

Introduction

Recent interest in two-dimensional (2D) materials has re-initiated intensive discussion on bulk layered materials' electronic and optical properties. The debate concerning the band gap of bulk hexagonal boron nitride (h-BN), its nature, and excitonic properties was re-opened by recent experiments^{1,2}. While graphite (and its 2D analog called graphene) is a zero band gap semi-metal, h-BN is a wide gap semiconductor with very high thermal and chemical stability suitable in devices operating under extreme conditions. Experimental estimation of the bulk h-BN band gap has been a long-debated issue, and different experiments have varied. The nature of the band gap was controversial too. Still, this recent experimental studies brought a turning point in this consensus and showed the band gap's nature as indirect and reported very accurate values of the electronic and optical band gaps.

Methods

Experimental lattice constants of $a = 2.502 \text{ \AA}$ and $c = 6.617 \text{ \AA}$ was used. The Vienna *ab initio* simulation package (VASP)³ implementing projector augmented-wave (PAW) method, GW set of PAWs, and cut-off energy $E_{\text{cut}} = 500 \text{ eV}$ are used in all calculations (2s1p electrons are explicitly treated). We use GW⁴ approximation with input orbitals from DFT and Perdew, Burke and Ernzerhof (PBE) functional⁵ for electronic structure calculations. The break condition for the electronic step is an energy difference of $1 \times 10^{-6} \text{ eV}$. Excitonic effects are accounted for by the Bethe-Salpeter equation⁶.

Benchmark GW and BSE study of h-BN band gaps

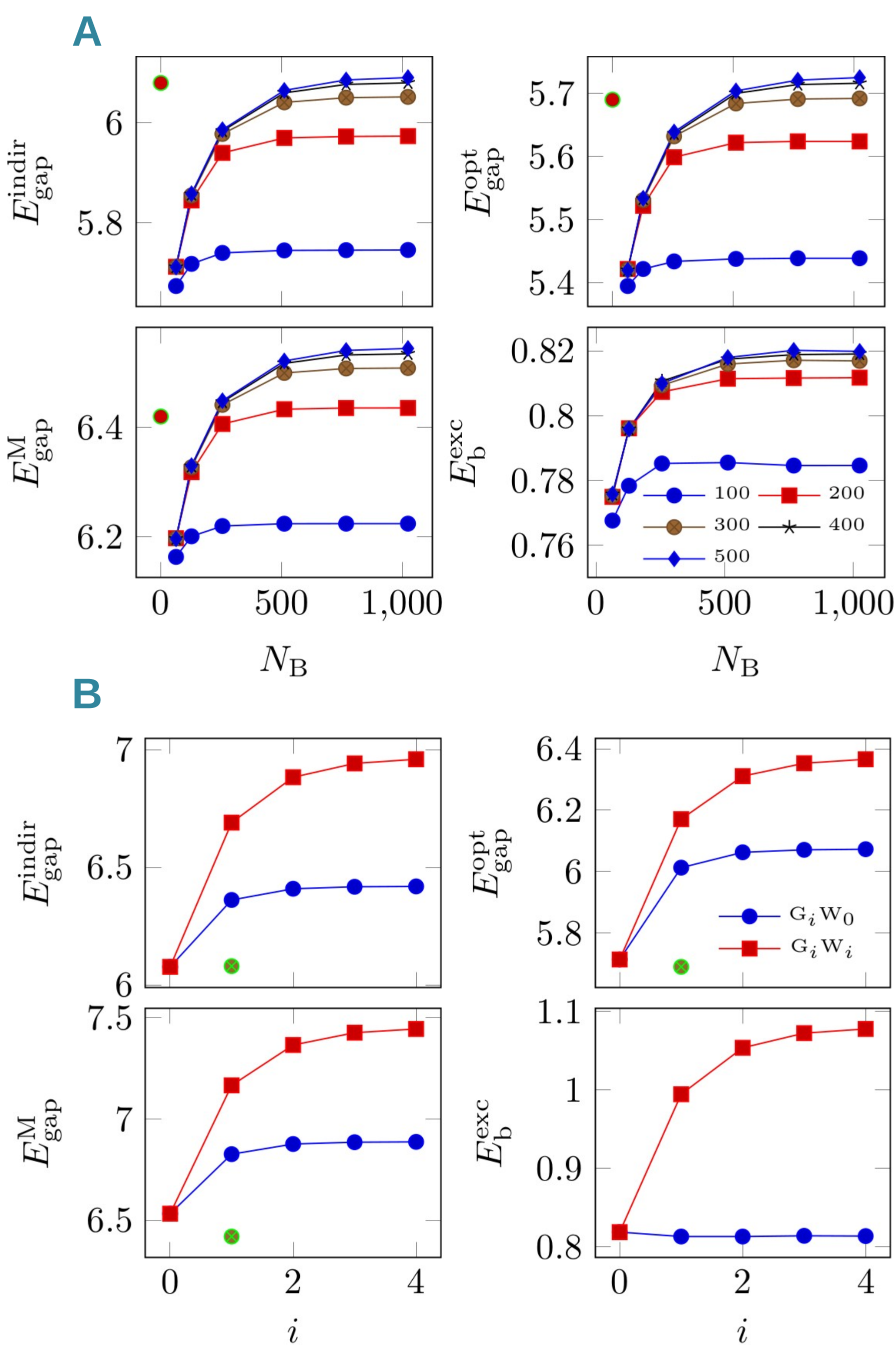


Figure 1. Convergence of h-BN (AA') band gaps E_{gap} (indirect, direct in M, optical) and exciton binding energy $E_{\text{b}}^{\text{exc}} = E_{\text{gap}}^{\text{M}} - E_{\text{b}}^{\text{opt}}$ in eV. A) With respect to GW number of bands N_{B} and energy cut-off E_{cut} (indicated in the legend, in eV); B) With respect to number of iteration i in G_0W_0 and G_0W_1 calculations. $12 \times 12 \times 4$ k-grid was used. Green points are experimental values.^{1,2}

Table 1. Comparison of calculated gap values with experimental values.

	$E_{\text{gap}}^{\text{indir}}$	$E_{\text{gap}}^{\text{M/K}}$	$E_{\text{gap}}^{\text{opt}}$	$E_{\text{b}}^{\text{exc}}$
Calc. AA'	6.08	6.53	5.71	0.82
Calc. AB	6.17	6.39	5.61	0.78
Exp. ^{1,2}	6.08	6.42	5.69	0.73

Results

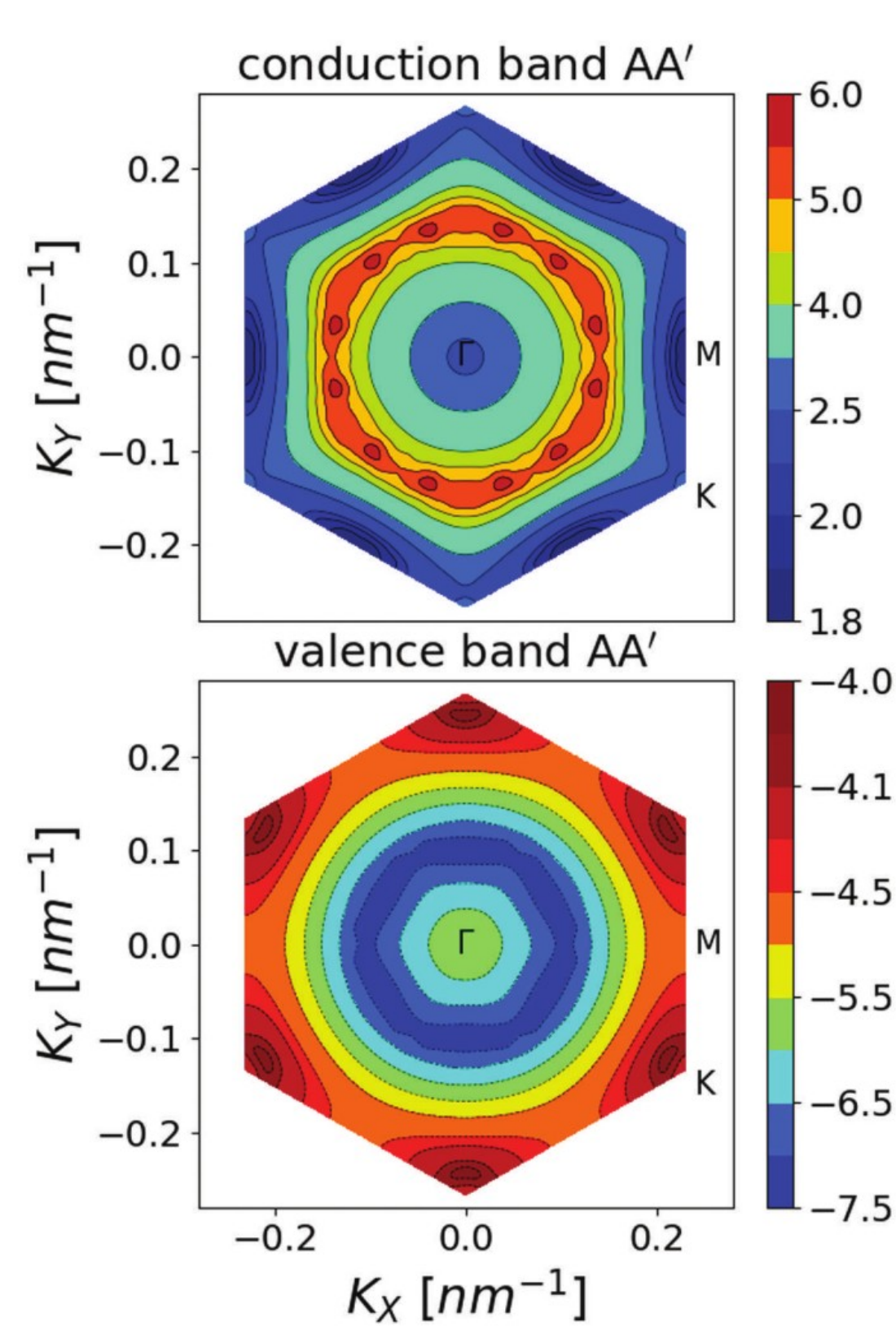


Figure 2. Conduction (top) and valence (bottom) bands of h-BN obtained from G_0W_0 calculation as cuts through the plane G-M-K in the first Brillouin zone.

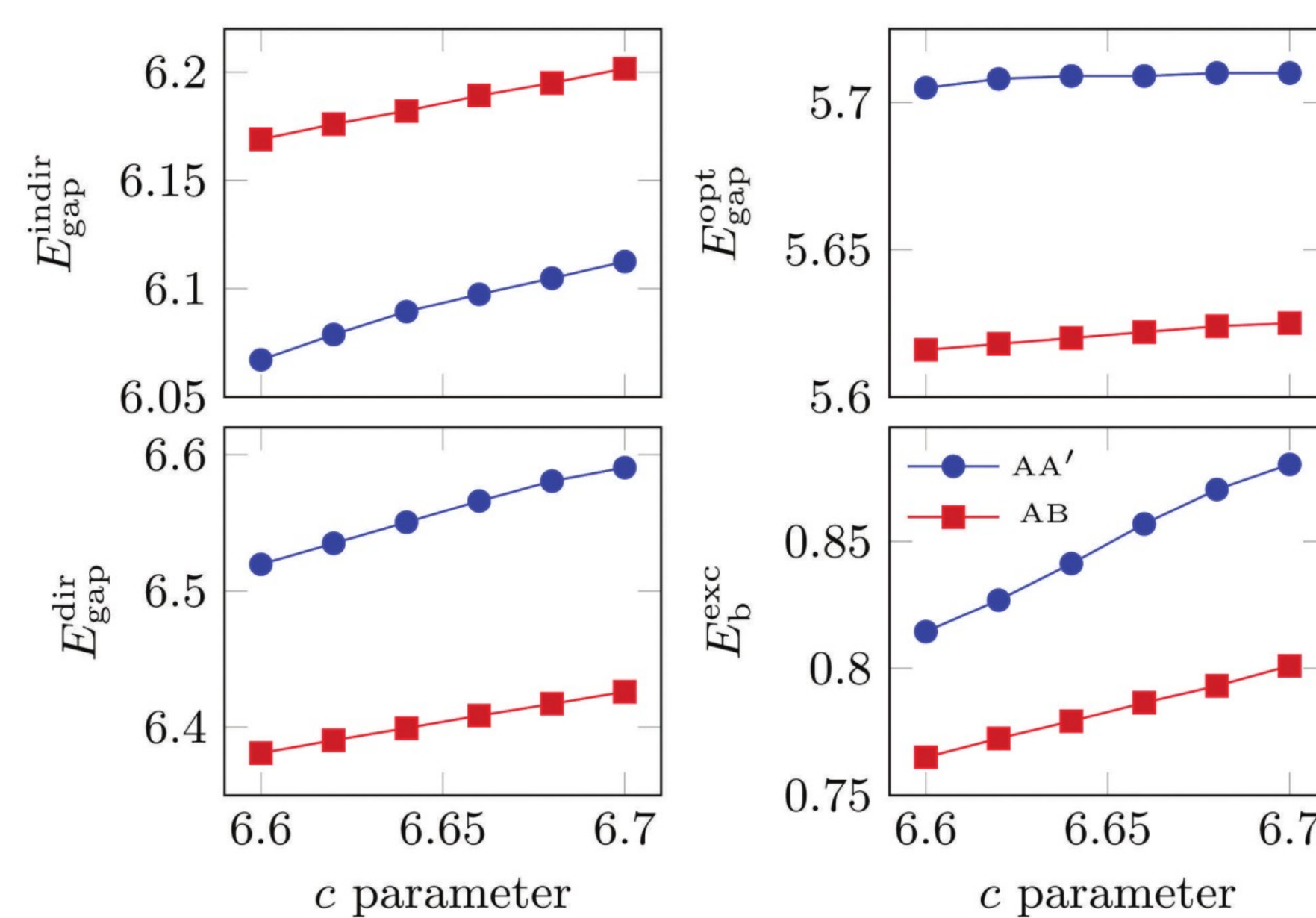


Figure 3. Change in h-BN band gaps E_{gap} (indirect, direct in M, optical) and exciton binding energy $E_{\text{b}}^{\text{exc}} = E_{\text{gap}}^{\text{M}} - E_{\text{b}}^{\text{opt}}$ in eV with respect to c lattice parameter. Two h-BN stacking configurations are considered, AA' and AB.

Simple scissor approximation of h-BN band structures

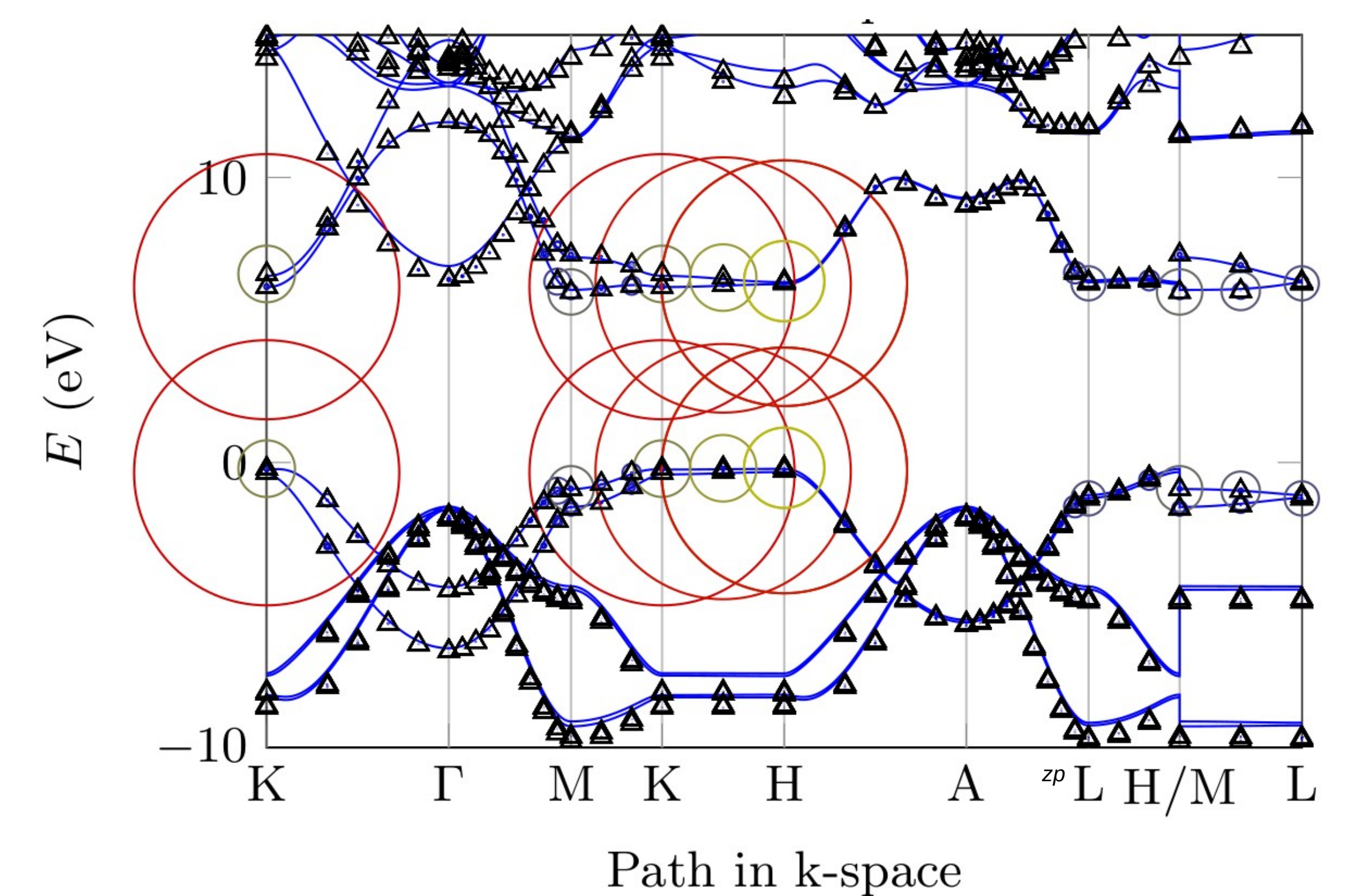


Figure 4. Electronic band structure of h-BN (AA') from G_0W_0 calculation (black triangles) and electron-hole contributions to first excitonic peak from BSE calculation (represented by radius of colored circles). Scissor corrected DFT (PBE) band structure, DFT+ Δ (blue lines), seems a very good approximation to the G_0W_0 band structure. Fermi energy is set as zero.

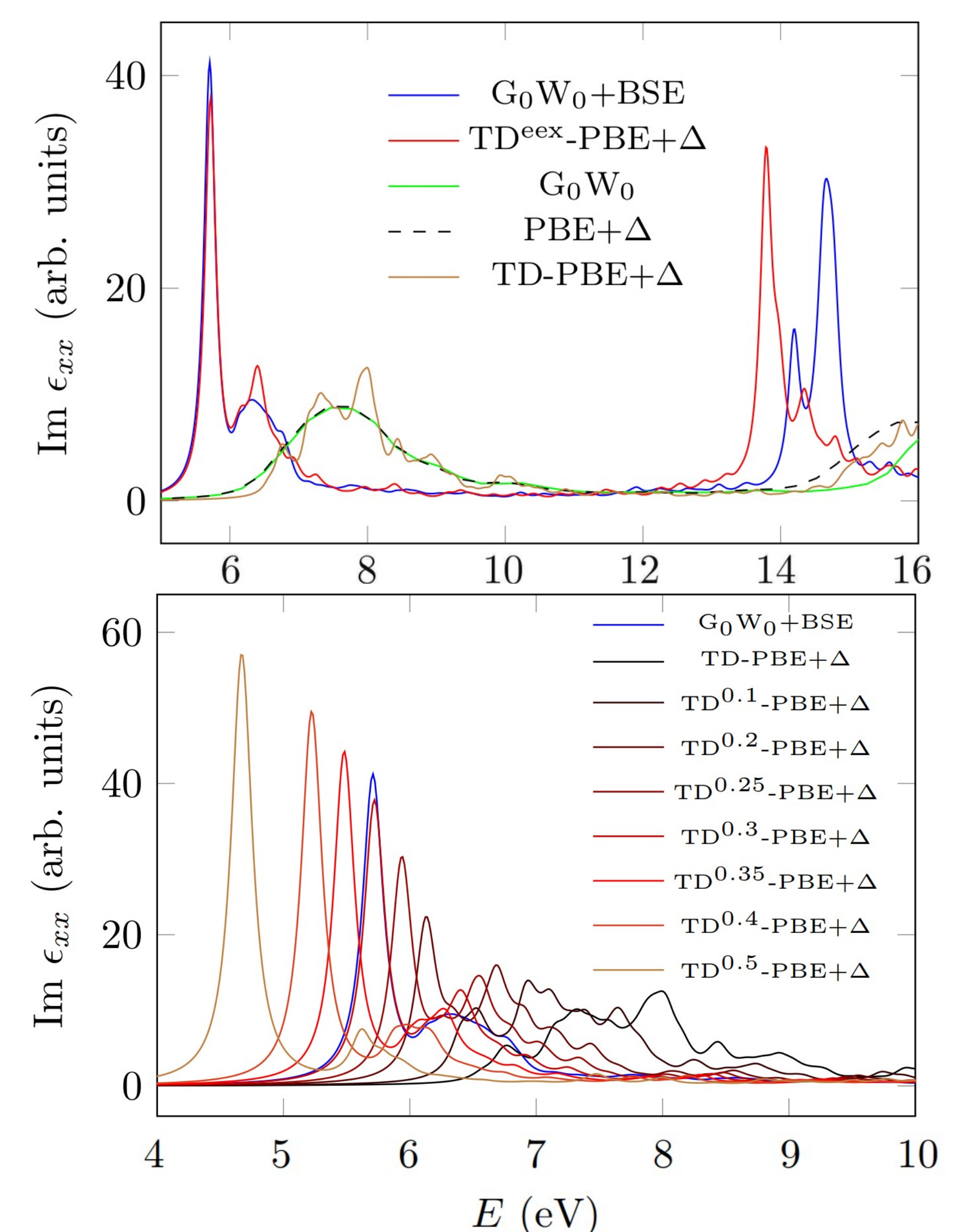


Figure 5. Optical absorption spectra (imaginary part of dielectric function) of h-BN (AA') using various approximate methods and the reference G_0W_0 +BSE curve (blue line). The electron-hole ladder diagrams in present TD-DFT calculations are approximated by the exact exchange (EEX) and different EEX/GGA ratio is evaluated (and labeled by the EEX part as $\text{TD}^{\text{EEX}}\text{-PBE}+\Delta$). We achieve surprisingly good approximation with EEX/GGA ratio of 0.3/0.7.

Conclusions

Our carefully converged results reveal h-BN as an indirect material (indirect gap $\approx 6.1 \text{ eV}$) with a huge excitonic effect ($\approx 0.8 \text{ eV}$) in agreement with recent revolutionary experiments^{1,2}. Variability of previous theoretical predictions and our convergence tests indicate that many-body methods should be used carefully, and numerical convergence should always be performed. On the other hand, based on benchmark G_0W_0 results, we suggest a computationally cheap scissor corrected DFT approach providing band structure comparable with the G_0W_0 band structure. Time-dependent DFT with a suitable exchange-correlation kernel can provide absorption spectra that mimic the full G_0W_0 +BSE spectra.

Acknowledgments

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References

- ¹G. Cassabois, P. Valvin and B. Gil, Nat. Photonics, 2016, 10, 262–266;
- ²T. C. Doan, J. Li, J. Y. Lin and H. X. Jiang, Appl. Phys. Lett., 2016, 109, 122101.
- ³G. Kresse and D. Joubert, Phys. Rev. B 59, 1758 (1999);
- ⁴L. Hedin, Phys. Rev., 1965, 139, A796–A823;
- ⁵J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996);
- ⁶H. Bethe and E. Salpeter, Phys. Rev., 1951, 82, 309–310.