



Direct/indirect band gap and exciton dispersion: Monolayer and bulk hexagonal boron nitride

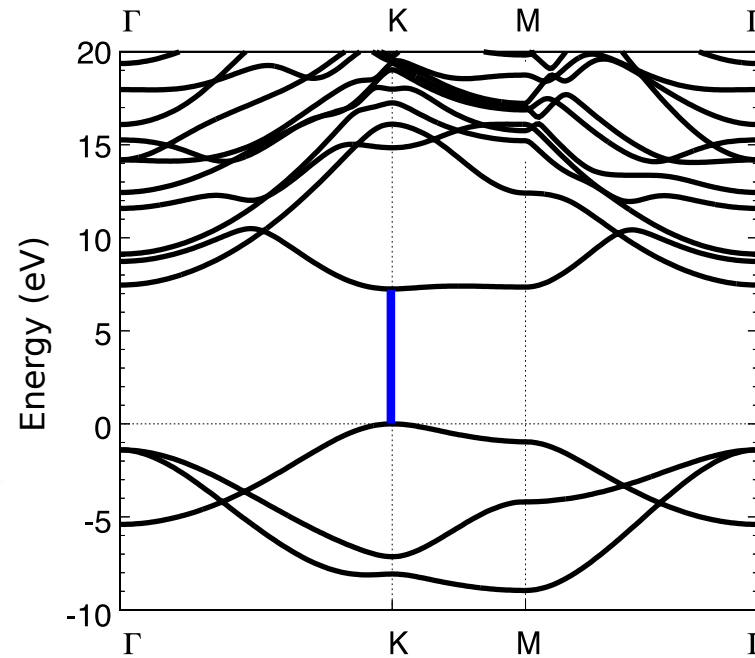
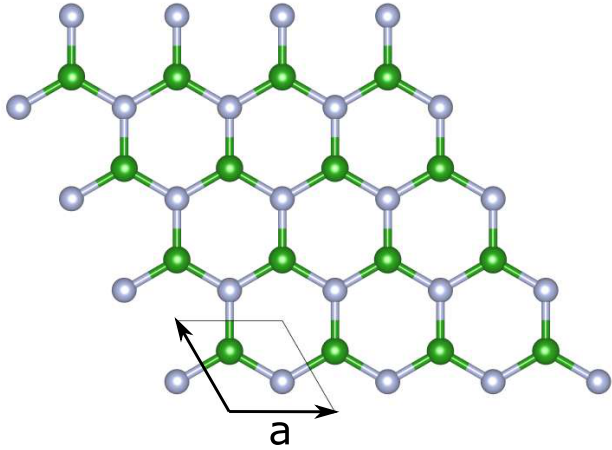
L. Sponza, L. Schué, H. Amara, C. Attaccalite, F. Ducastelle, A. Loiseau, J. Barjon

Outlook

- **The curious spectra of hexagonal boron nitride (hBN)**
contradiction between electronic and optical properties
modeling free carriers and excitons
- **Tight-binding model of the exciton**
validation of the model in the monolayer
insight from the monolayer to the bulk
- **Ab initio exciton dispersion in bulk hBN**
conciliation of the contradictions (theory)
experimental evidences
- **Predictions about the Bernal stacking**

Hexagonal boron nitride: electronic structure

Monolayer



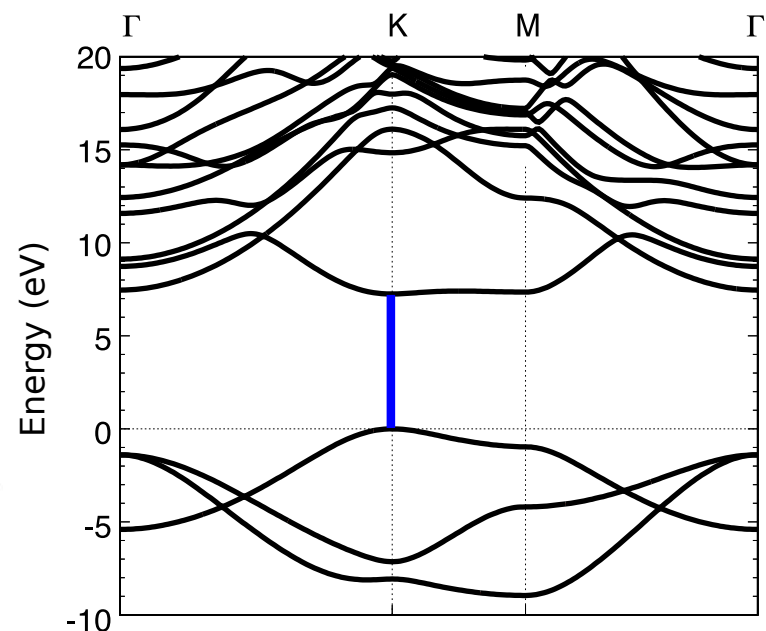
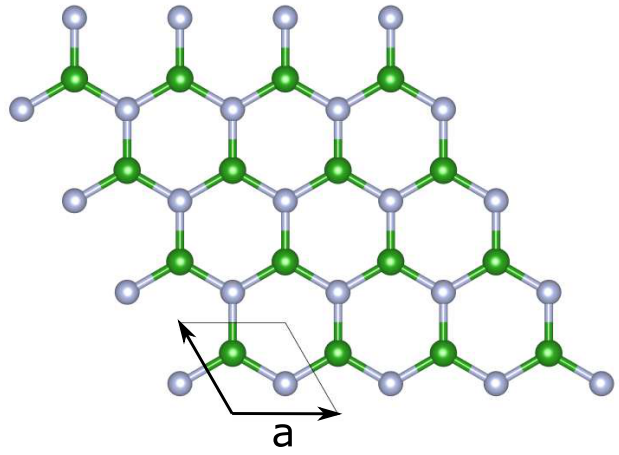
quasiparticle gap
GGA + 2.75 eV

direct K 7.25 eV

indirect KM 7.35 eV

Hexagonal boron nitride: electronic structure

Monolayer

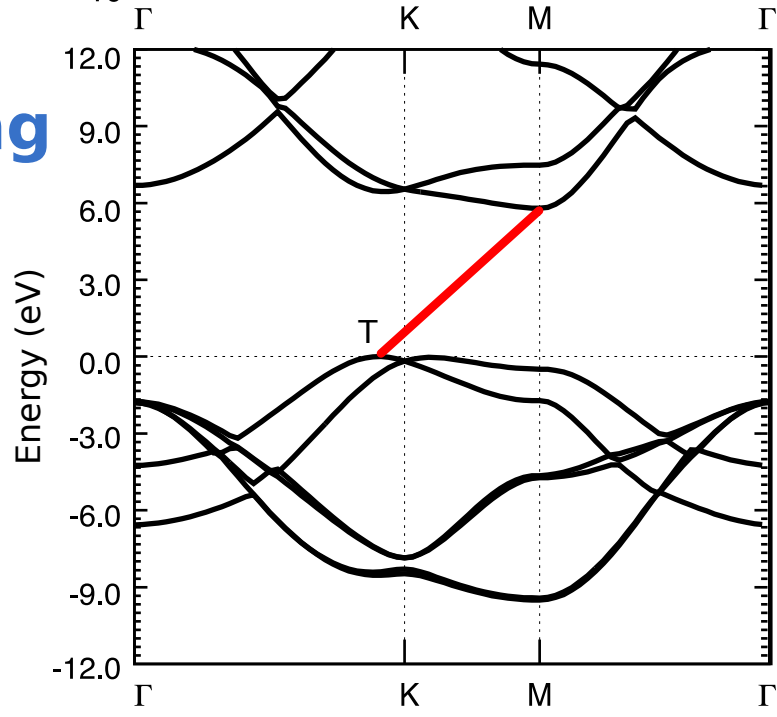
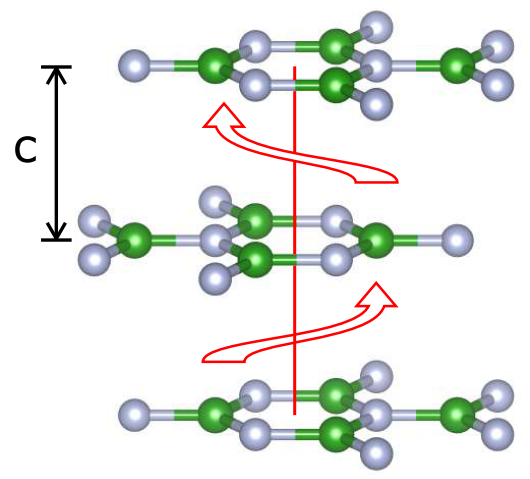


quasiparticle gap
GGA + 2.75 eV

direct K 7.25 eV

indirect KM 7.35 eV

Bulk: AA' stacking



quasiparticle gap
LDA + G_0W_0

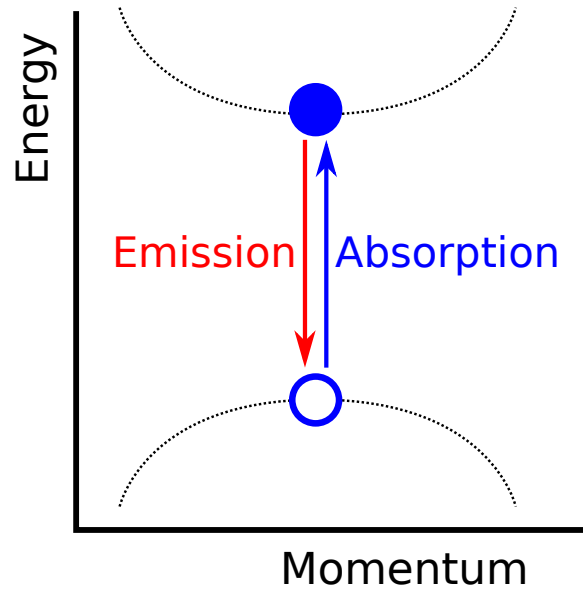
direct T 6.45 eV

direct M 6.28 eV

indirect TM 5.80 eV

Expectations from direct and indirect gaps

Direct gap



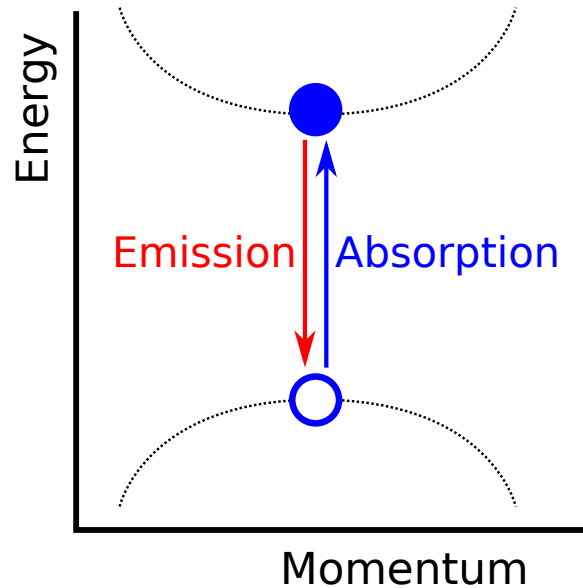
coupling only
to **photons ($q=0$)**



- High probability
- High efficiency

Expectations from direct and indirect gaps

Direct gap

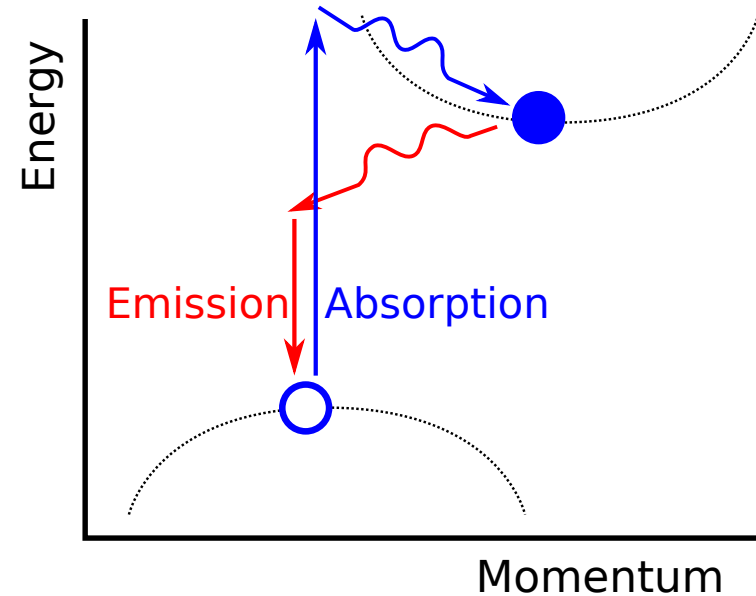


coupling only
to **photons ($q=0$)**



- High probability
- High efficiency

Indirect gap

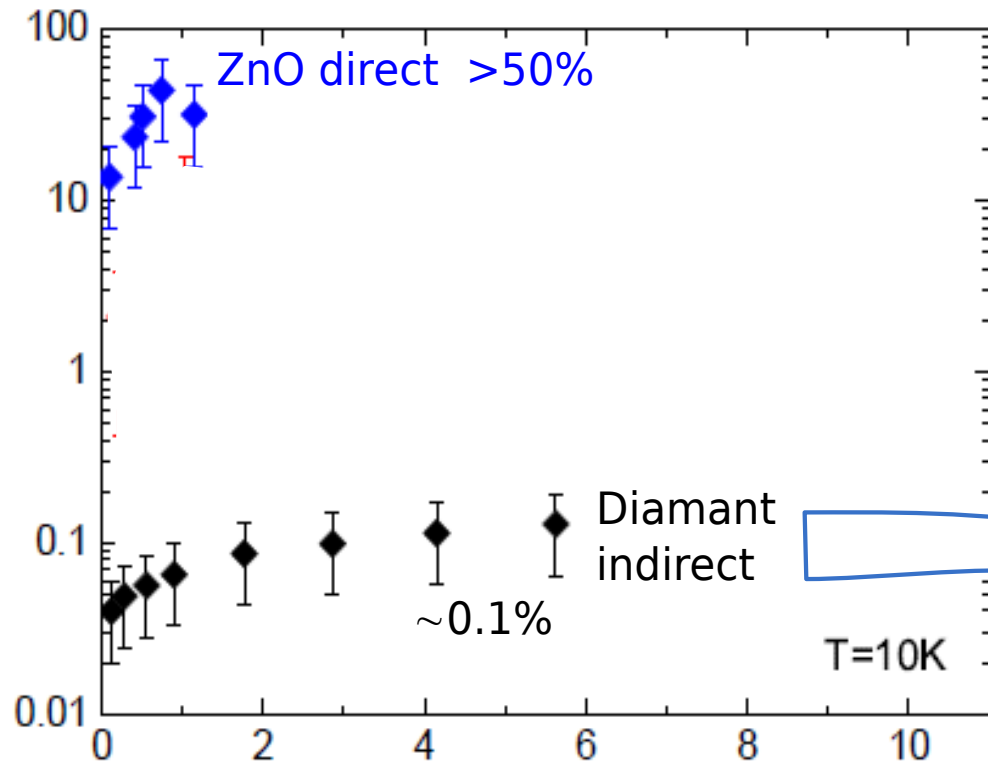


coupling
to **photons ($q=0$)**
and **phonons ($q\neq 0$)**

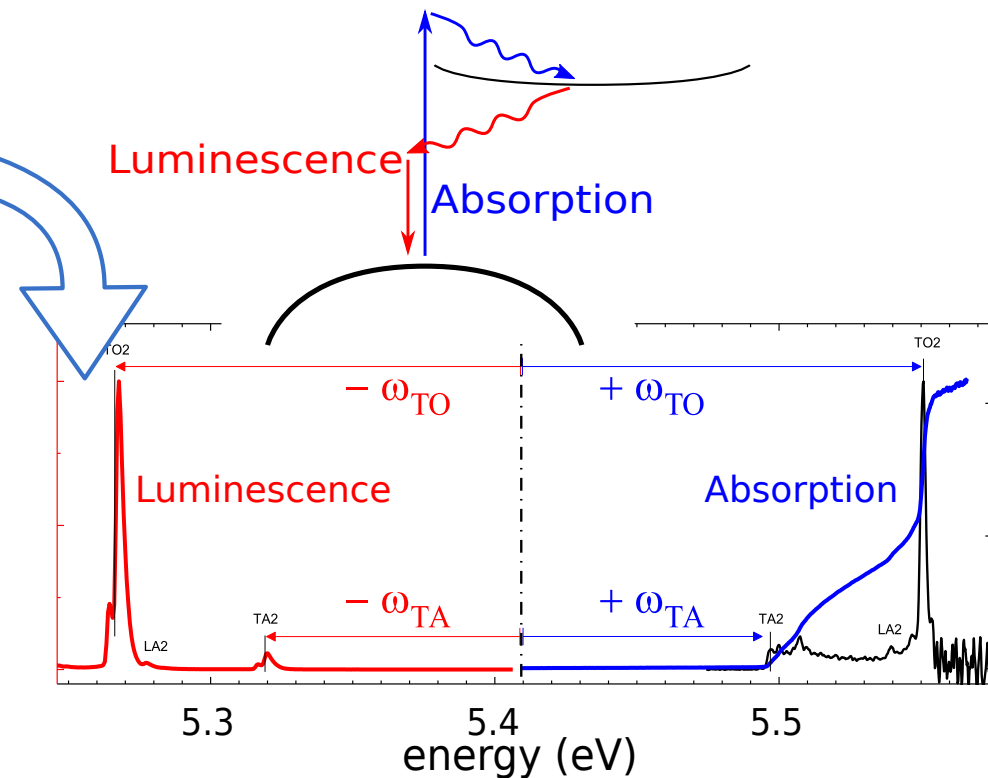


- Low probability
- Low efficiency

Experimental luminescence of bulk hBN

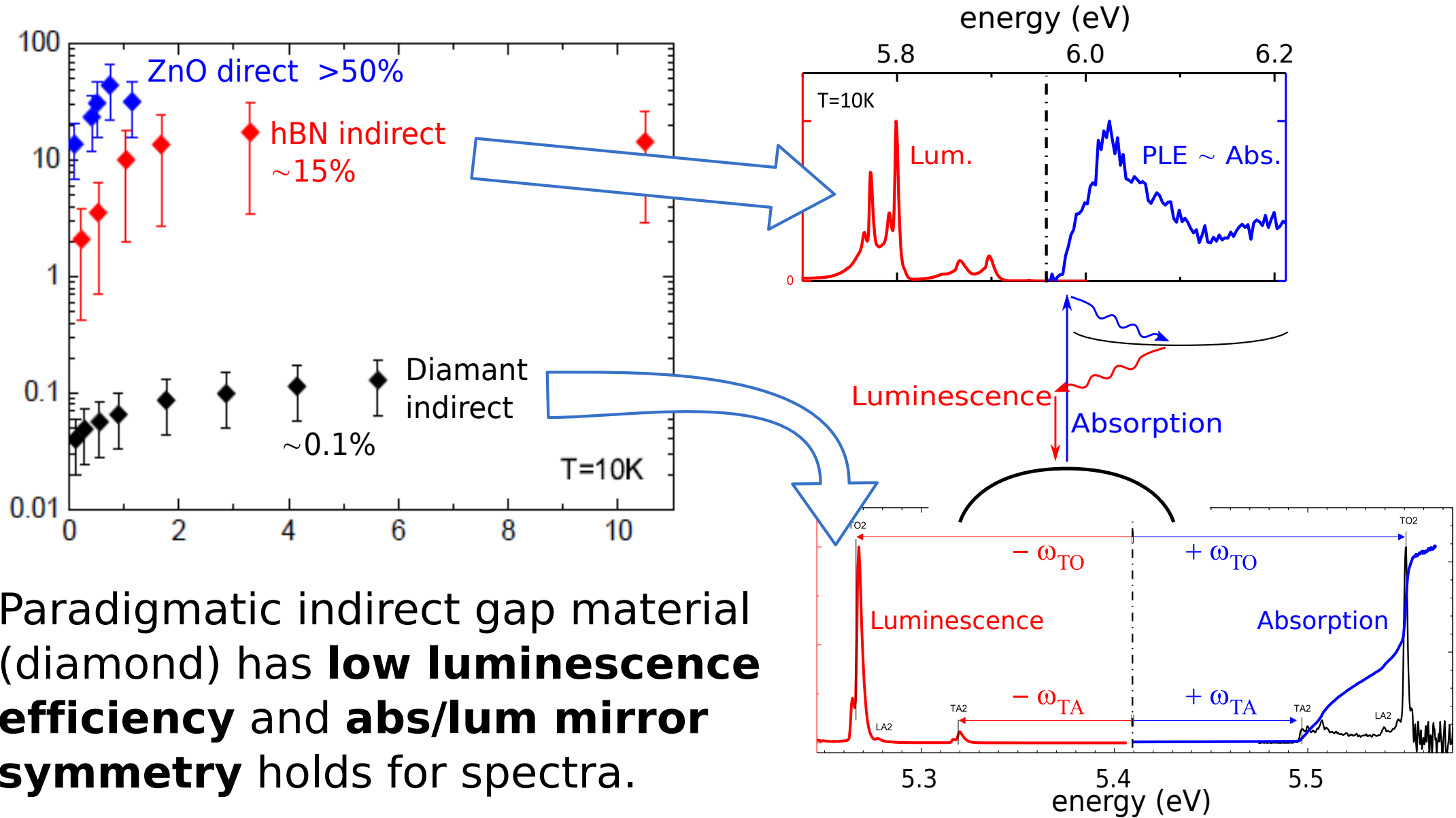


Paradigmatic indirect gap material (diamond) has **low luminescence efficiency** and **abs/lum mirror symmetry** holds for spectra.



Experimental luminescence of bulk hBN

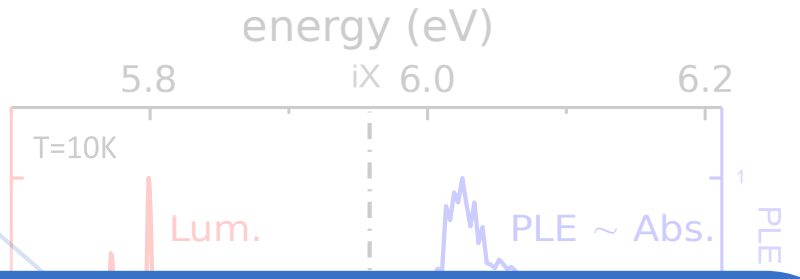
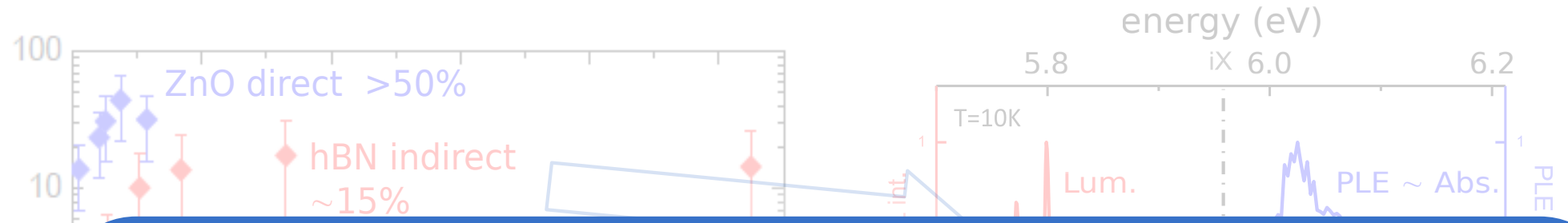
High luminescence efficiency No abs/lum mirror symmetry



Paradigmatic indirect gap material (diamond) has **low luminescence efficiency** and **abs/lum mirror symmetry** holds for spectra.

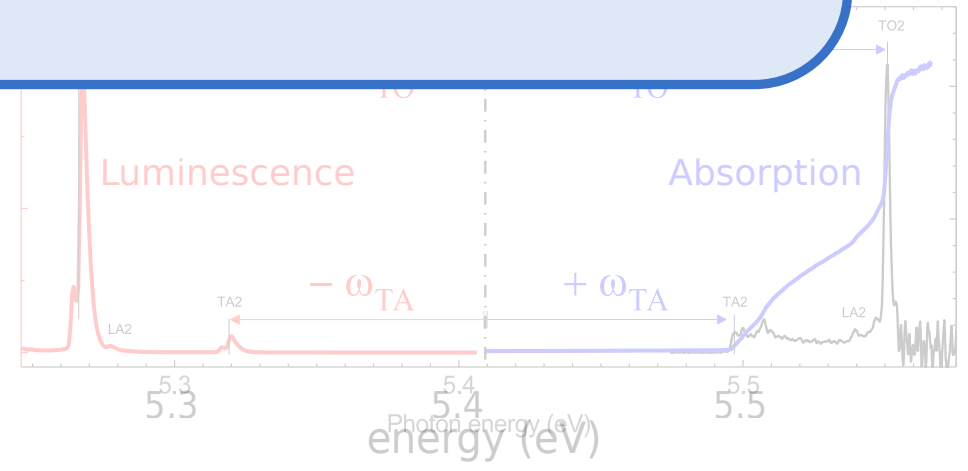
Experimental luminescence of bulk hBN

High luminescence efficiency No abs/lum mirror symmetry



Despite the indirect gap of bulk hBN, luminescence efficiency is very high and abs/lum specularity does not hold

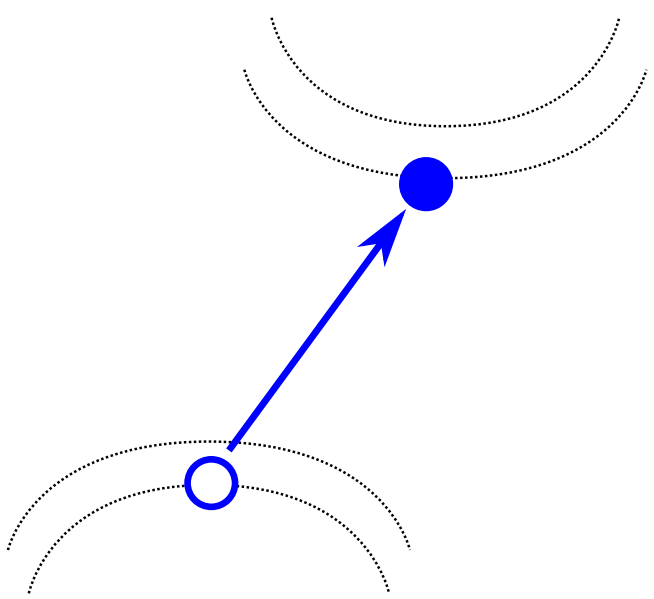
Paradigmatic indirect gap material (diamond) has **low luminescence efficiency** and **abs/lum mirror symmetry** holds for spectra.



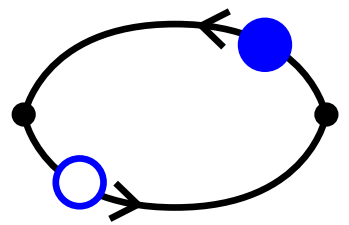
1-particle and 2-particle excitations

Free carriers: electron + hole

Quasiparticle: scissor, GW...
two 1-particle propagators

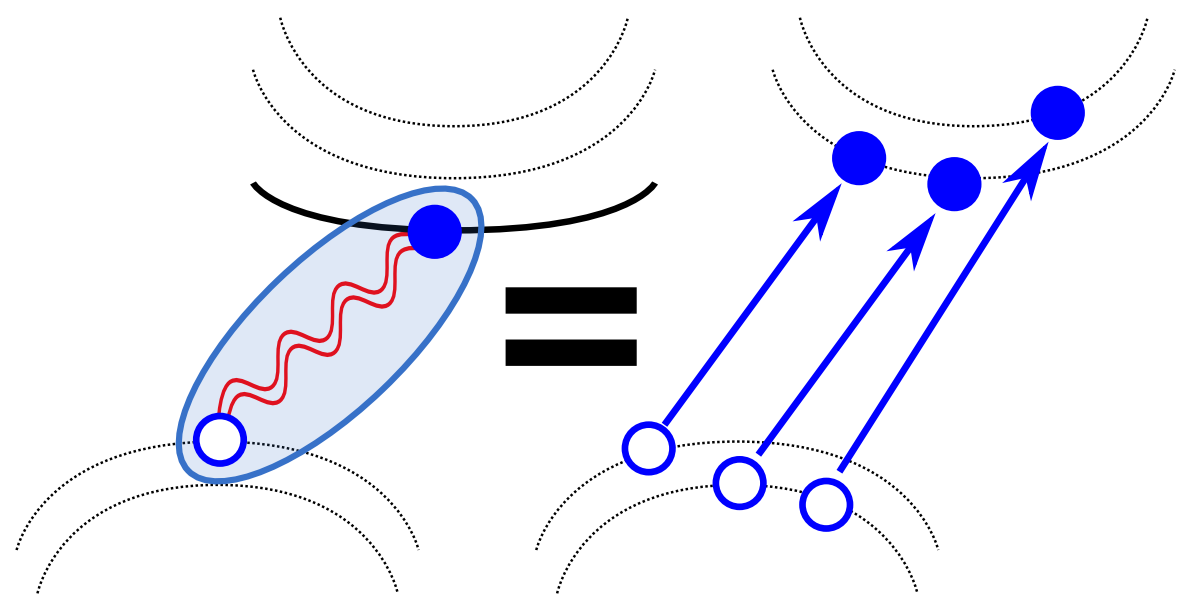


Dipole-allowed transitions between points of the **band structure**.

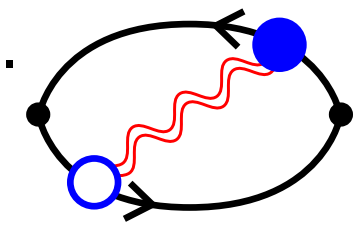


Exciton: electron-hole pair

Bethe-Salpeter equation
single 2-particle propagator

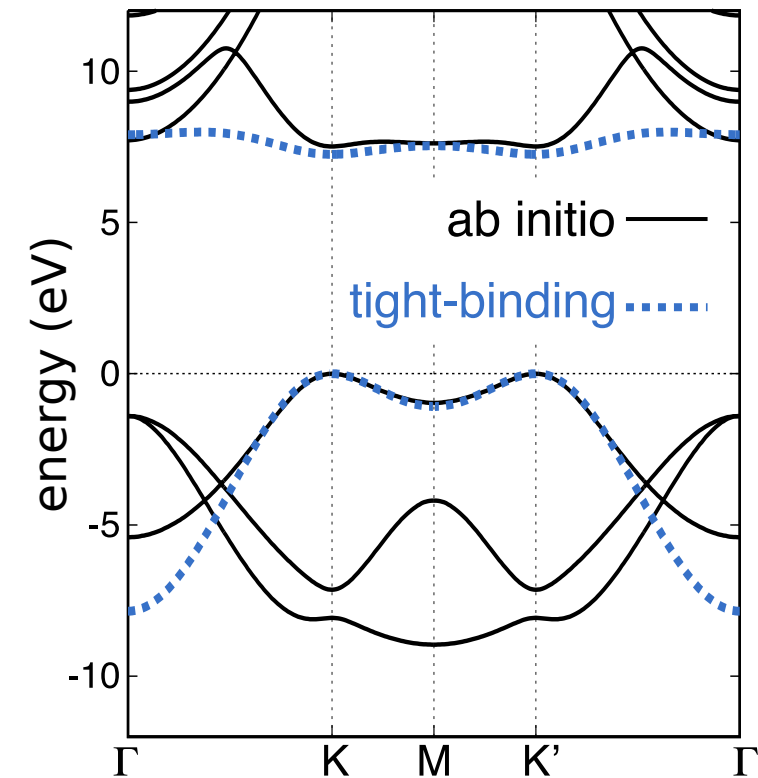
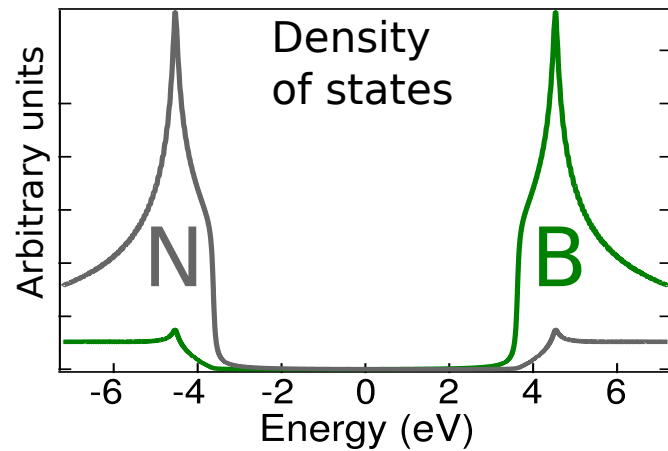


Excitonic Hamiltonian on a basis of free carriers.
Excitonic levels.



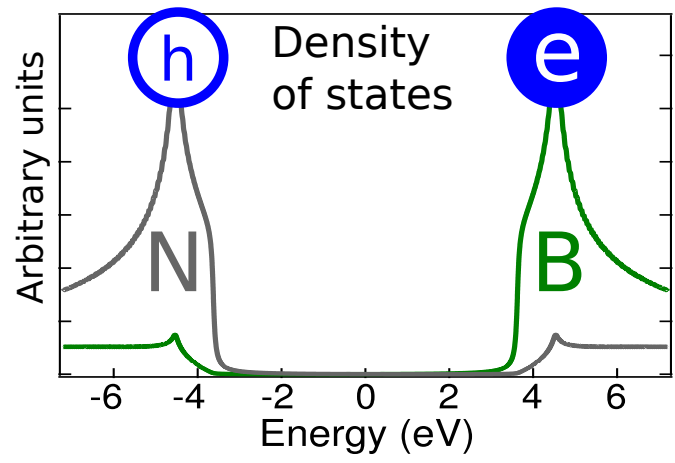
1-particle and 2-particle excitations

1-particle model



1-particle and 2-particle excitations

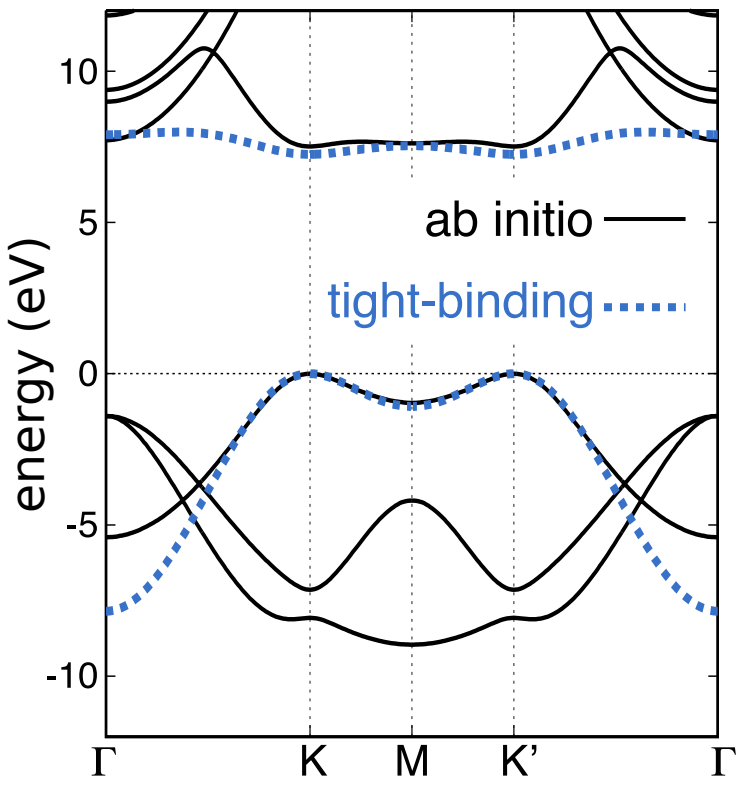
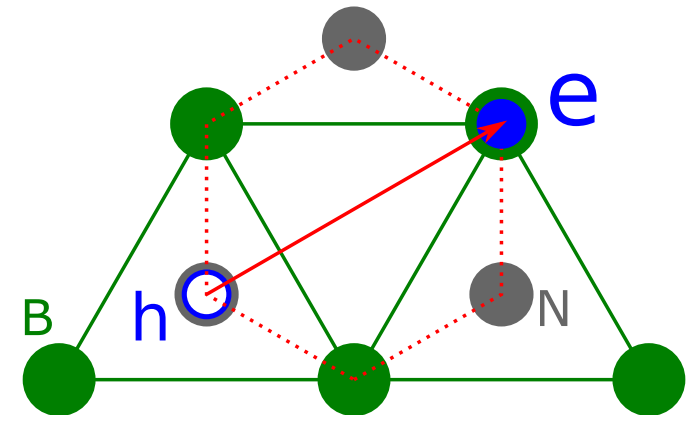
1-particle model



Excitonic model

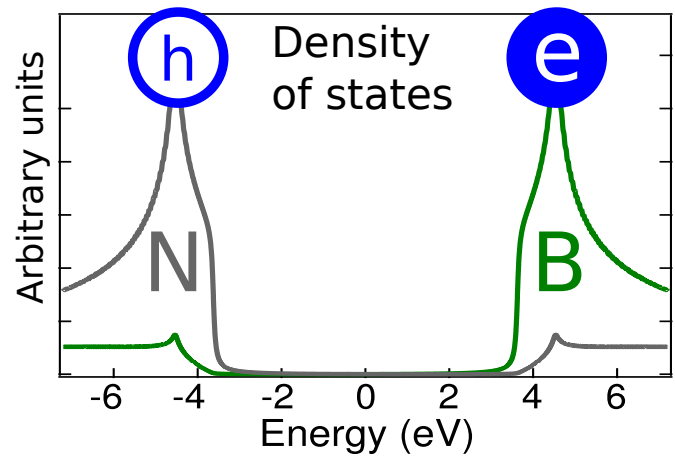
T. Galvani, PRB **94** (2016)

1-particle
triangular lattice
attractive source



1-particle and 2-particle excitations

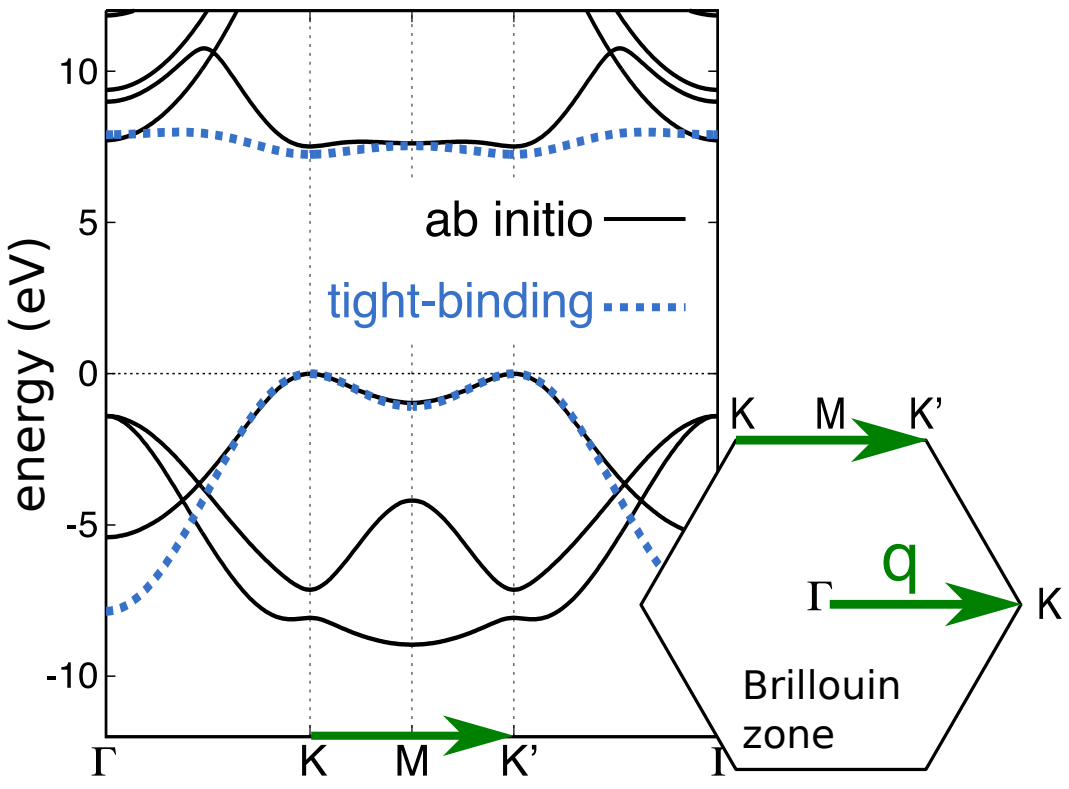
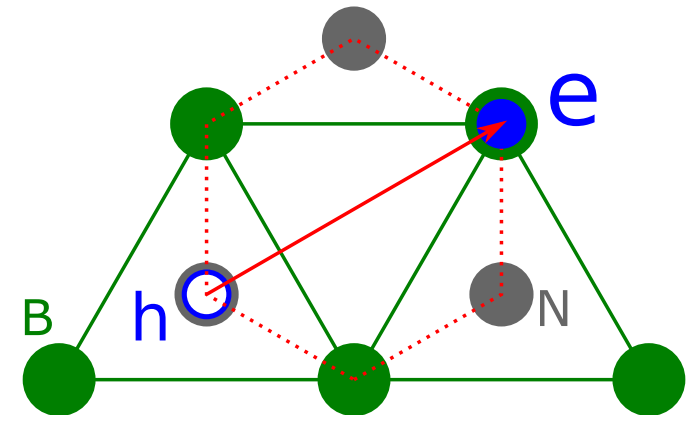
1-particle model



T. Galvani, PRB **94** (2016)

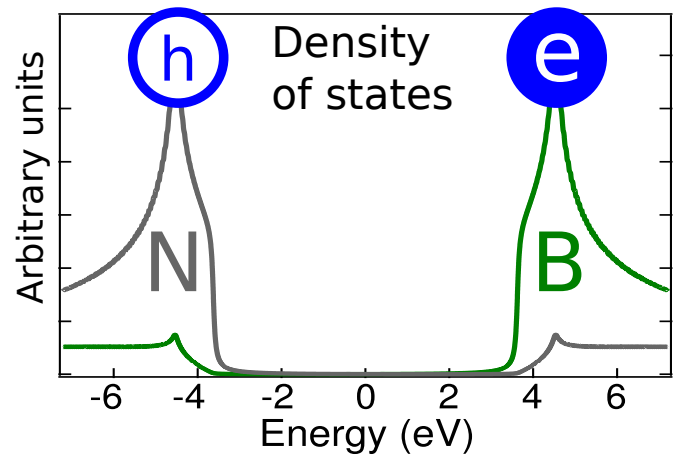
1-particle
triangular lattice
attractive source

Excitonic model



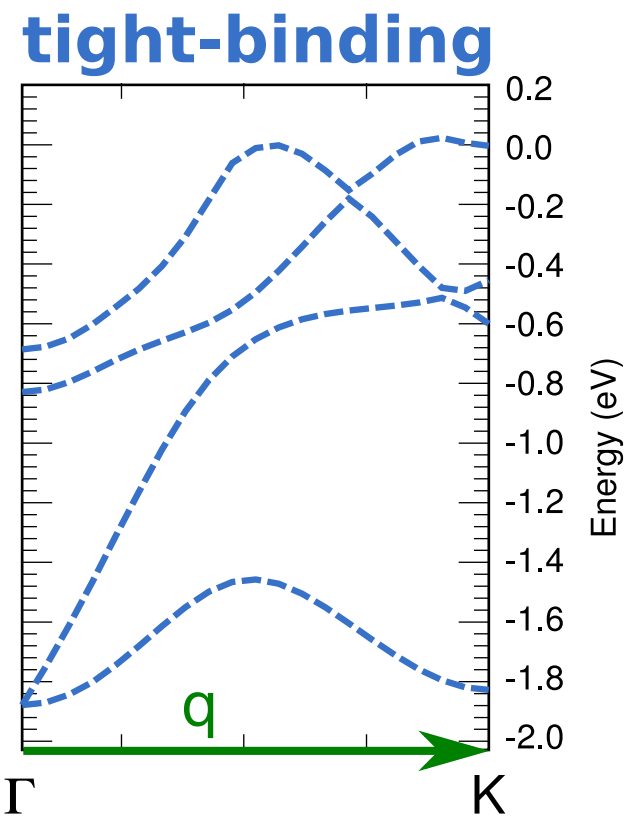
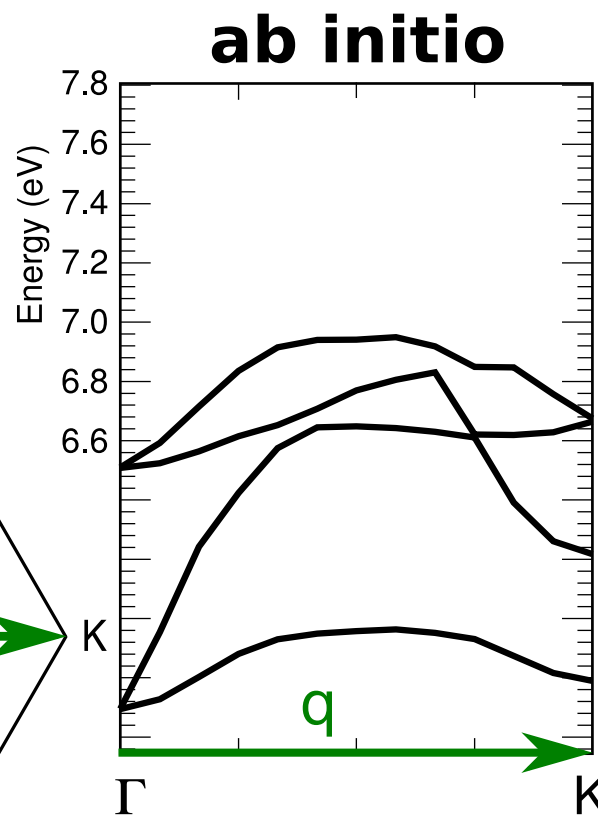
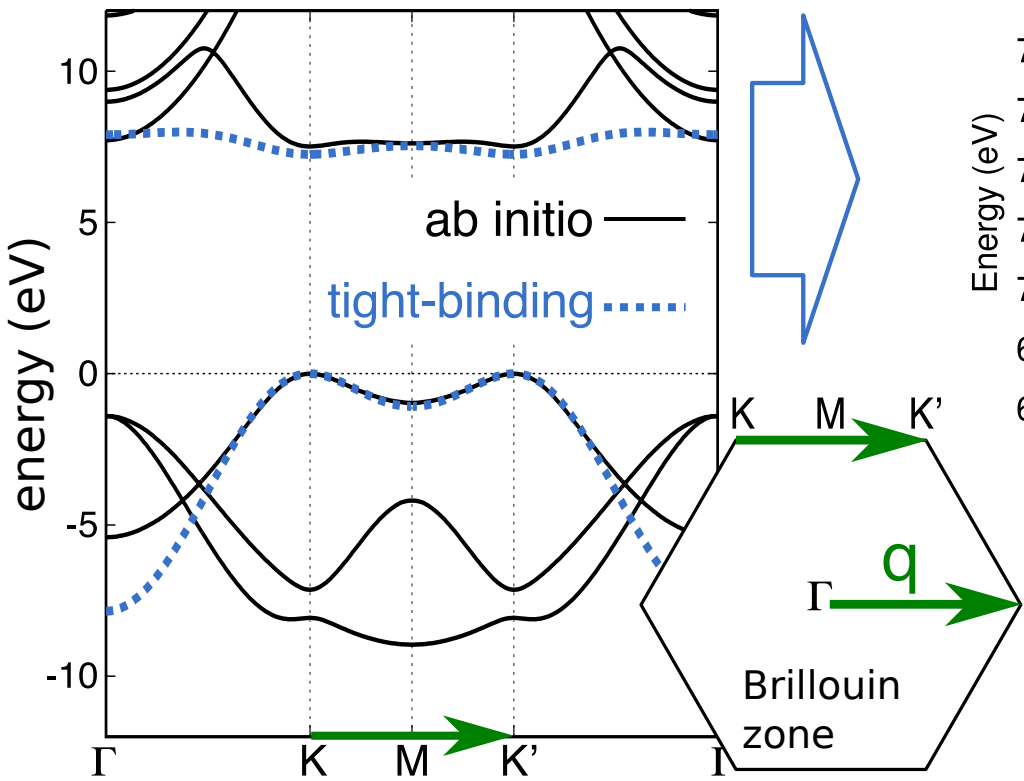
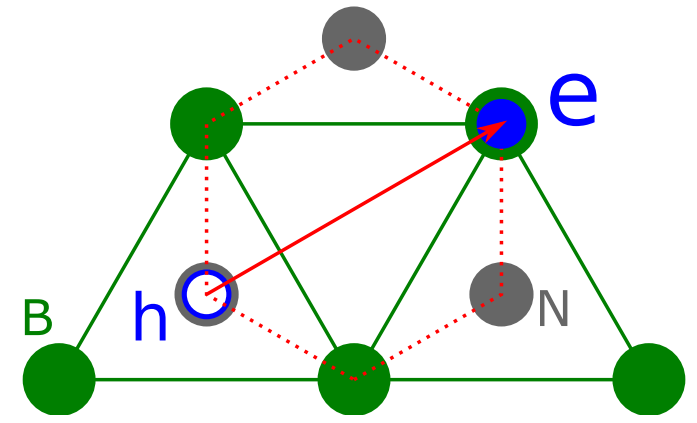
1-particle and 2-particle excitations

1-particle model

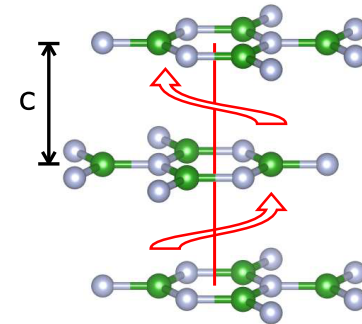
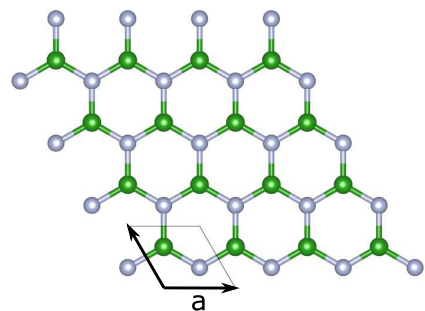


T. Galvani, PRB **94** (2016)
1-particle
 triangular lattice
 attractive source

Excitonic model



From monolayer to bulk AA'

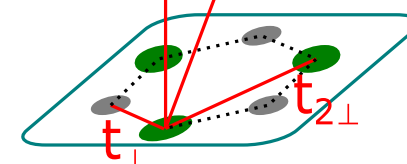
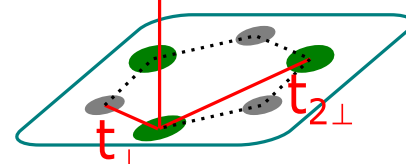
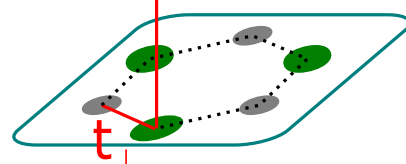
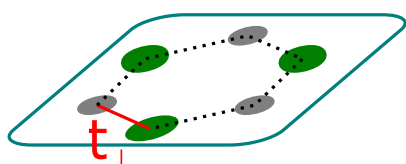
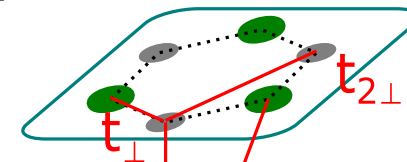
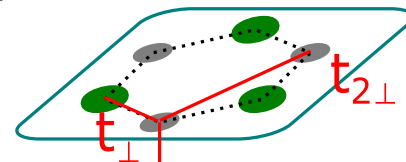
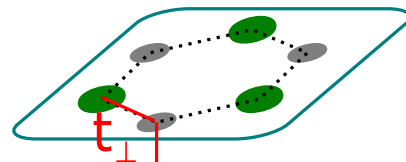
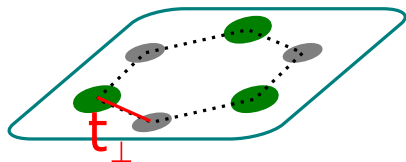
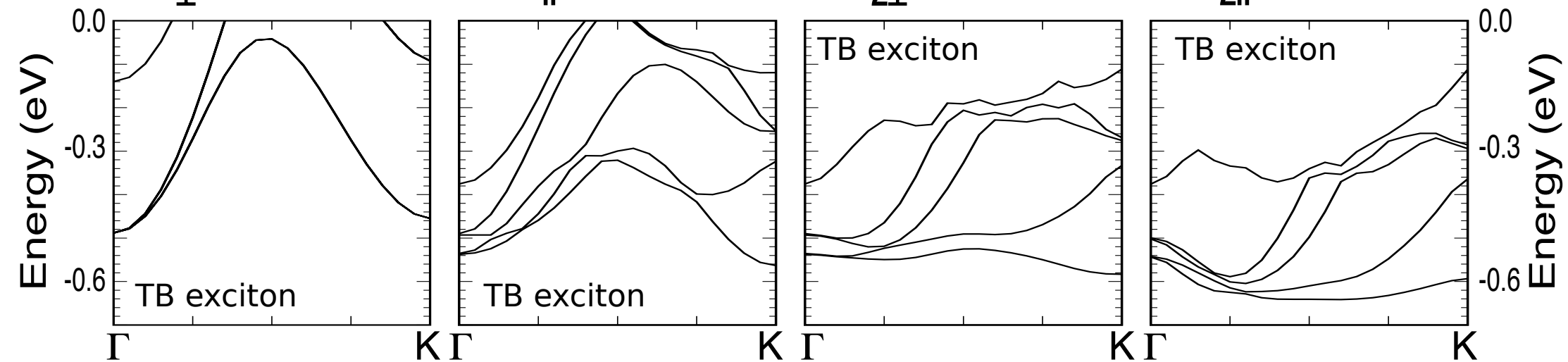


$t_{\perp} = -2.33 \text{ eV}$

$t_{\parallel} = 0.5 \text{ eV}$

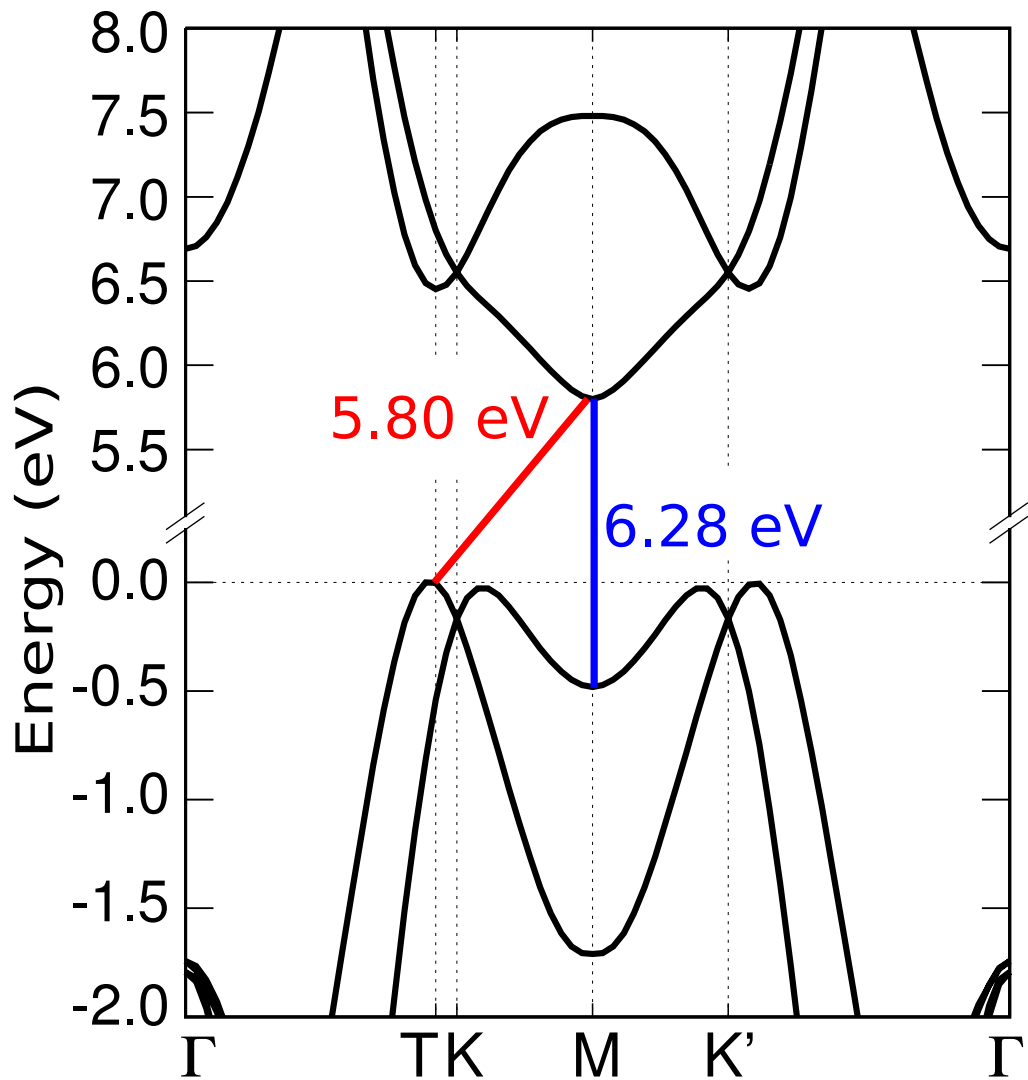
$t_{2\perp} = -0.4 \text{ eV}$

$t_{2\parallel} = -0.1 \text{ eV}$



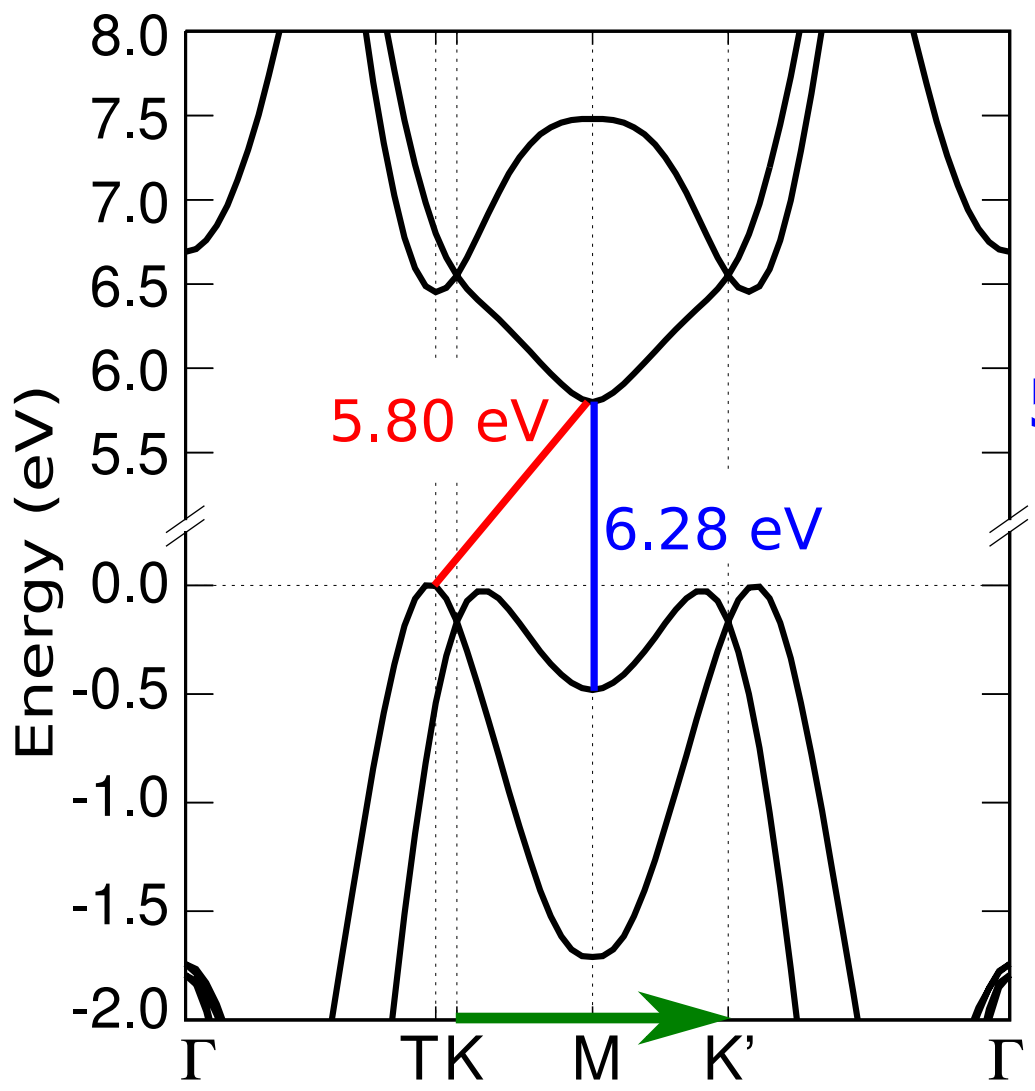
Exciton dispersion in bulk AA'

ab-initio band structure

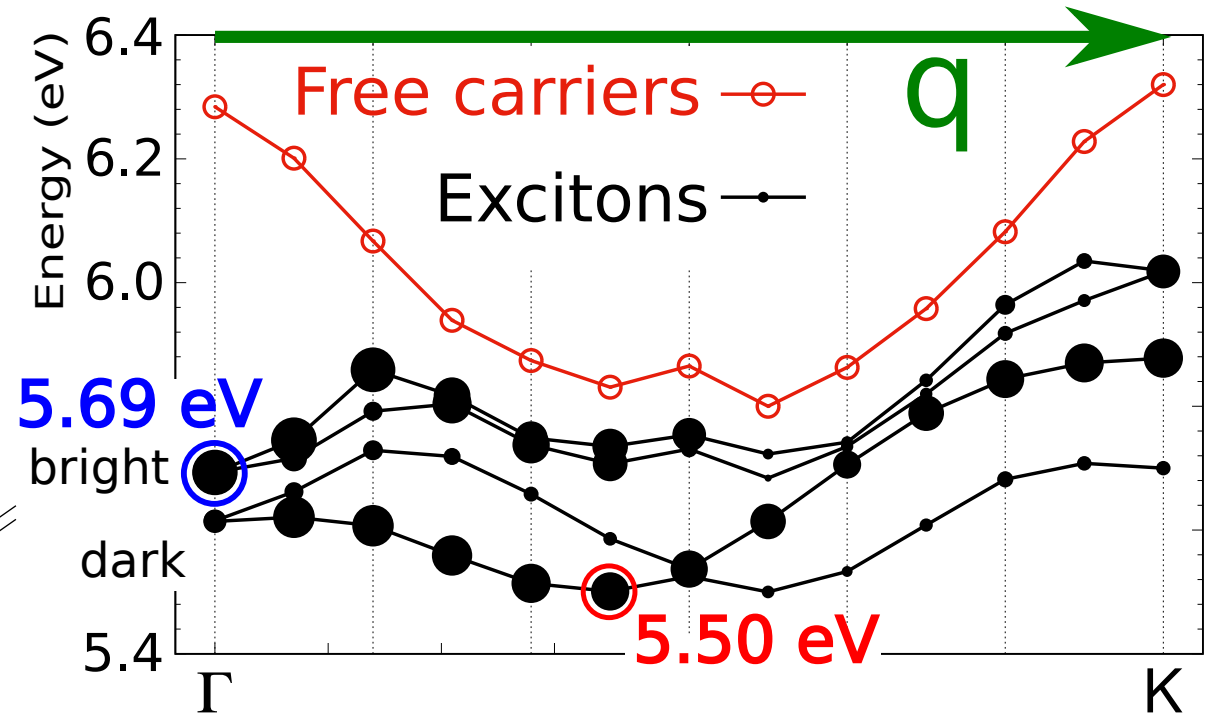


Exciton dispersion in bulk AA'

ab-initio band structure



ab initio e-h dispersion



Variations of the binding energy lead to a flattening of the excitonic dispersion.

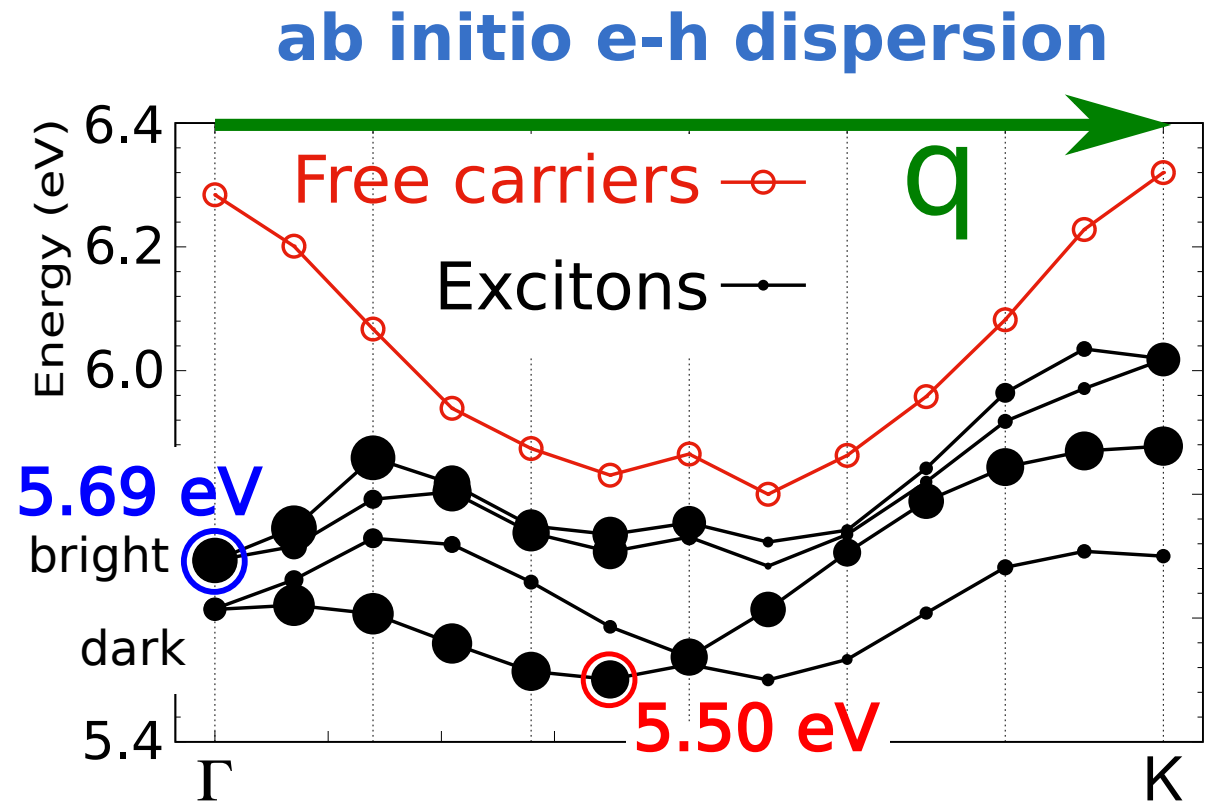
Direct (bright) and indirect excitons lie within 0.2 eV.

Consistent explanation of the optical properties

Flat dispersion = localized e-h

a) Electron and hole spatially close (high overlap)

b) Strong exciton-phonon coupling.



Consistent explanation of the optical properties

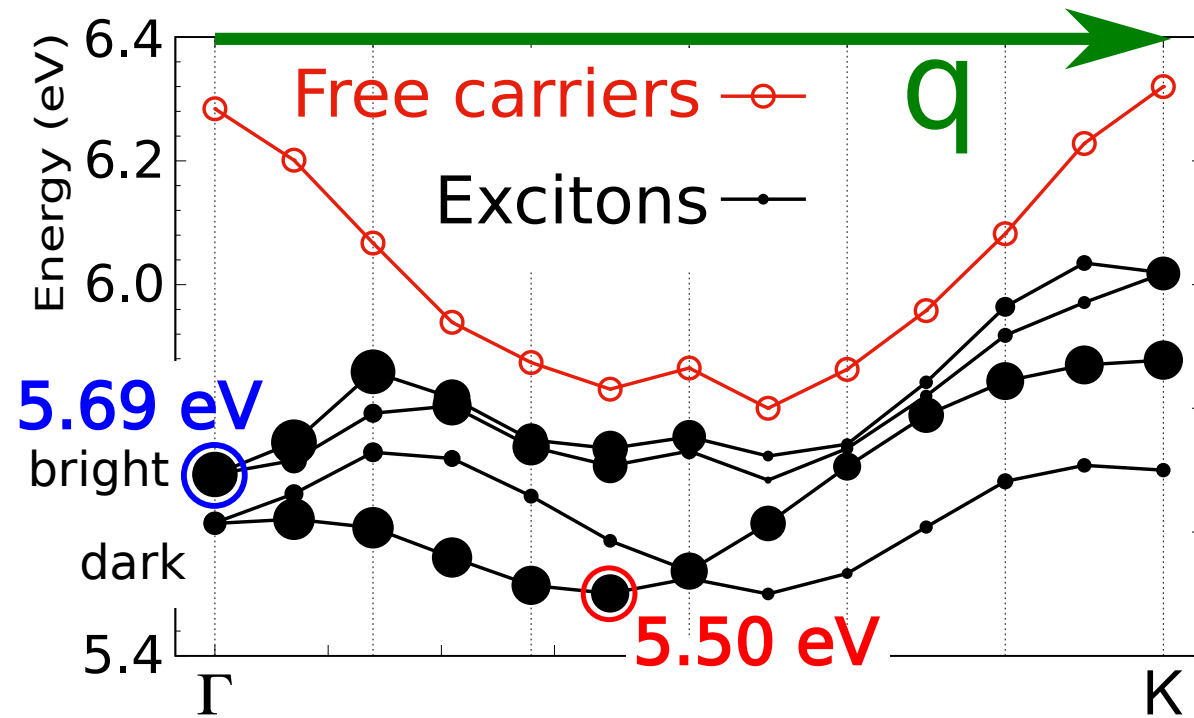
Flat dispersion = localized e-h

a) **Electron and hole spatially close** (high overlap)

b) **Strong exciton-phonon coupling.**

1) high probability for radiative recombination (phonon-mediated)

ab initio e-h dispersion



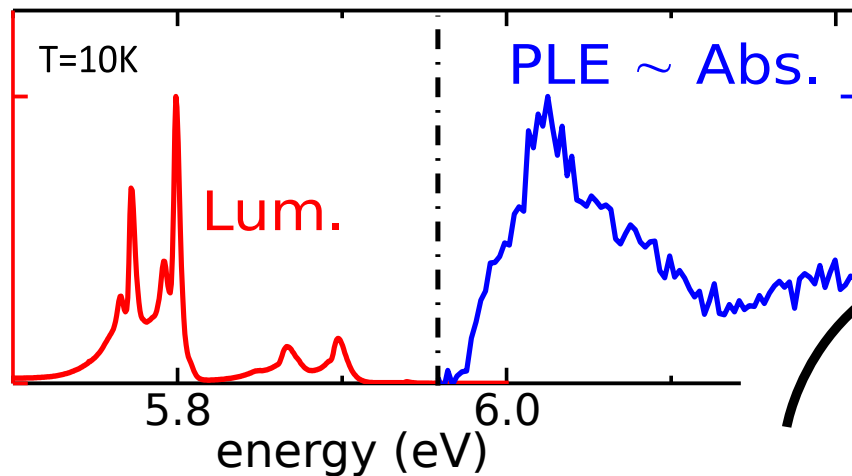
Consistent explanation of the optical properties

Flat dispersion = localized e-h

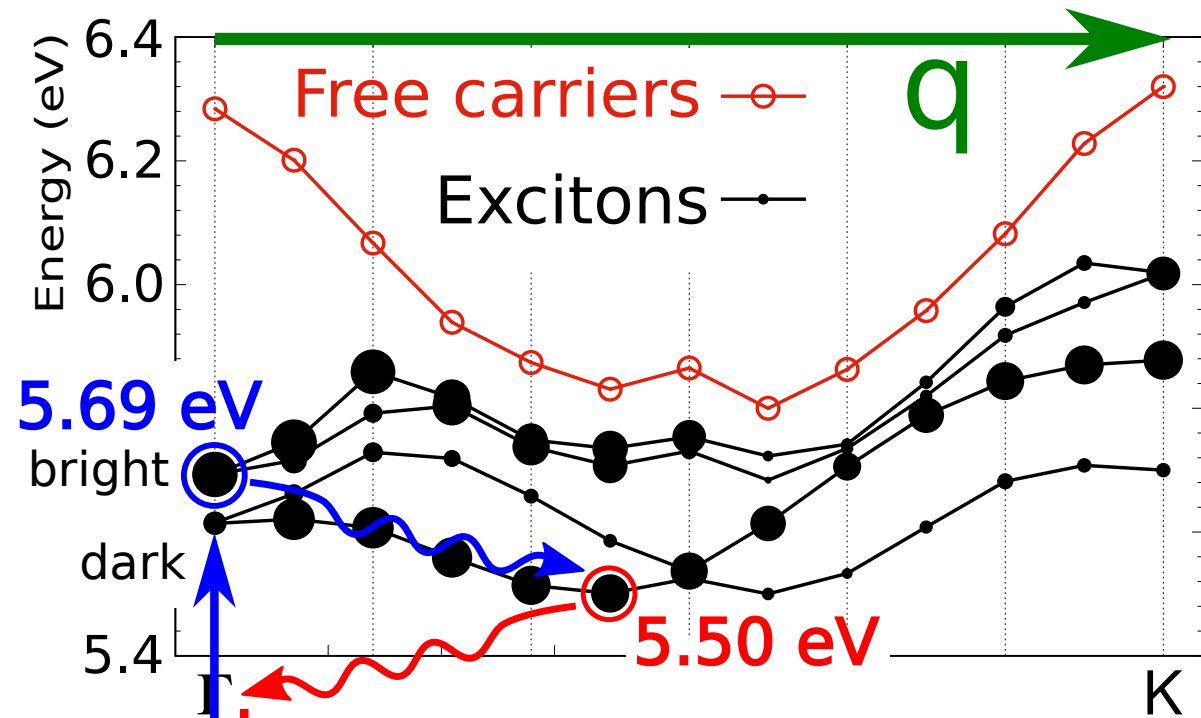
a) **Electron and hole spatially close** (high overlap)

b) **Strong exciton-phonon coupling.**

1) **high probability for radiative recombination (phonon-mediated)**



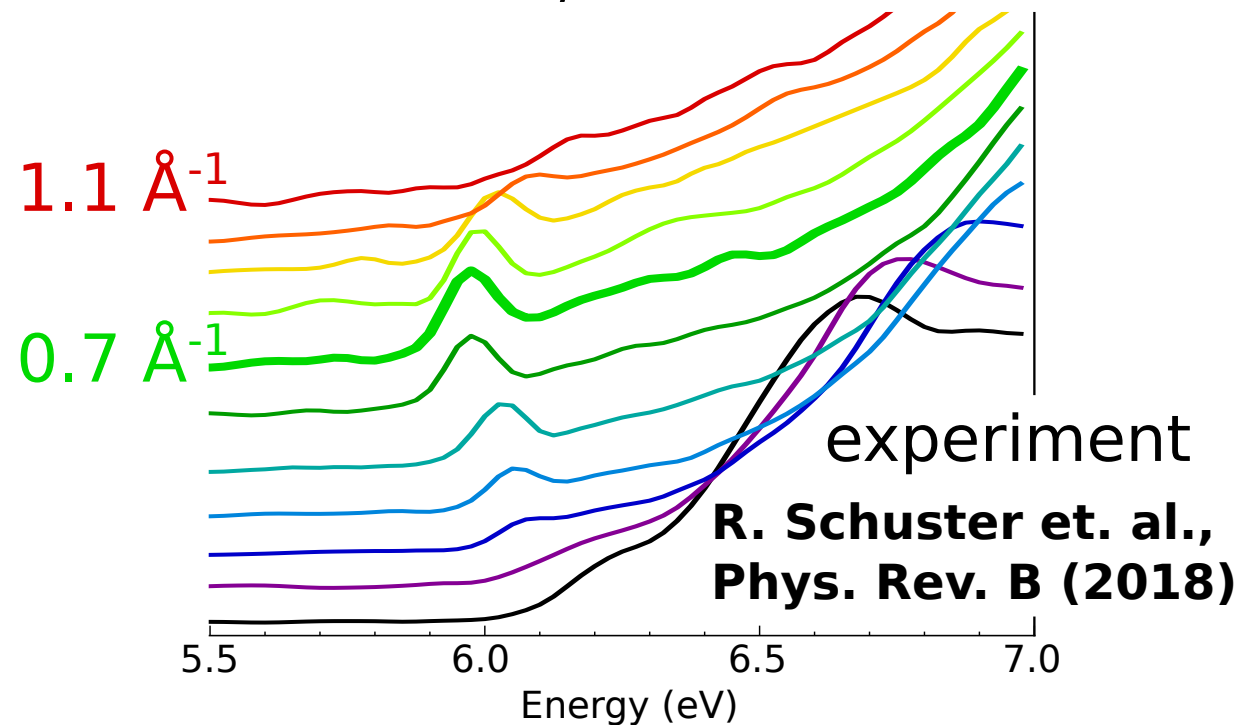
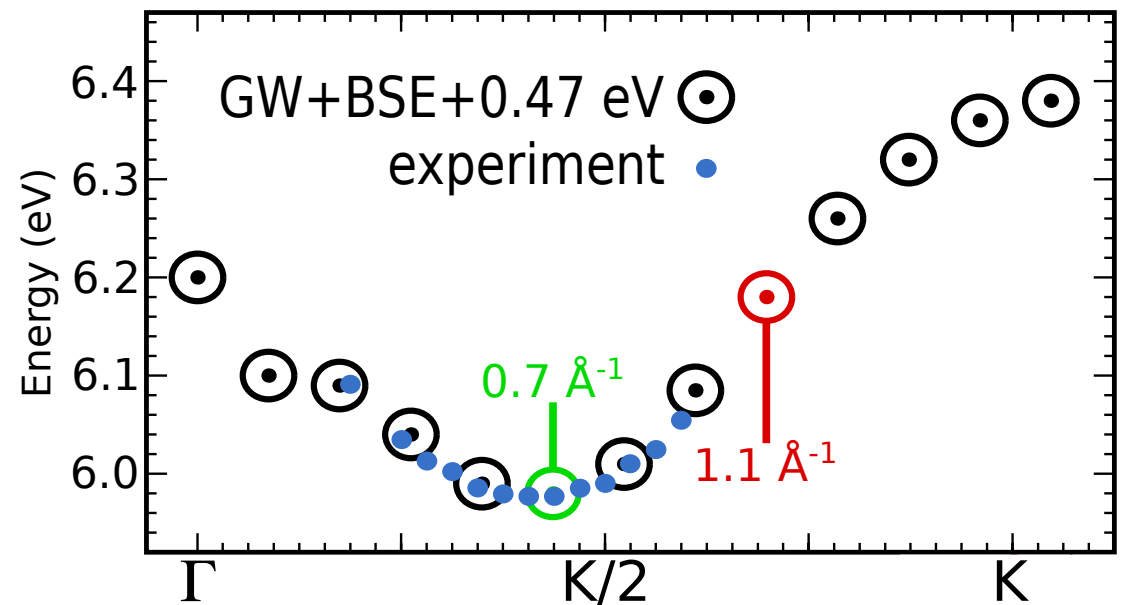
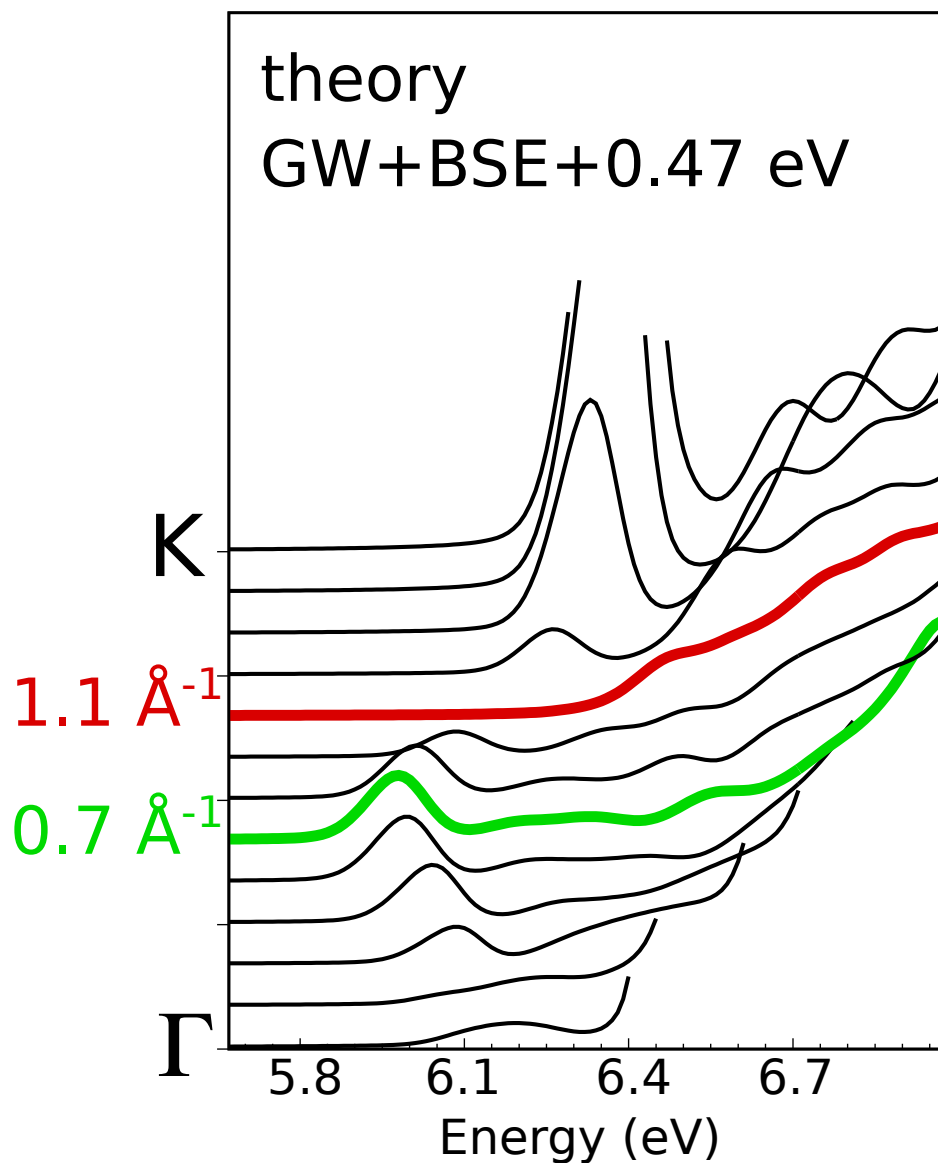
ab initio e-h dispersion



2) **No abs/lum mirror because absorption passes through a resonant state, while luminescence does not.**

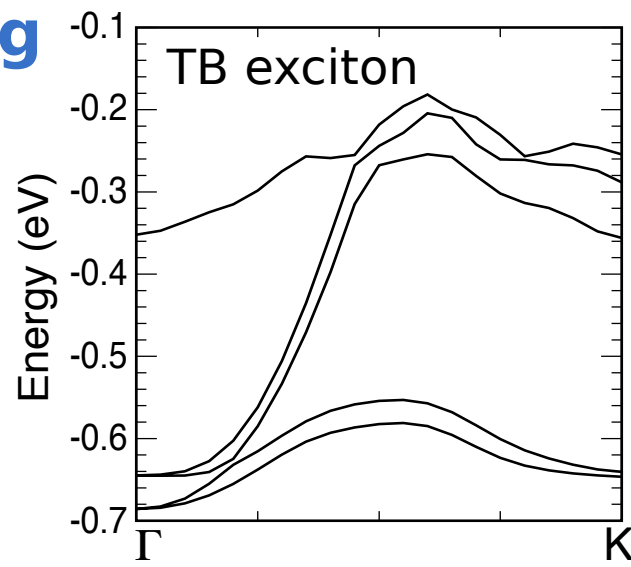
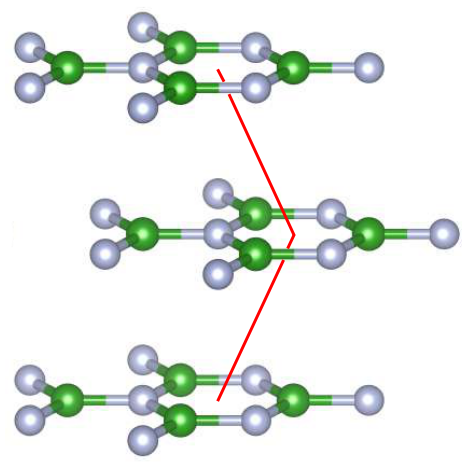
Confirmation from experimental evidences

Loss function at finite q

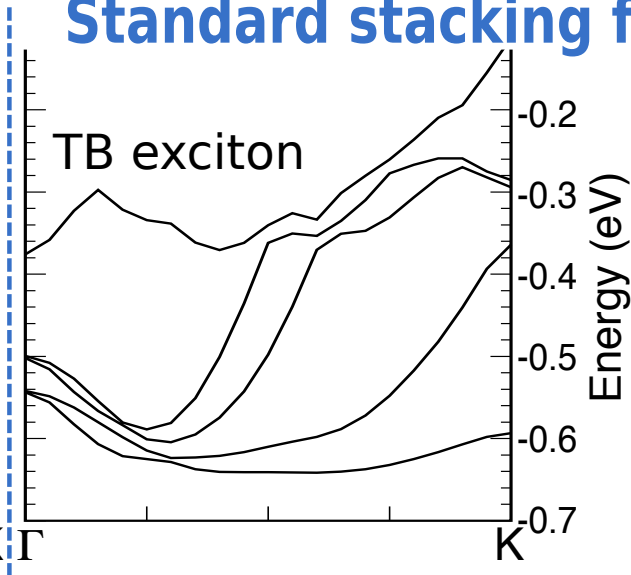
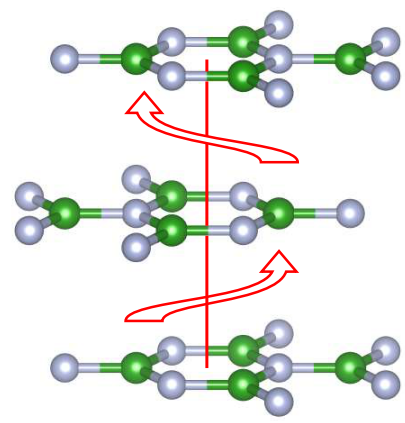


Intriguing prediction about Bernal stacking

Bernal stacking

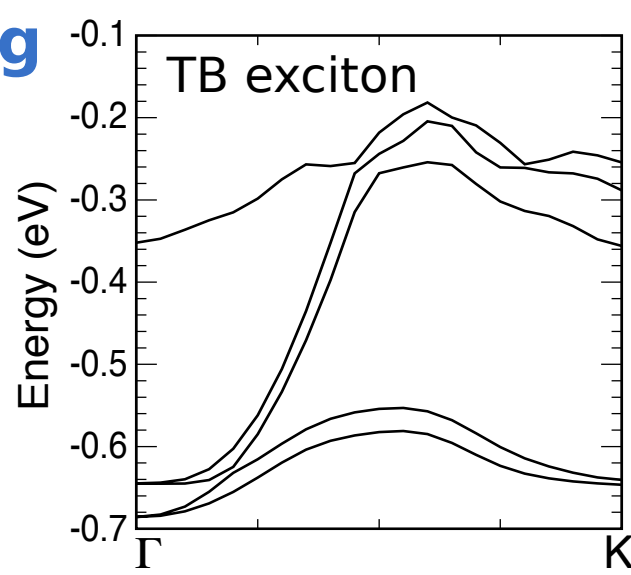
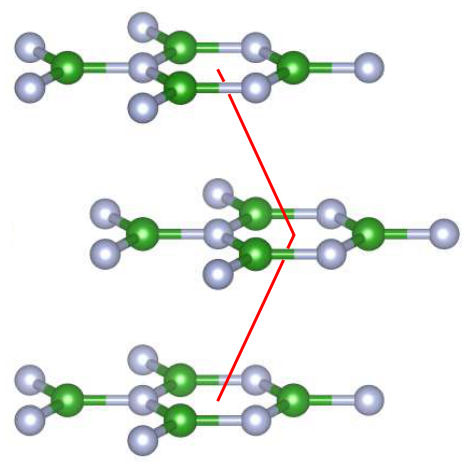


Standard stacking for comparison

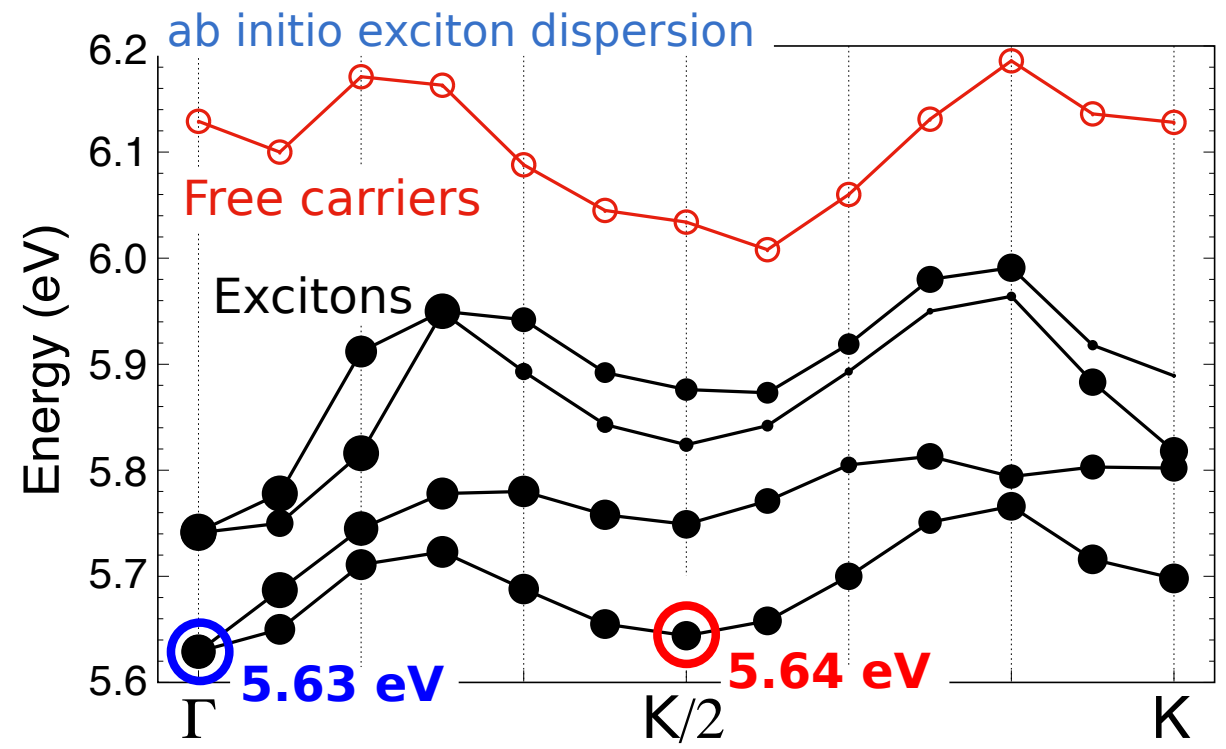
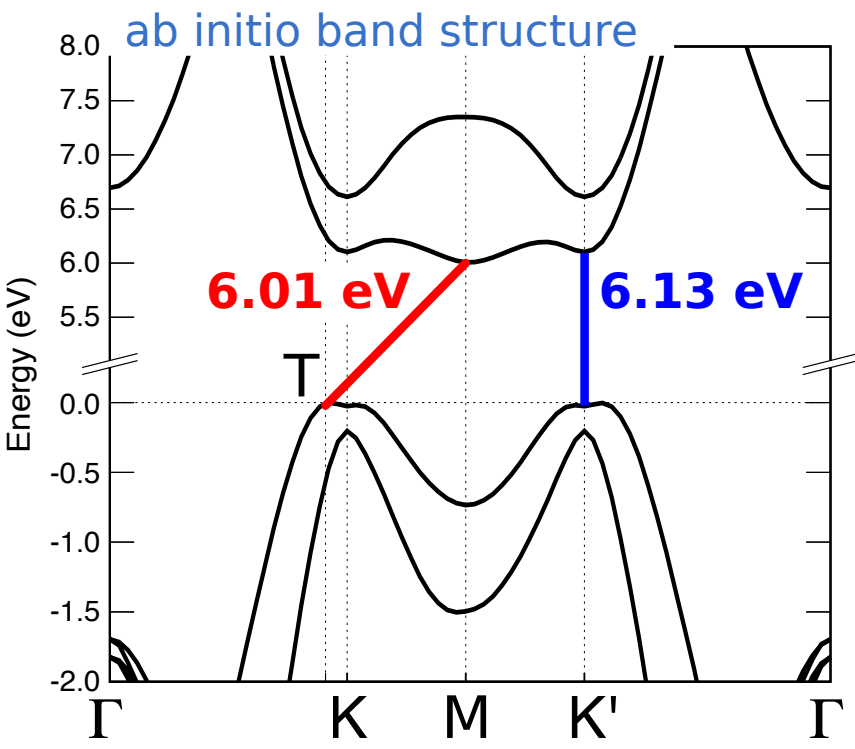
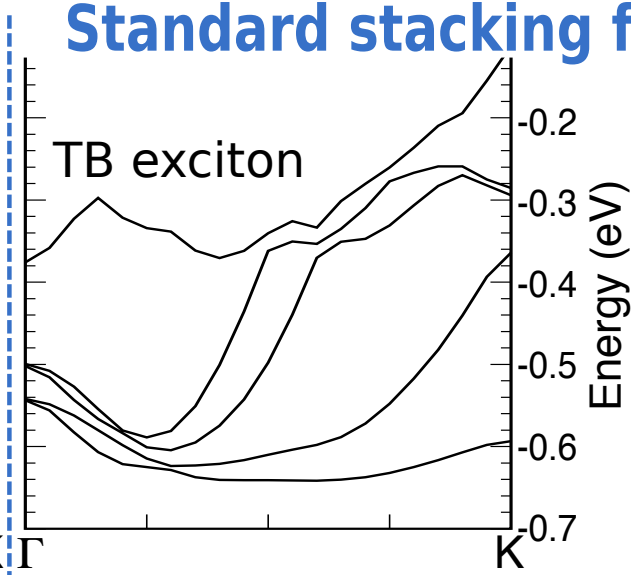
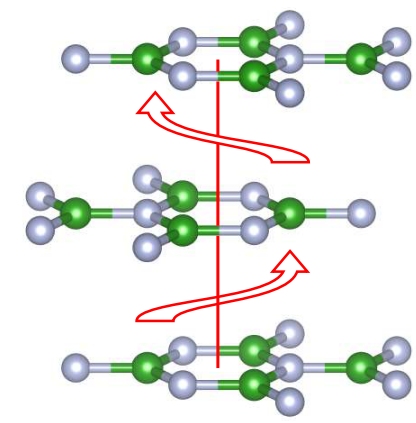


Intriguing prediction about Bernal stacking

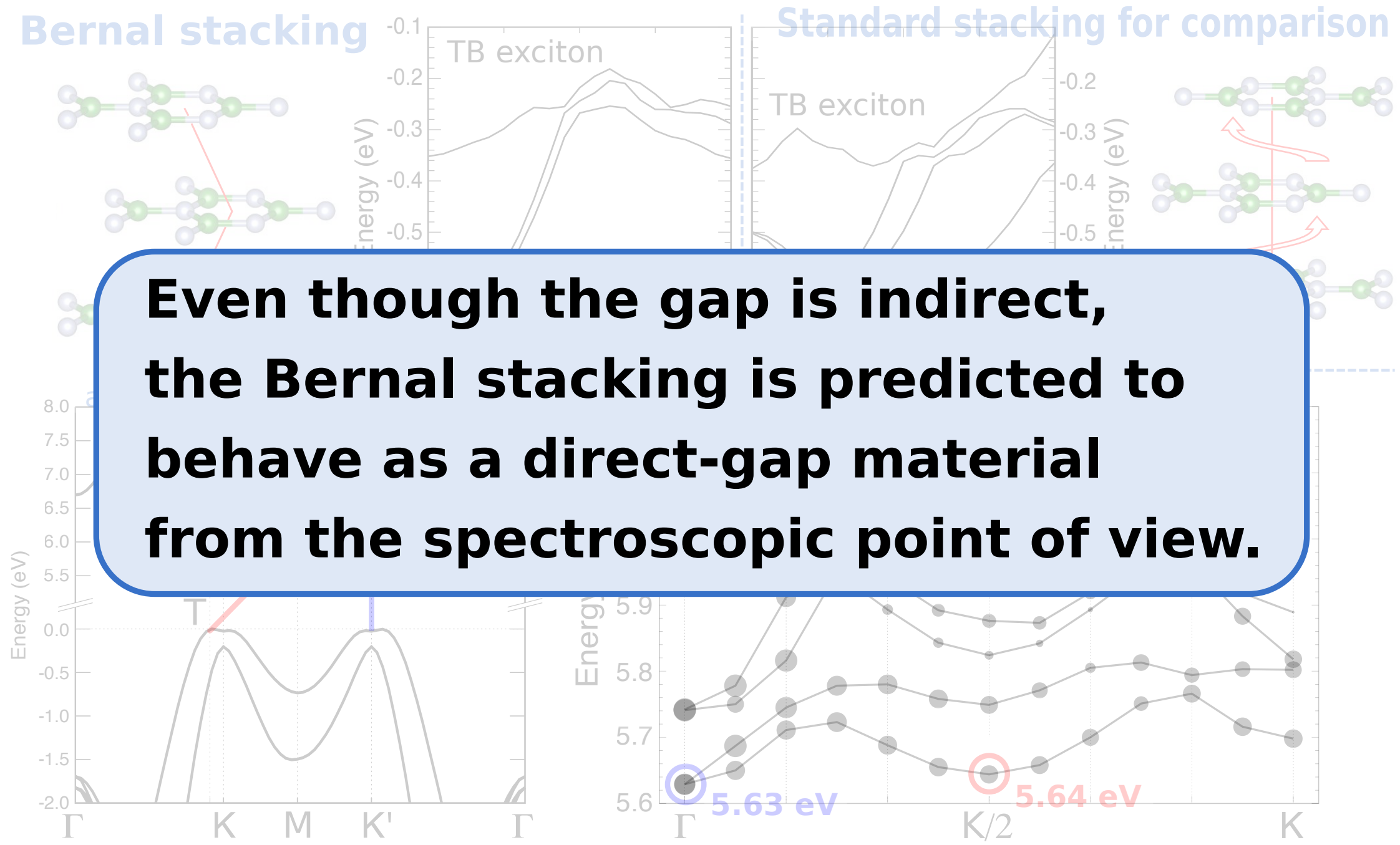
Bernal stacking



Standard stacking for comparison



Intriguing prediction about Bernal stacking



Even though the gap is indirect, the Bernal stacking is predicted to behave as a direct-gap material from the spectroscopic point of view.

Conclusions

- 1) Tight-binding model for excitons in 2D** and layered hBN.
Insight when applied to bulk and to different polymorphs.
- 2) Flattening of the exciton dispersion** in hBN leads to a strong electron-phonon coupling and high emission efficiency.
Consistent explanation of conflicting data coming from experimental spectra and theoretical band structure.
Experimental evidence of the theoretical explanation.
- 3) Prediction of even stronger effect in Bernal hBN.**

Conclusions

- 1) Tight-binding model for excitons in 2D** and layered hBN.
Insight when applied to bulk and to different polymorphs.
- 2) Flattening of the exciton dispersion** in hBN leads to a strong electron-phonon coupling and high emission efficiency.
Consistent explanation of conflicting data coming from experimental spectra and theoretical band structure.
Experimental evidence of the theoretical explanation.
- 3) Prediction of even stronger effect in Bernal hBN.**

Reasoned bibliography:

- K. Watanabe *et al.*, Nat. Materials 3, 404 (2004)
- L. Schué *et al.*, Nanoscale 8, 6986 (2016)
- G. Cassabois *et al.*, Nat. Photonics 10, 262 (2016)
- T. Q. P. Vuong *et al.*, Phys. Rev. B 95, 045207 (2017)
- L. Schué, **L. Sponza** *et al.*, arXiv:1803.03766 (2018)

mostly experimental
on luminescence

- T. Galvani *et al.*, Phys. Rev. B 94, 125303 (2016)
- **L. Sponza** *et al.*, Phys. Rev. B 97, 075121 (2018)
- **L. Sponza** *et al.*, arXiv:1806.06201 (2018)
- F. Paleari *et al.*, arXiv: 1803.00982 (2018)

mostly theoretical
TB & ab initio

Conclusions

1) Tight-binding model for excitons in 2D and layered hBN.

2)

Thanks for your attention

3) Prediction of even stronger effect in Bernal hBN.

Reasoned bibliography:

- K. Watanabe *et al.*, Nat. Materials 3, 404 (2004)
- L. Schué *et al.*, Nanoscale 8, 6986 (2016)
- G. Cassabois *et al.*, Nat. Photonics 10, 262 (2016)
- T. Q. P. Vuong *et al.*, Phys. Rev. B 95, 045207 (2017)
- L. Schué, **L. Sponza** *et al.*, arXiv:1803.03766 (2018)

mostly experimental
on luminescence

- T. Galvani *et al.*, Phys. Rev. B 94, 125303 (2016)
- **L. Sponza** *et al.*, Phys. Rev. B 97, 075121 (2018)
- **L. Sponza** *et al.*, arXiv:1806.06201 (2018)
- F. Paleari *et al.*, arXiv: 1803.00982 (2018)

mostly theoretical
TB & ab initio