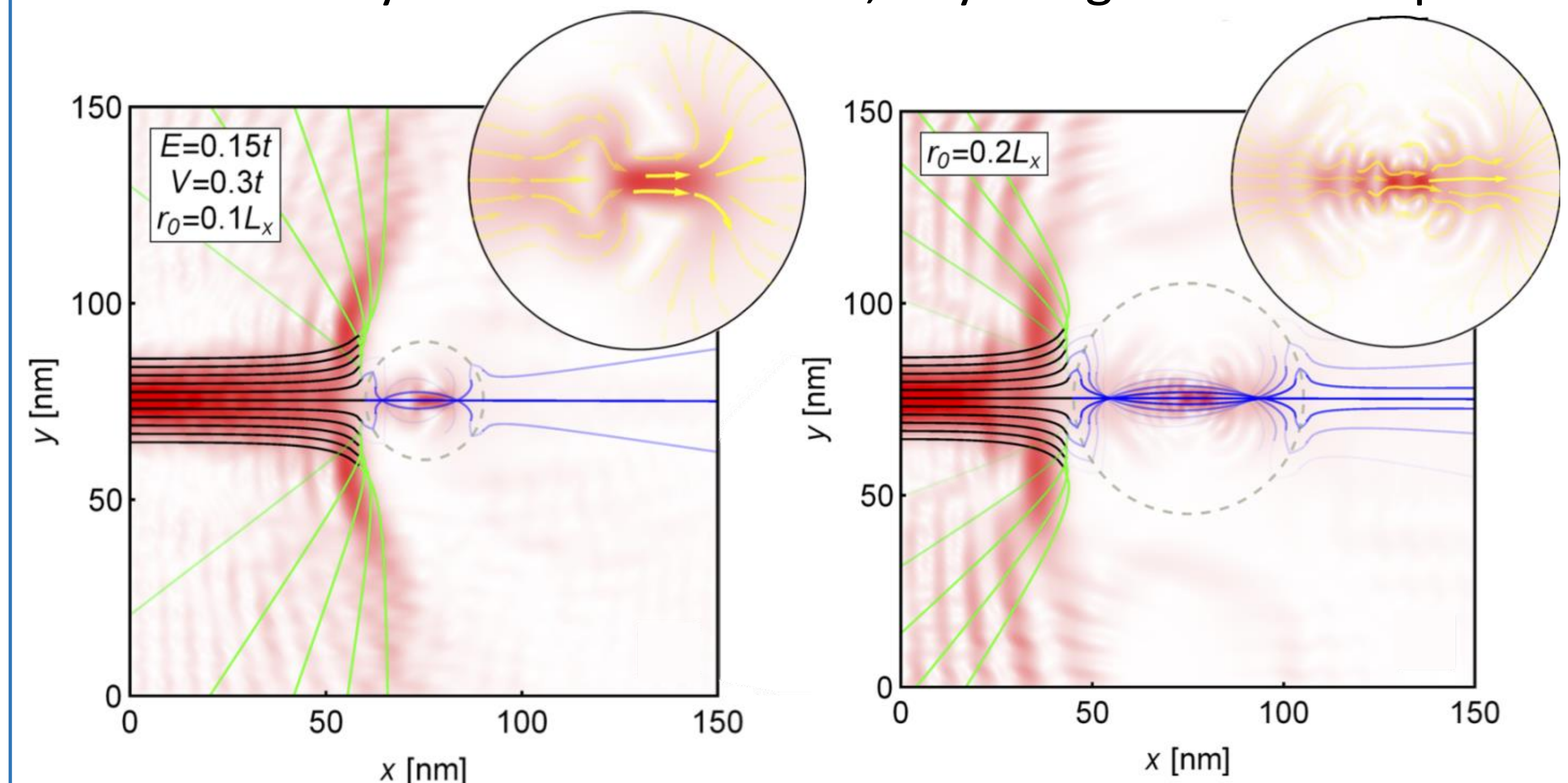
Maxwell's fisheye lens



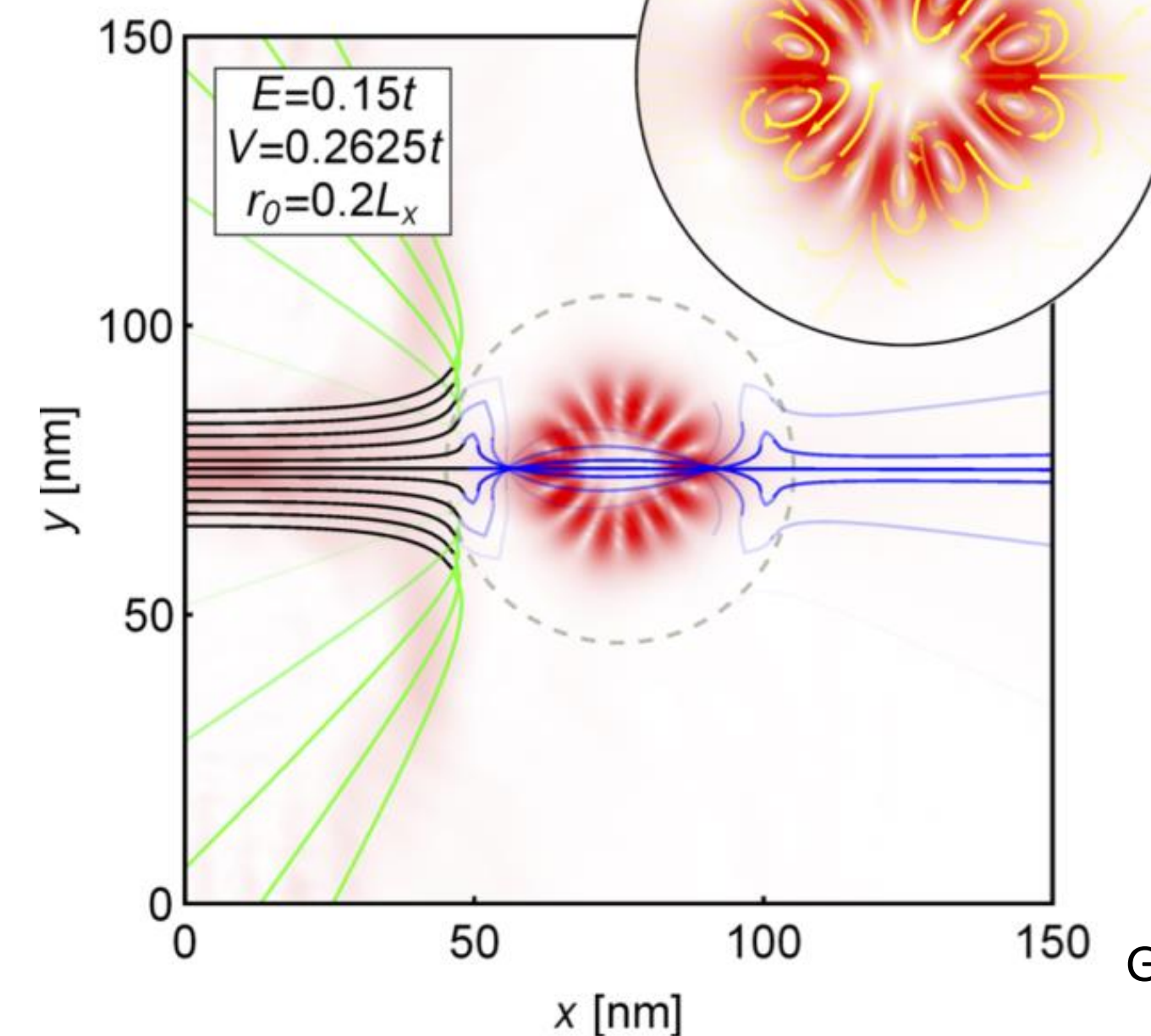
Smooth circular pn junctions

Semiclassical trajectories: $\theta = \theta_0 + l \int_{r_0}^r \frac{s(r') dr'}{r' \sqrt{r'^2 n^2(r') - l^2}}$

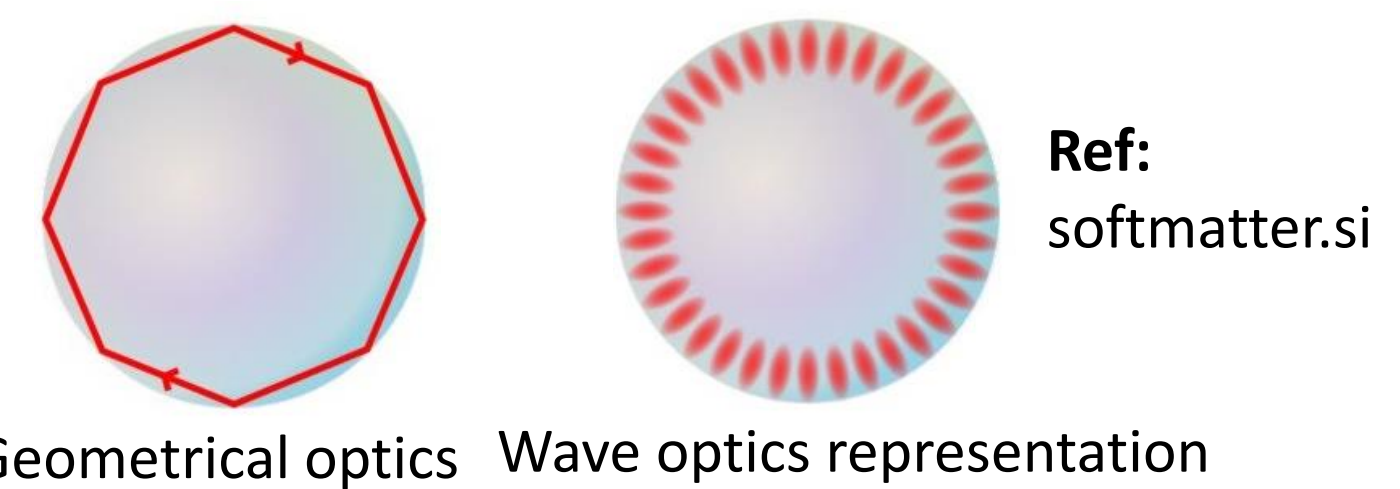
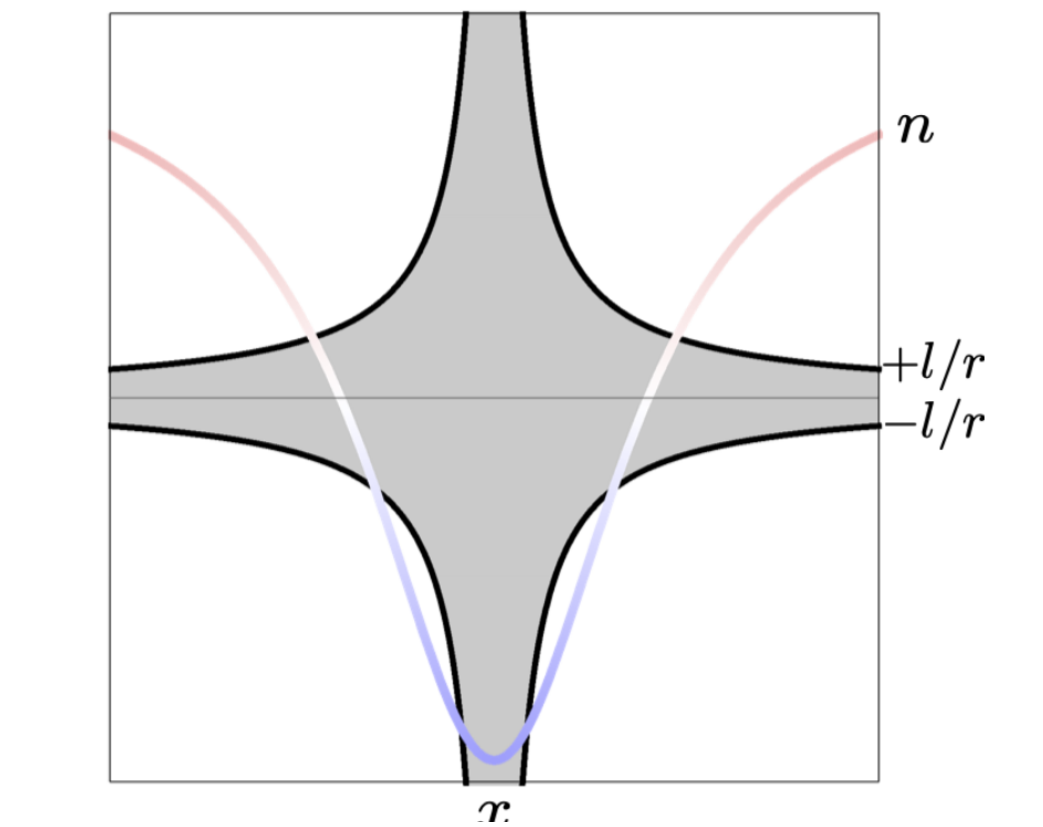
Look on the inside of the dashed circle (p region): significant interference by internal reflections, beyond geometrical optics.



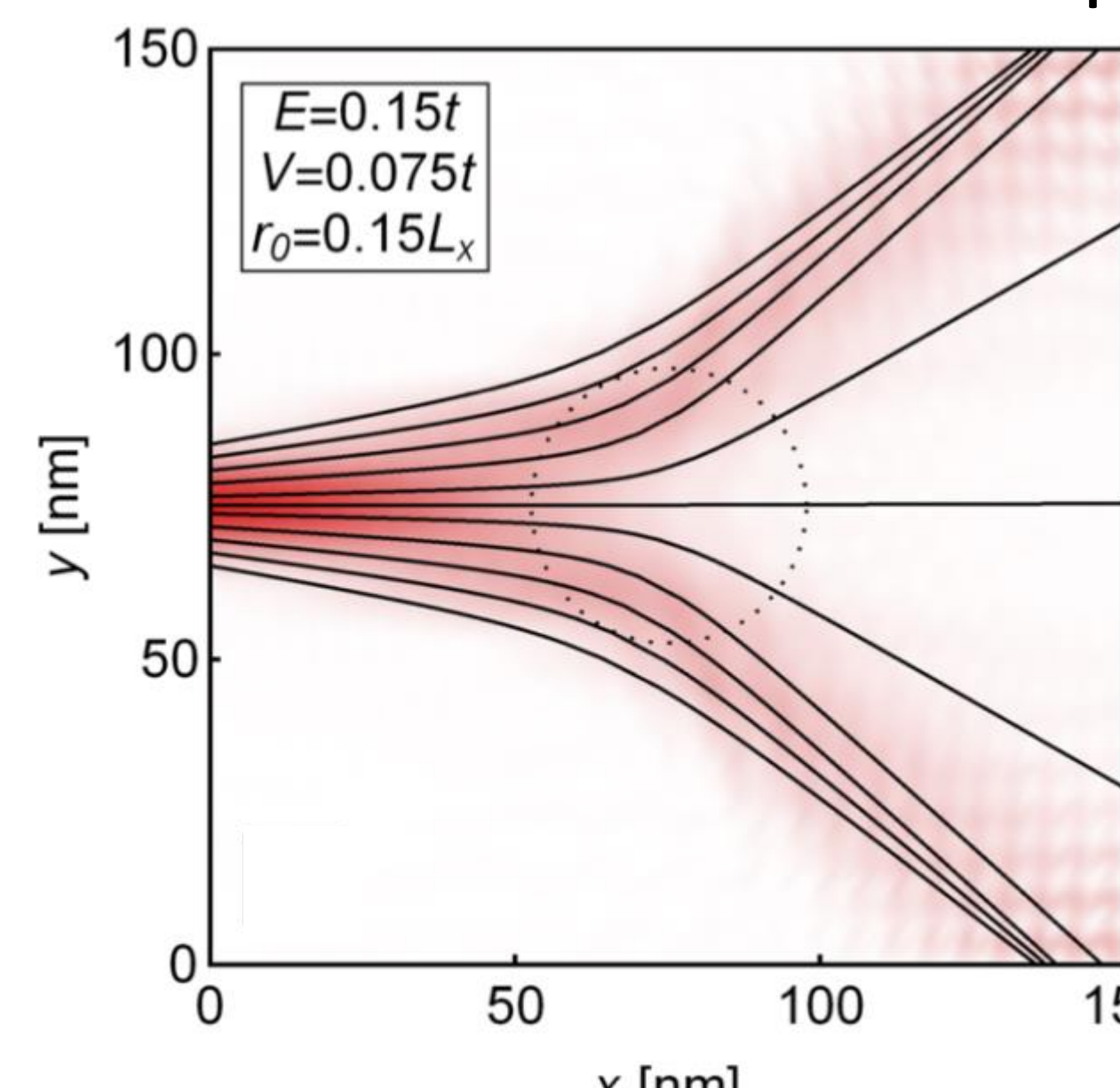
Whispering Gallery Modes



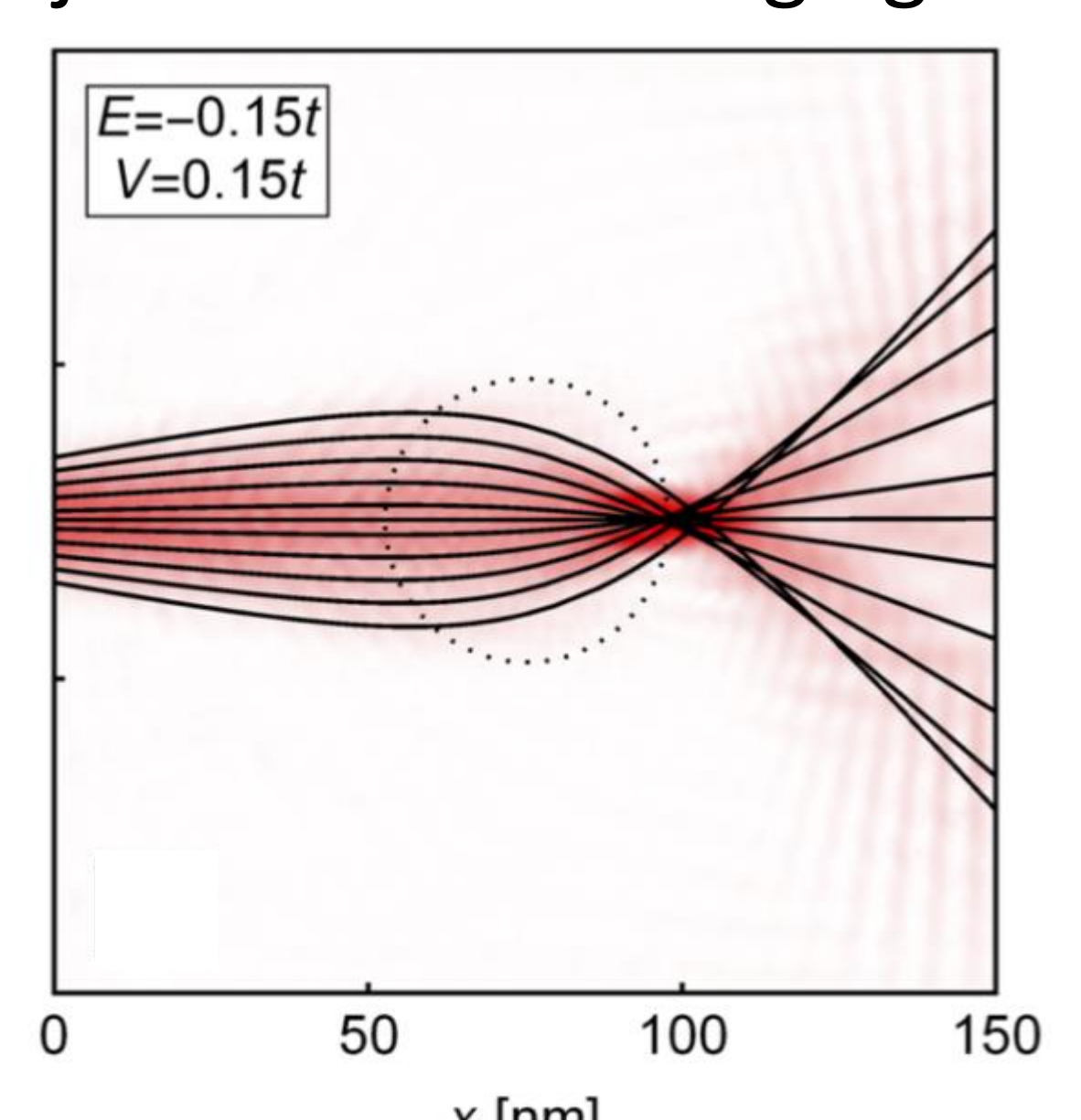
Classical forbidden regions



nn' jct: beam splitter



pp' jct: act like converging lens



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REFERENCES

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