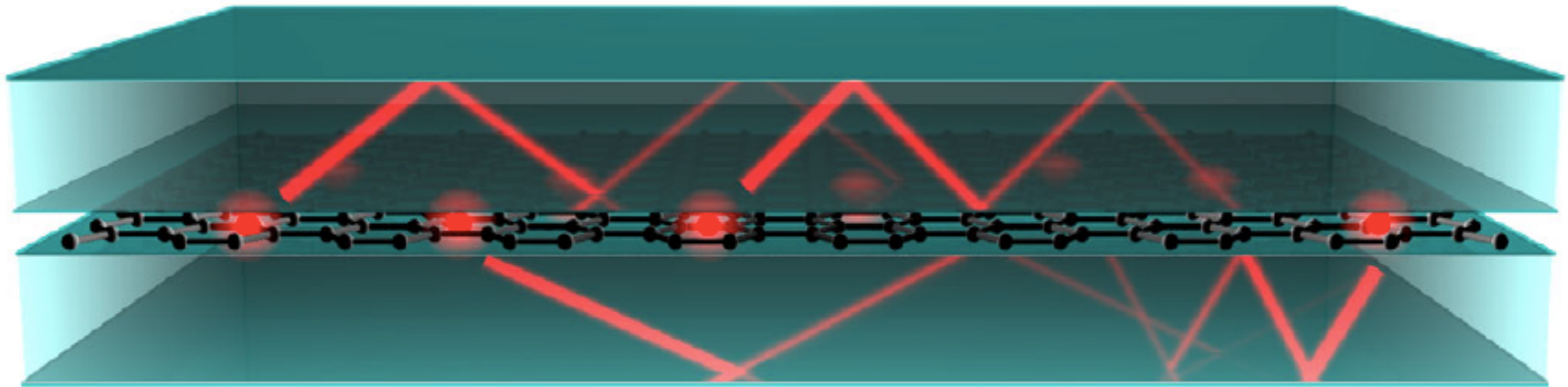


Out-of-plane heat transfer in Van der Waals stacks



ICFO^R

The Institute of Photonic
Sciences

Klaas-Jan Tielrooij

March 29th 2017

Barcelona, ES

Acknowledgements



Nano-optoelectronics Group
www.koppensgroup.icfo.eu

ICFO, Spain

Frank Koppens

Niels Hesp

Mark Lundeborg

Mathieu Massicotte

Peter Schmidt

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MPIP Mainz, Germany

Mischa Bonn

Dmitry Turchinovich

Zoltan Mics

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Takashi Taniguchi

Kenji Watanabe



Radboud Universiteit Nijmegen



POLITECNICO
MILANO 1863

DIPARTIMENTO DI FISICA

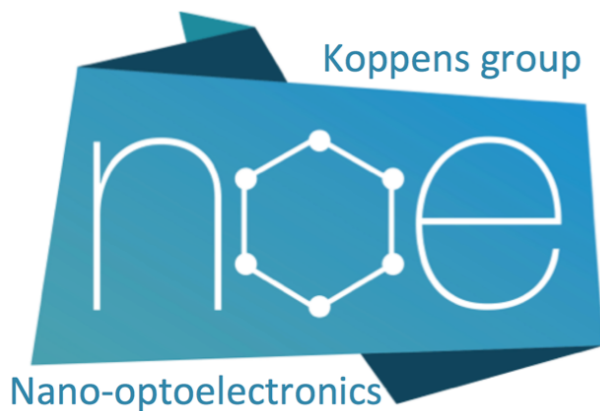
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UNIVERSITY



MAX-PLANCK-GESELLSCHAFT



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POLITECNICO MILANO 1863

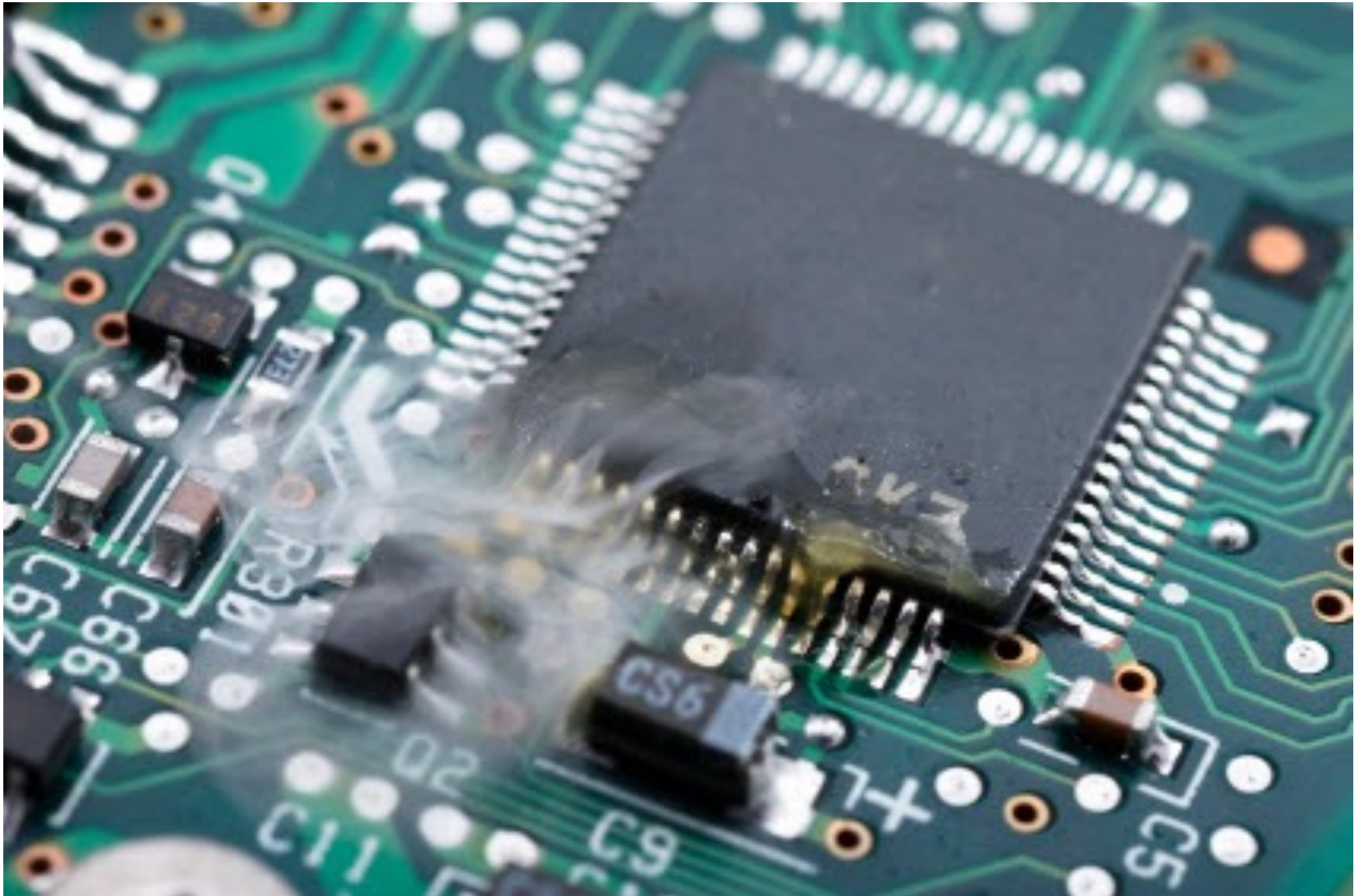
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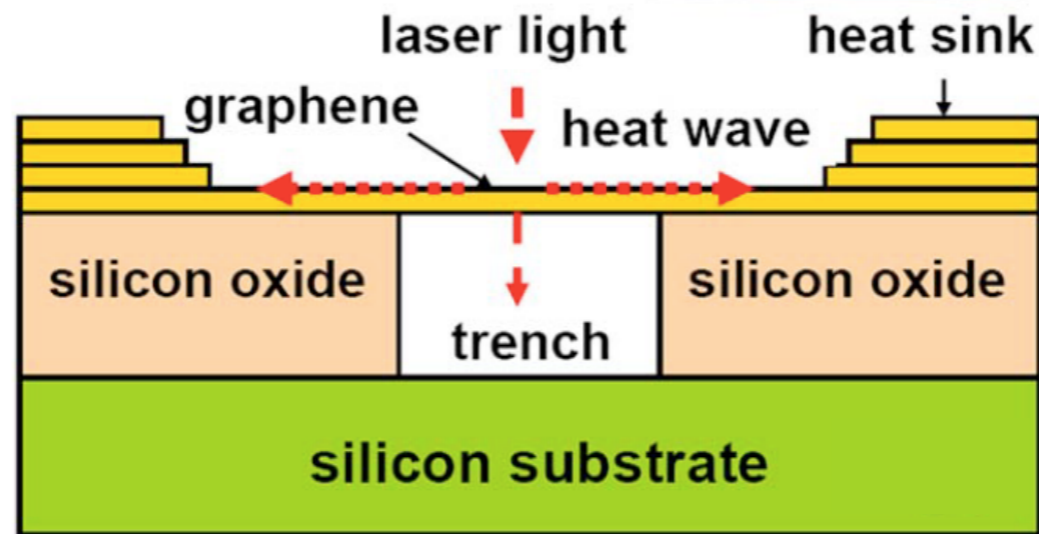
MAX-PLANCK-GESellschaft



Thermal management



Graphene & thermal management

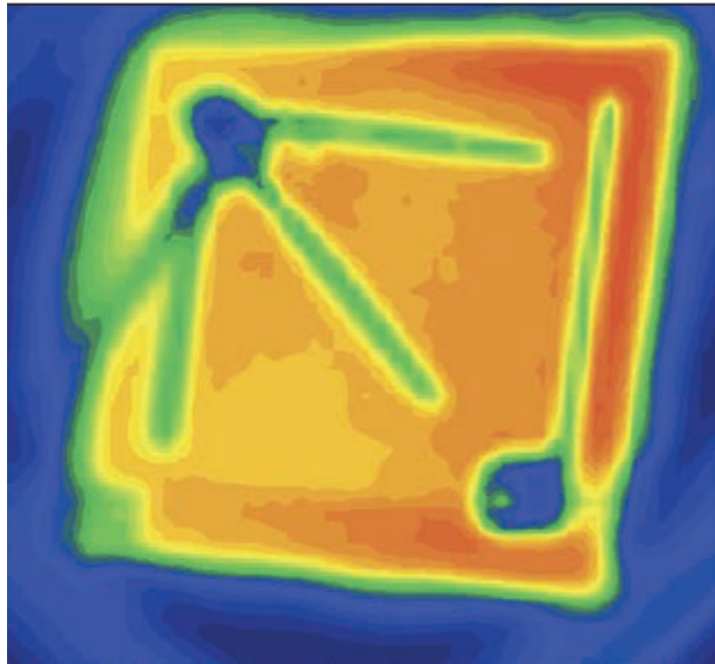


Ghosh et al, *APL* 92, 151911 (2008)

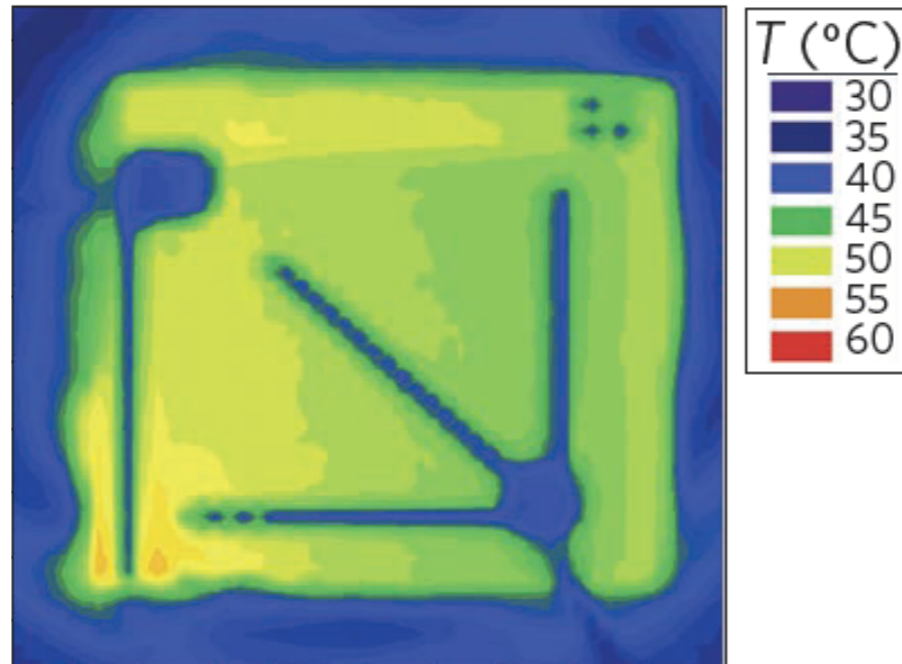
- ➔ **Suspended graphene** has a very high in-plane thermal conductivity:
>1000 W/mK
- ➔ **Supported graphene: ideal substrate = heat sink!**

Graphene & thermal management

Light-emitting diodes



Conventional GaN LED

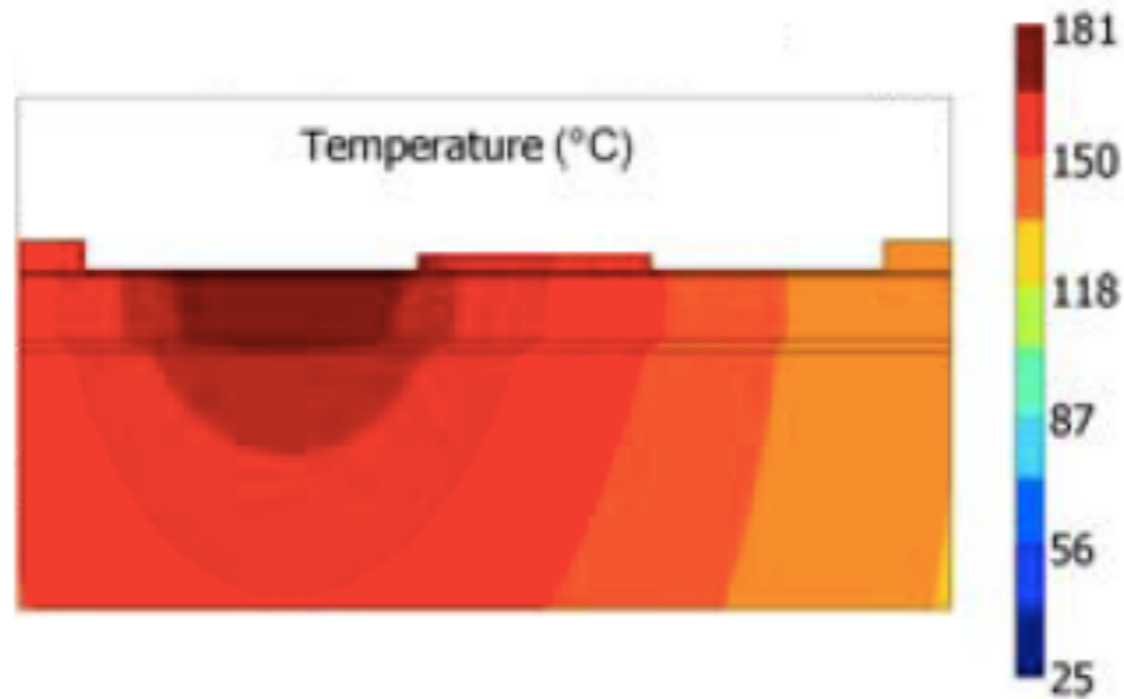


Embedded graphene layer GaN LED

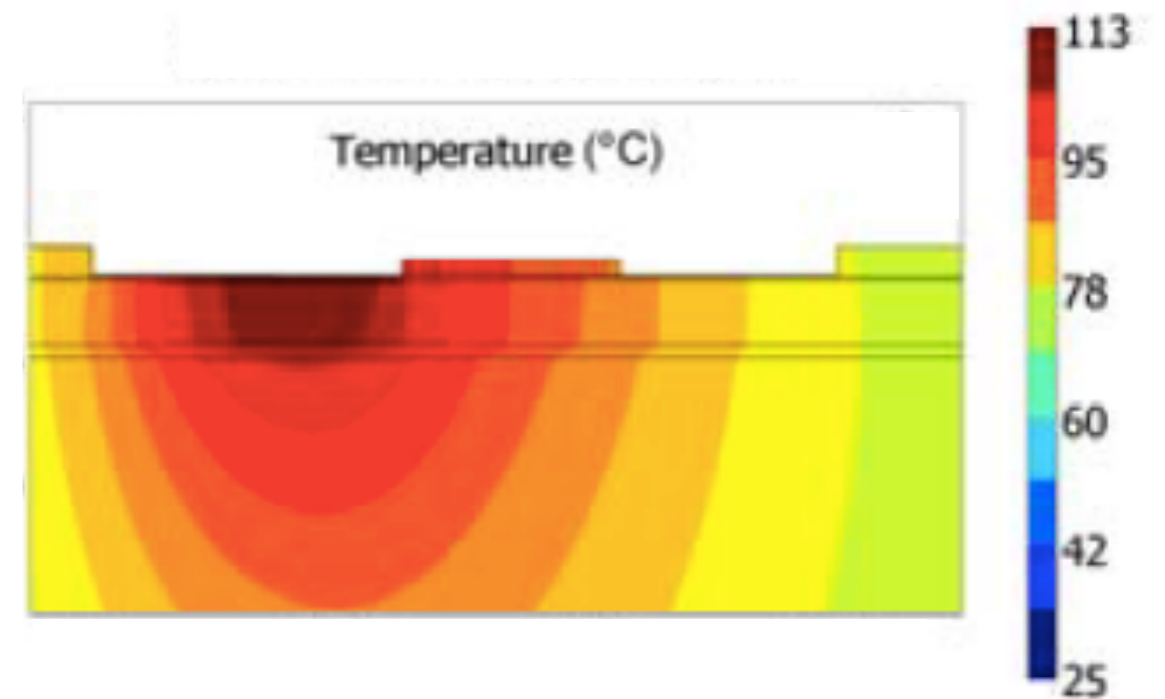
Han et al, *Nature Comm.* 4, 1452 (2013)

Graphene & thermal management

Field-effect transistors



AlGaIn/GaN FET



AlGaIn/GaN FET with graphene/graphite

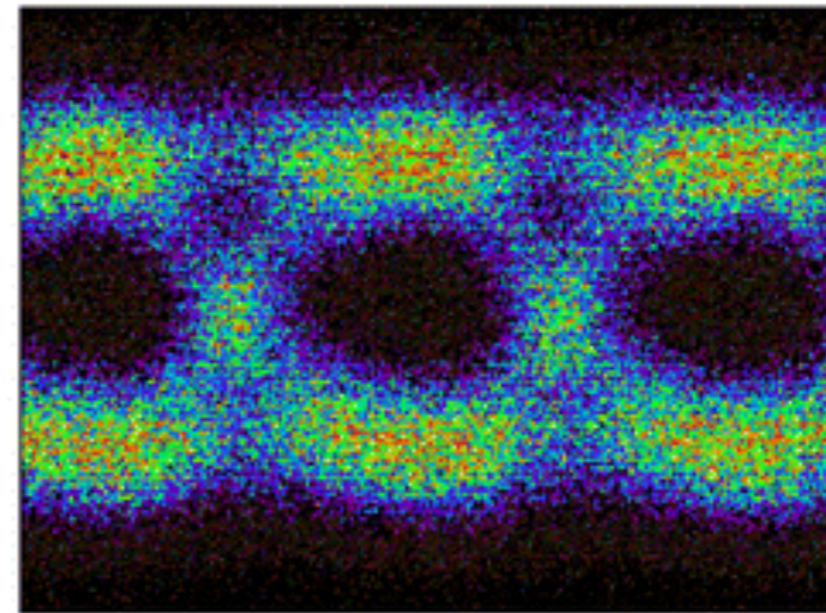
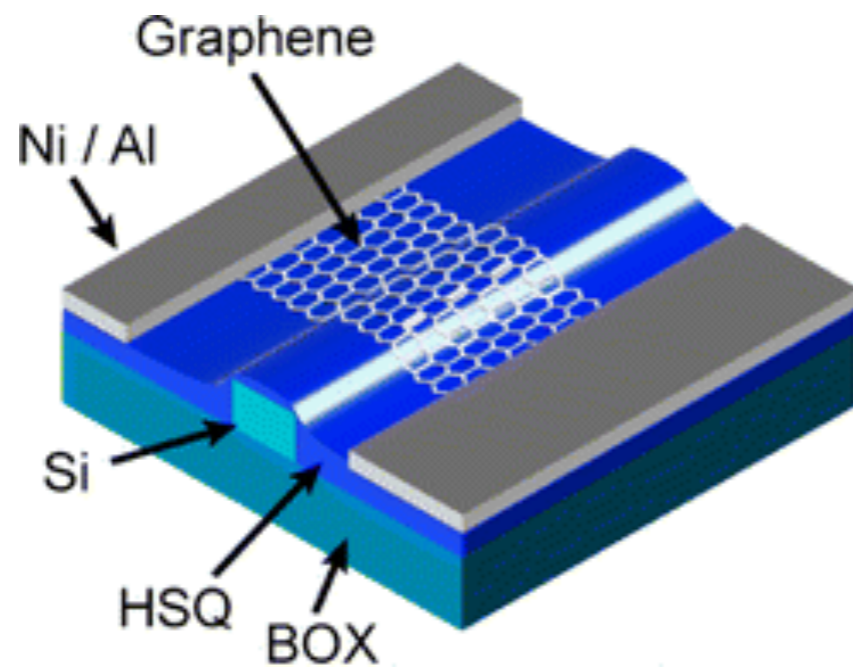
Yan et al, *Nature Comm.* 3, 827 (2012)

Graphene & thermal management

Fast photodetectors

Fast photodetectors

>50 Gbit/s



Schall et al, *ACS Photonics* (2014)

Fast photodetectors

Hot graphene electrons

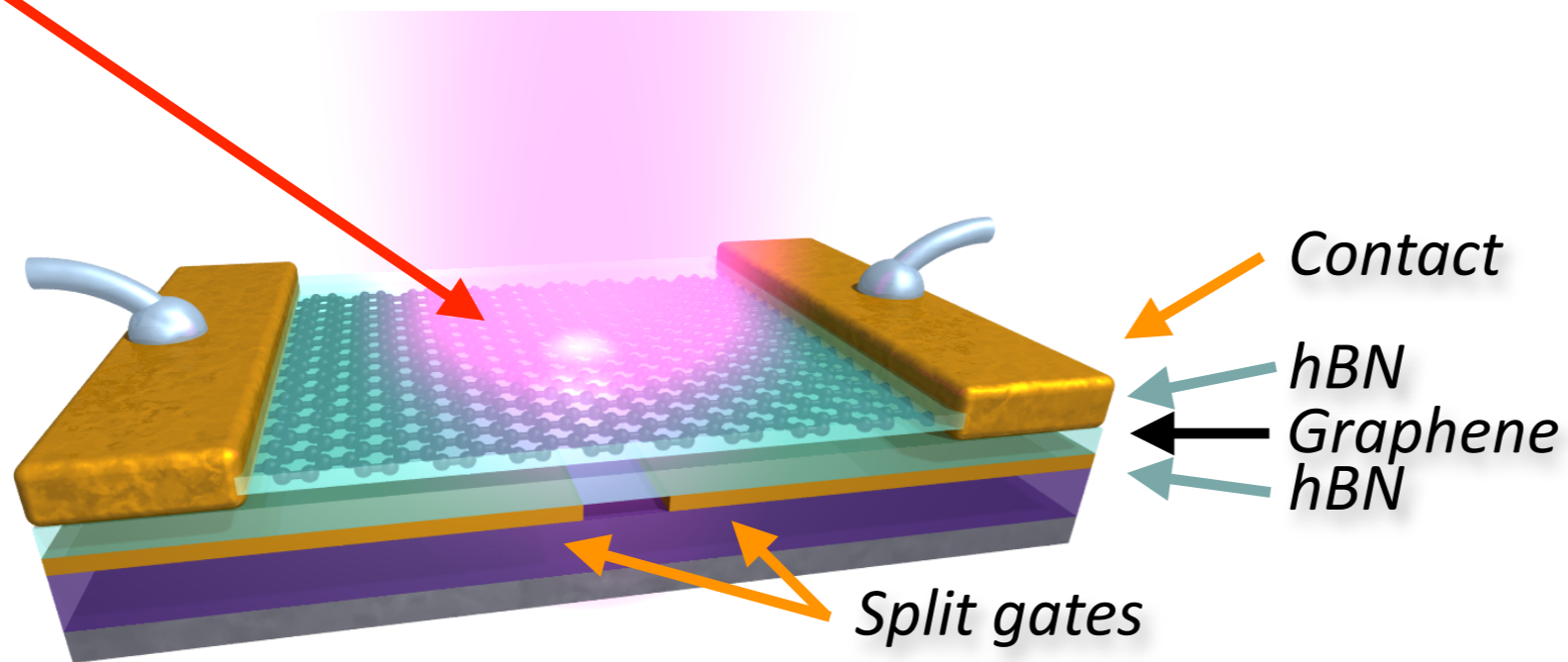


Photo-thermoelectric (PTE) detector

Song et al. *PRL* (2011)
Gabor et al. *Science* (2011)
Koppens et al. *Nature Nano* (2014)

Fast photodetectors

Hot graphene electrons

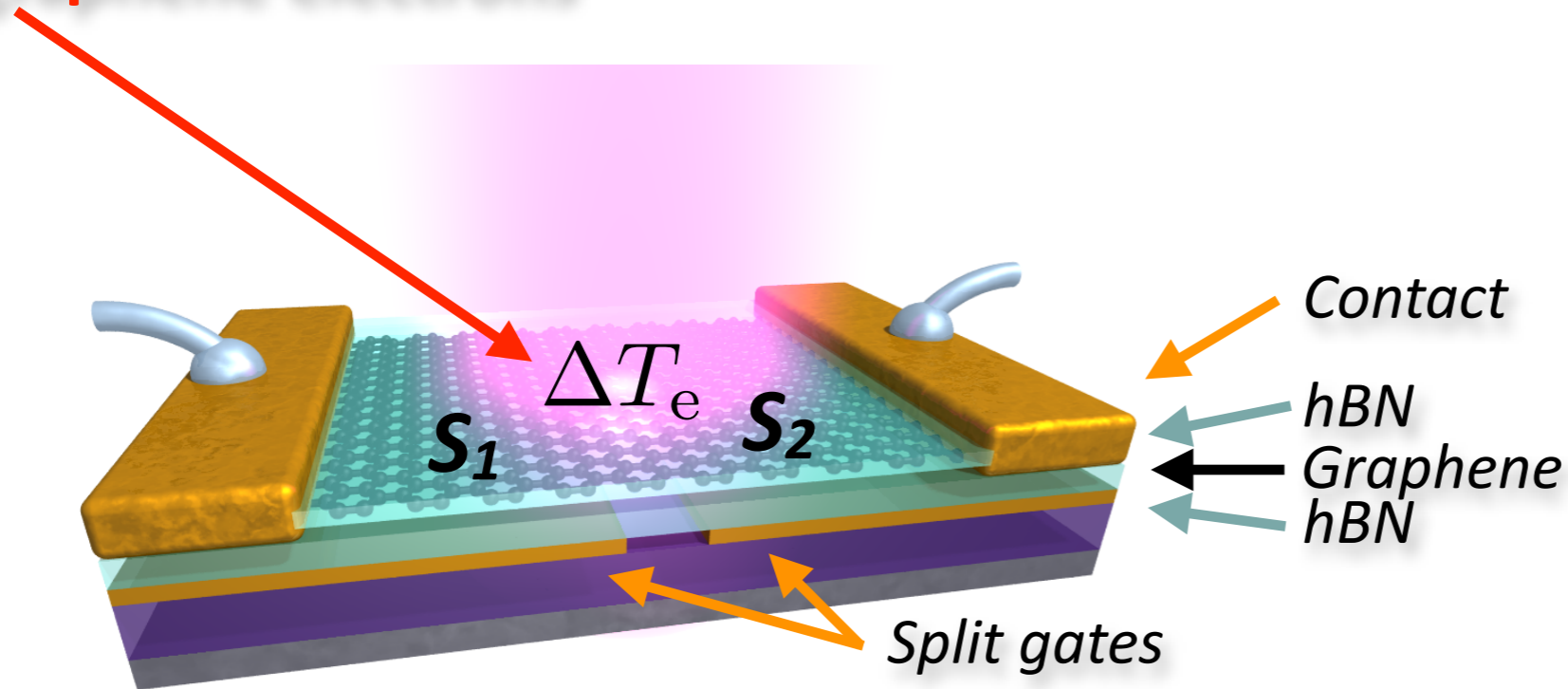
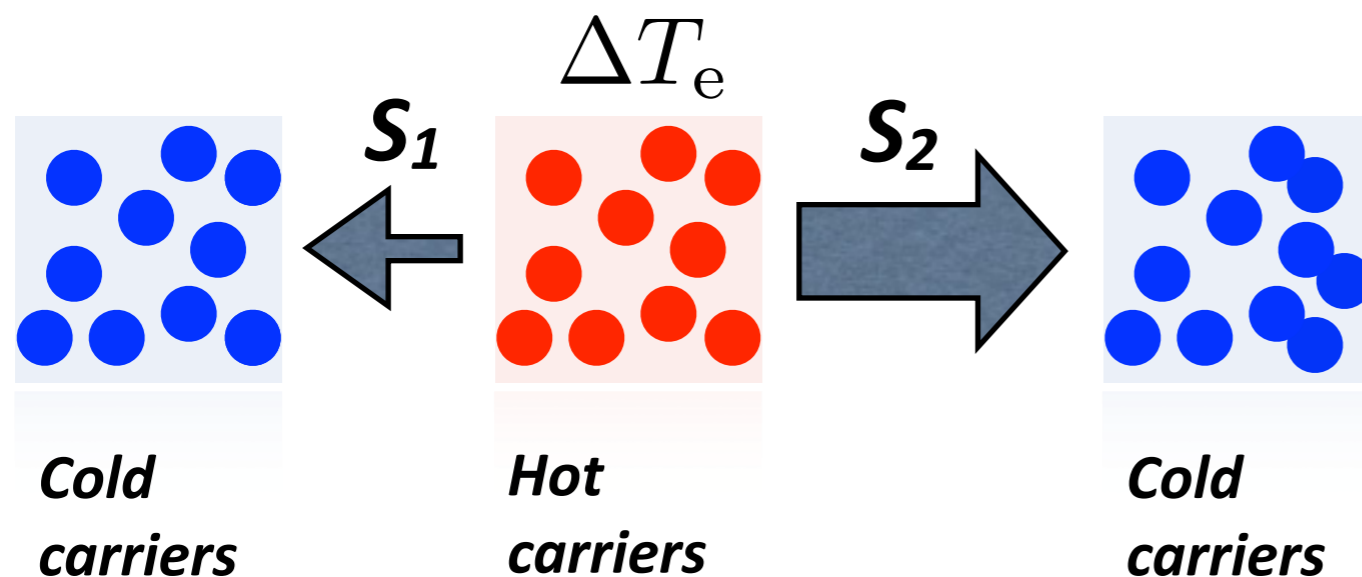


Photo-thermoelectric (PTE) detector

Use the heat!



Electron heat \neq phonon heat

Song et al. *PRL* (2011)
Gabor et al. *Science* (2011)
Koppens et al. *Nature Nano* (2014)

Fast photodetectors

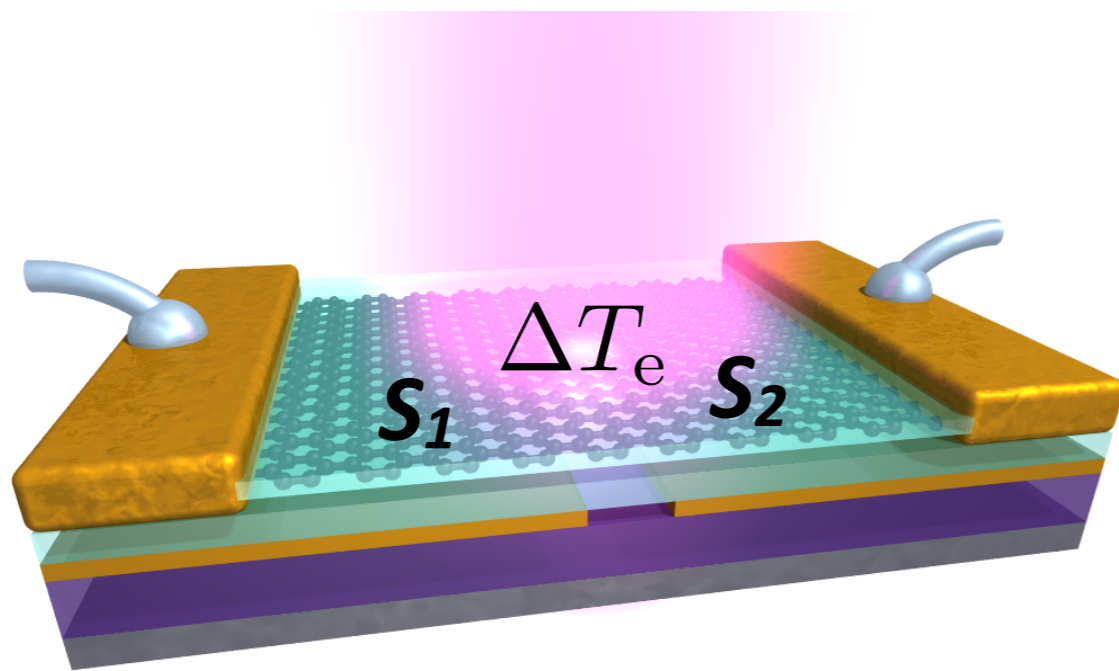


Photo-thermoelectric (PTE) detector

$$V_{\text{PTE}} = (S_2 - S_1) \Delta T_e$$

$$\Delta T_e \propto \frac{P_{\text{abs}}}{\Gamma_{\text{cool}}} = \frac{P_{\text{abs}} \tau_{\text{cool}}}{C_n}$$

Electron heat **phonon heat**

Song et al. *PRL* (2011)

Gabor et al. *Science* (2011)

Koppens et al. *Nature Nano* (2014)

Fast photodetectors

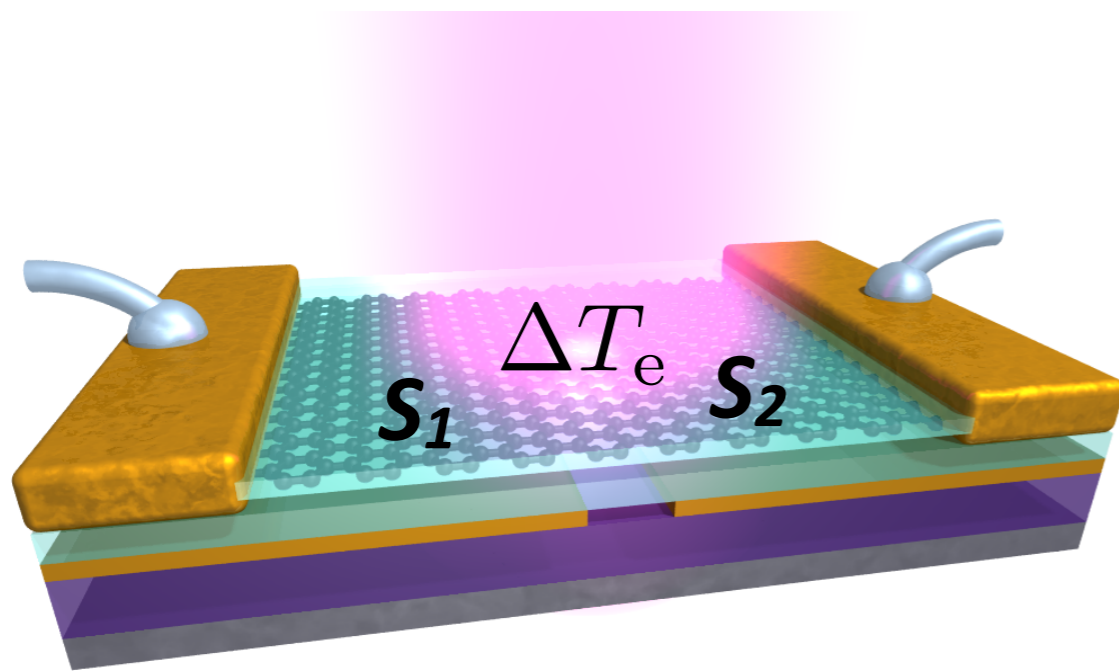


Photo-thermoelectric (PTE) detector

$$V_{\text{PTE}} = (S_2 - S_1) \Delta T_e$$

$$\Delta T_e \propto \frac{P_{\text{abs}}}{\Gamma_{\text{cool}}} = \frac{P_{\text{abs}} \tau_{\text{cool}}}{C_n}$$

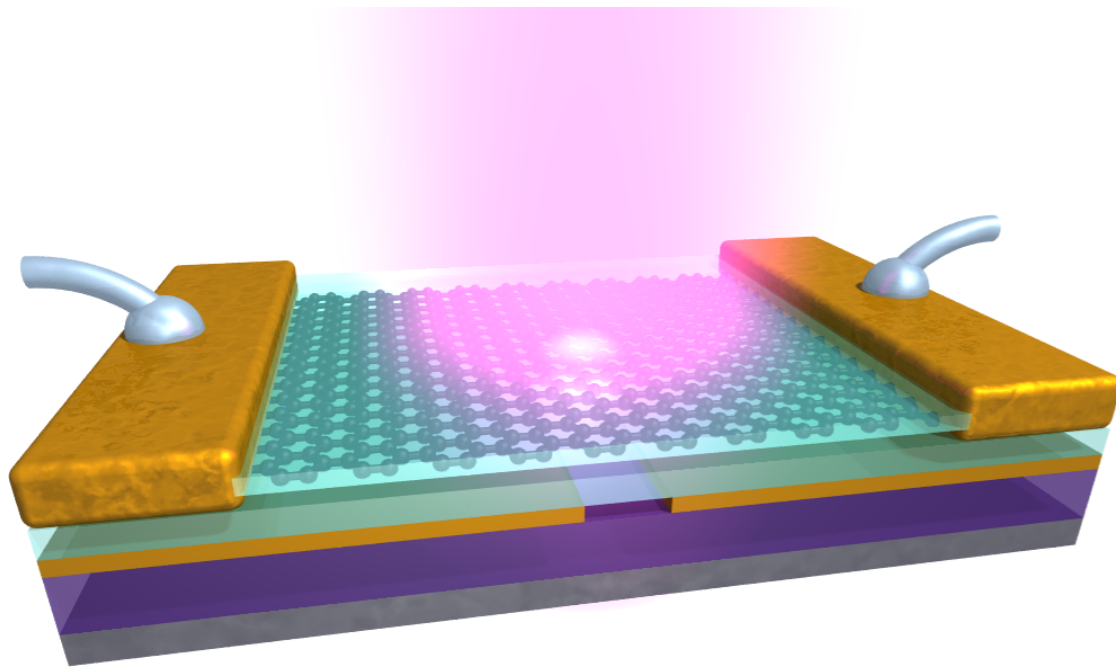
Electron heat phonon heat

➔ Slow electron cooling is beneficial!

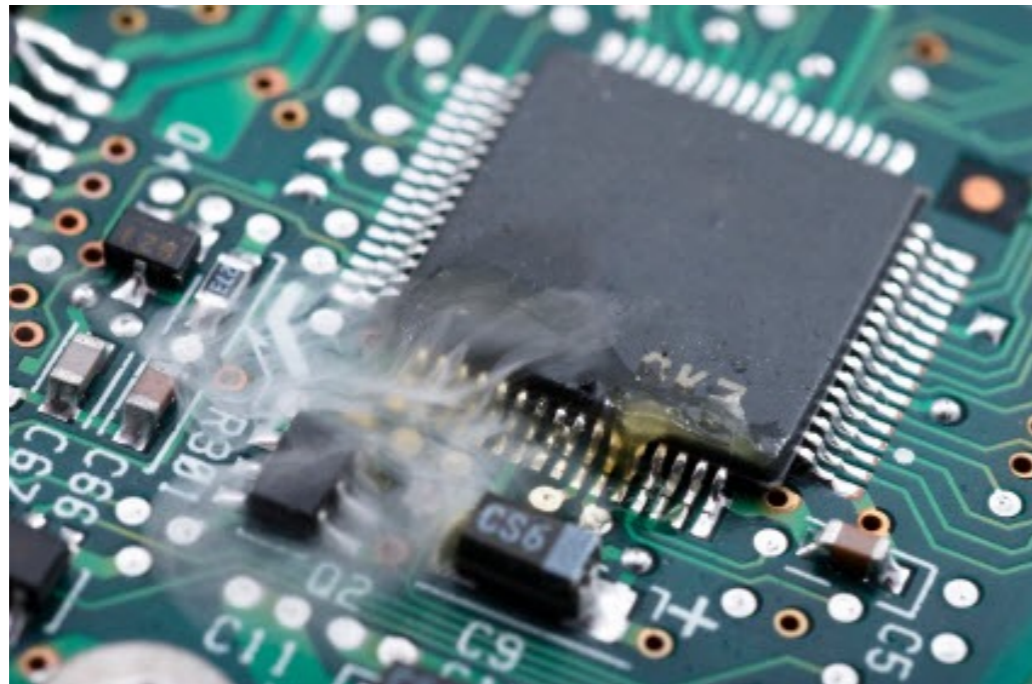
Song et al. *PRL* (2011)
Gabor et al. *Science* (2011)
Koppens et al. *Nature Nano* (2014)

Understand thermal transport

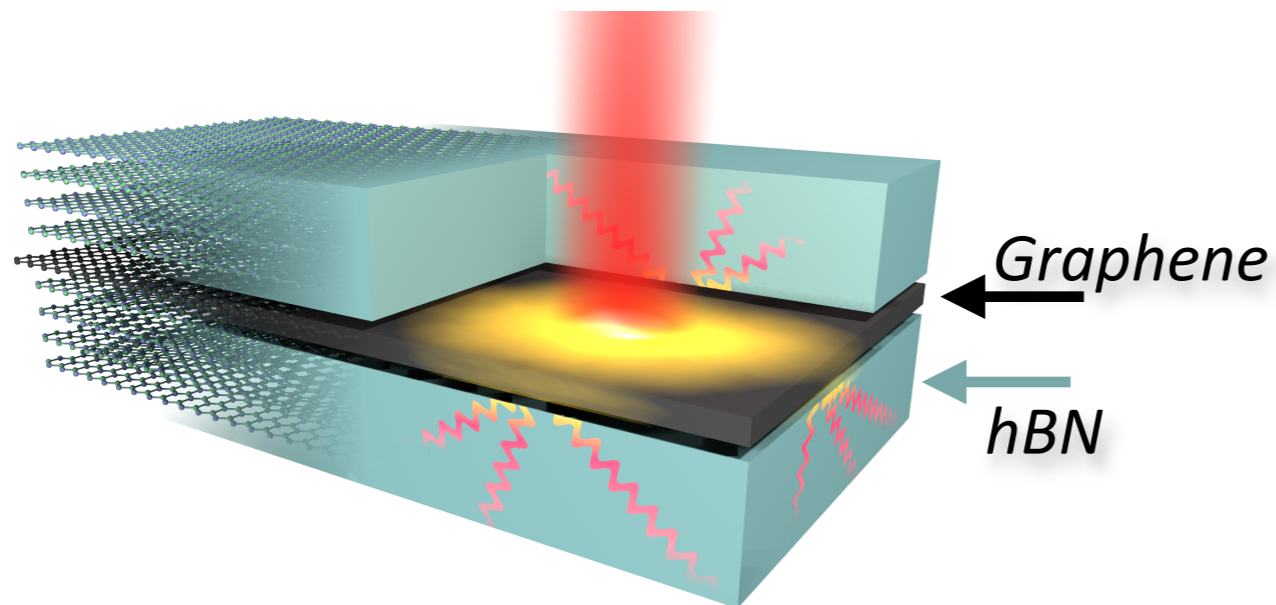
➔ Photodetectors: electron cooling?



➔ Thermal management: ideal substrate = heat sink!

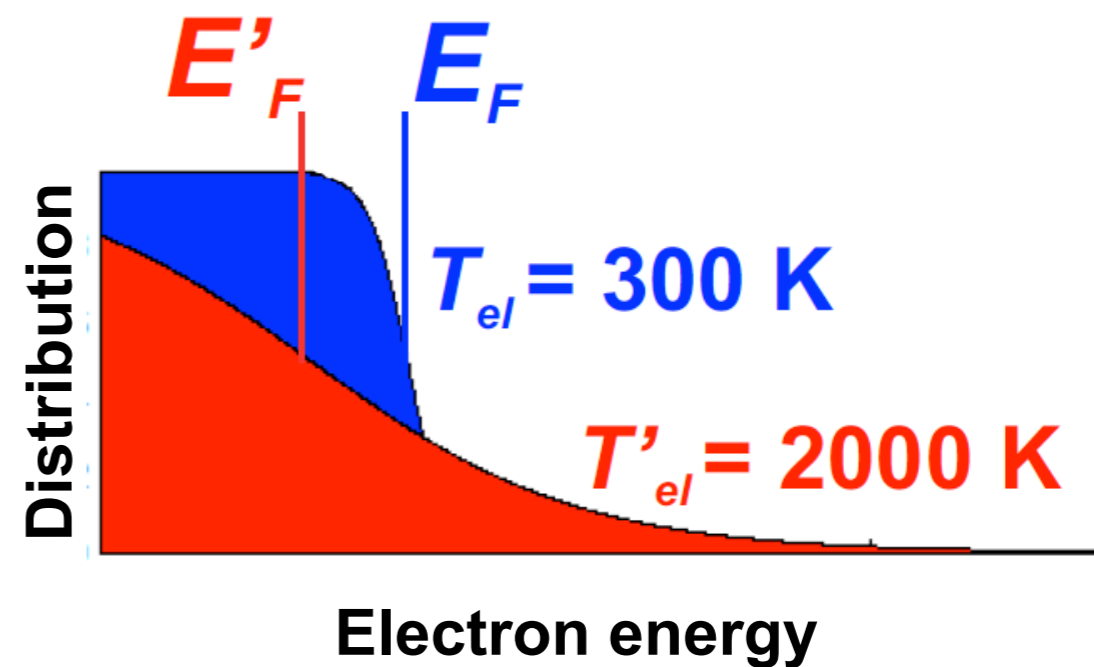
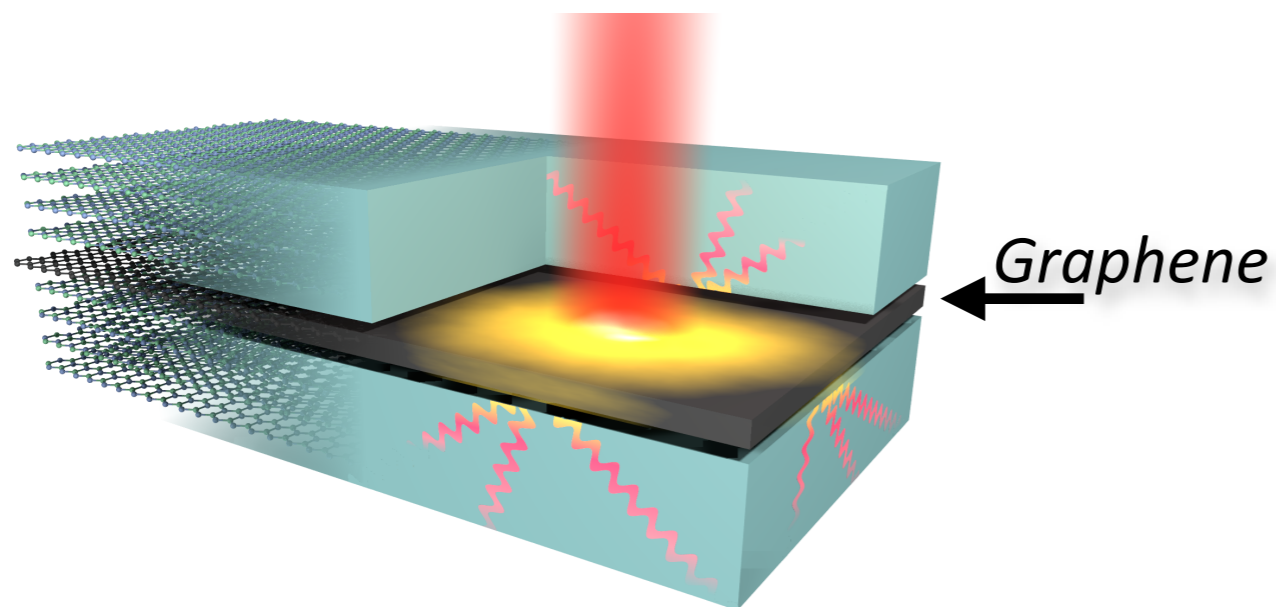


Understand thermal transport



Efficient **out-of-plane** heat transfer:
Hot graphene electrons to **hBN hyperbolic phonon polaritons**

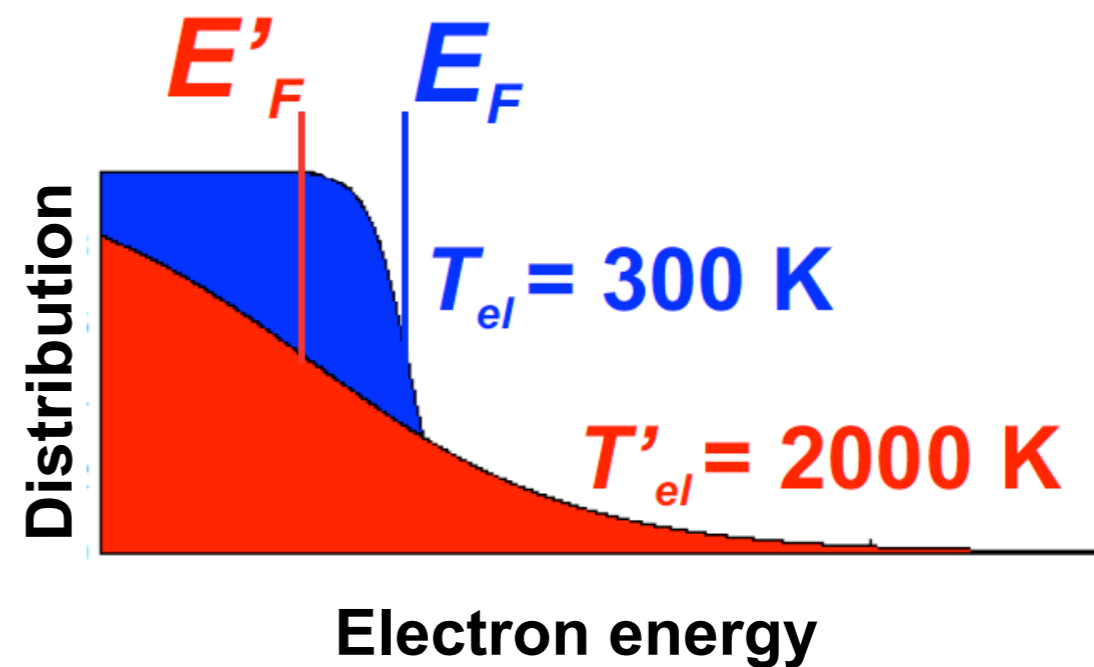
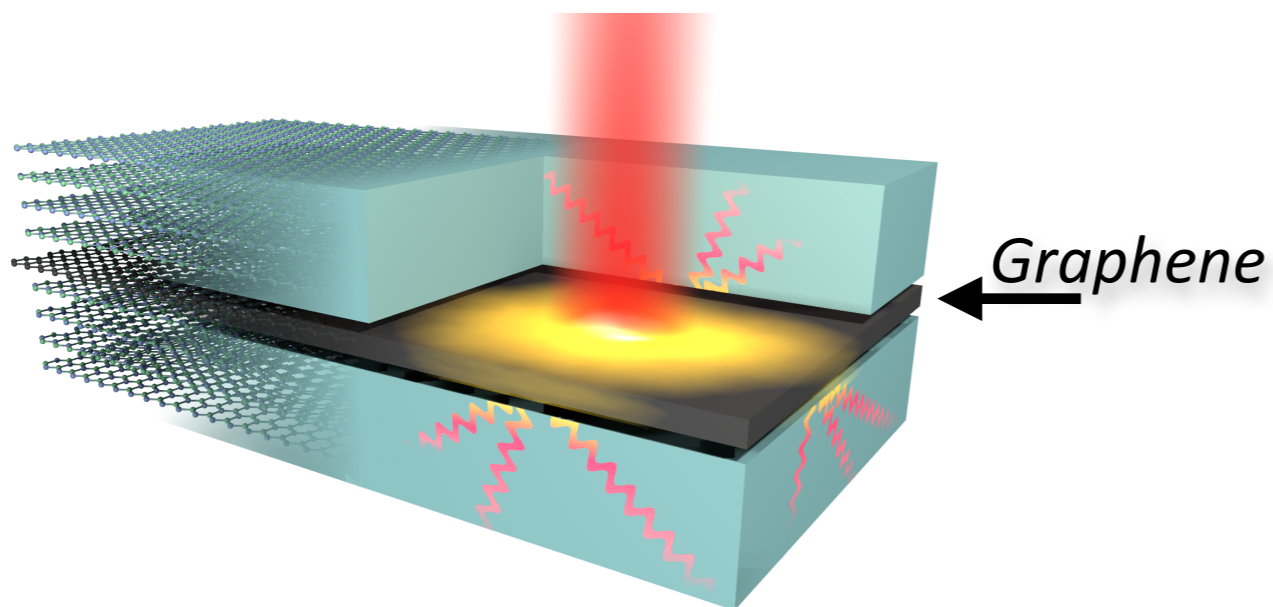
Graphene: Hot electrons



Hot electrons:
broadened Fermi-Dirac distribution

Electron heat \neq phonon heat

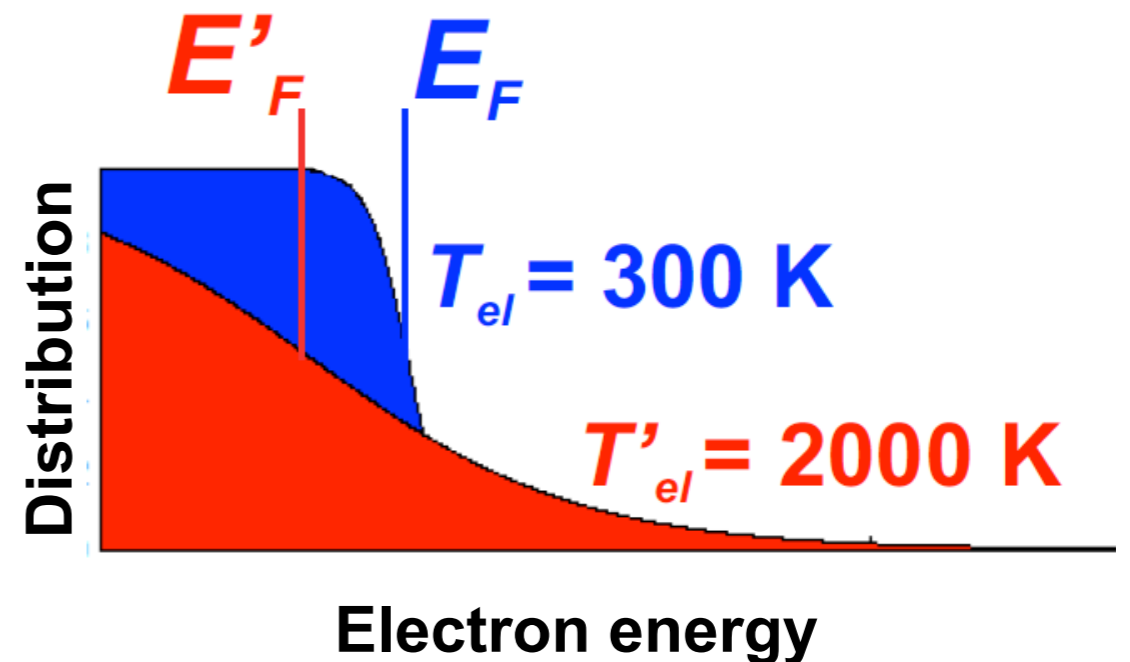
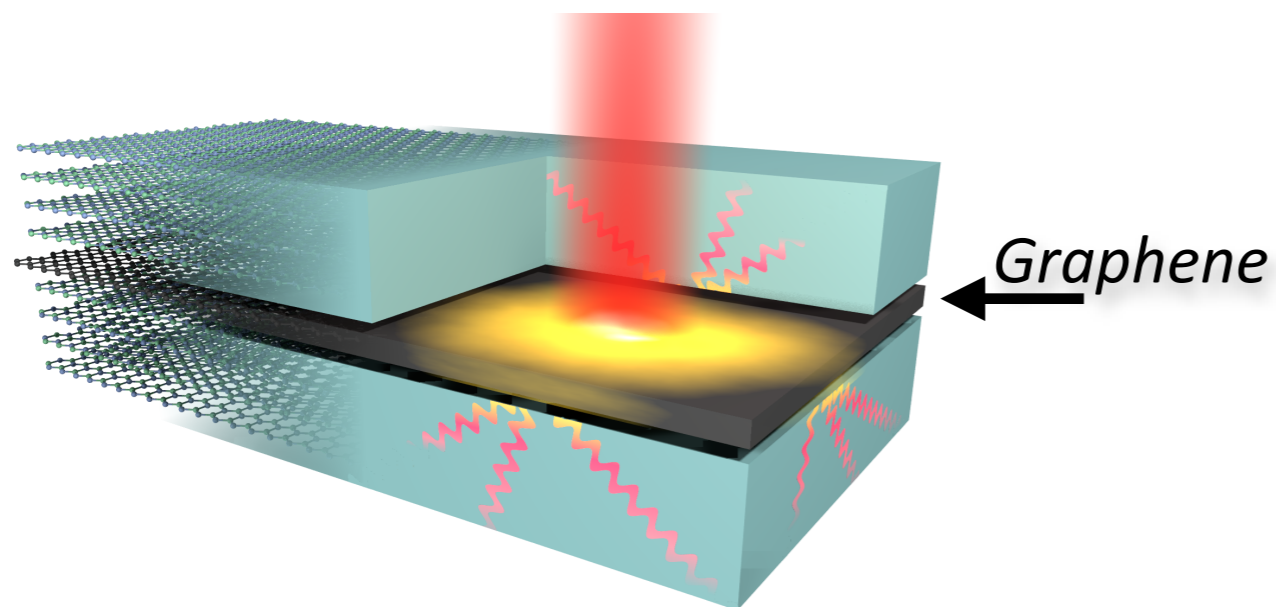
Graphene: Hot electrons



Planck radiation: coupling to *far-field* light in vacuum

$$k < \omega/c$$

Graphene: Hot electrons



Planck radiation: coupling to *far-field* light in vacuum

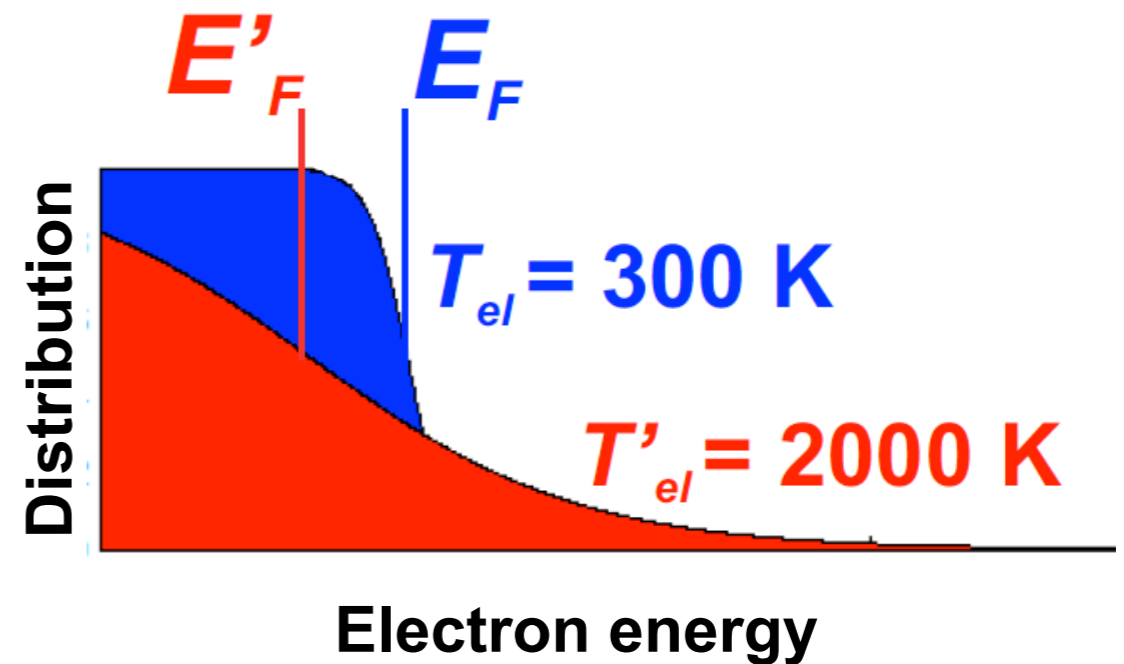
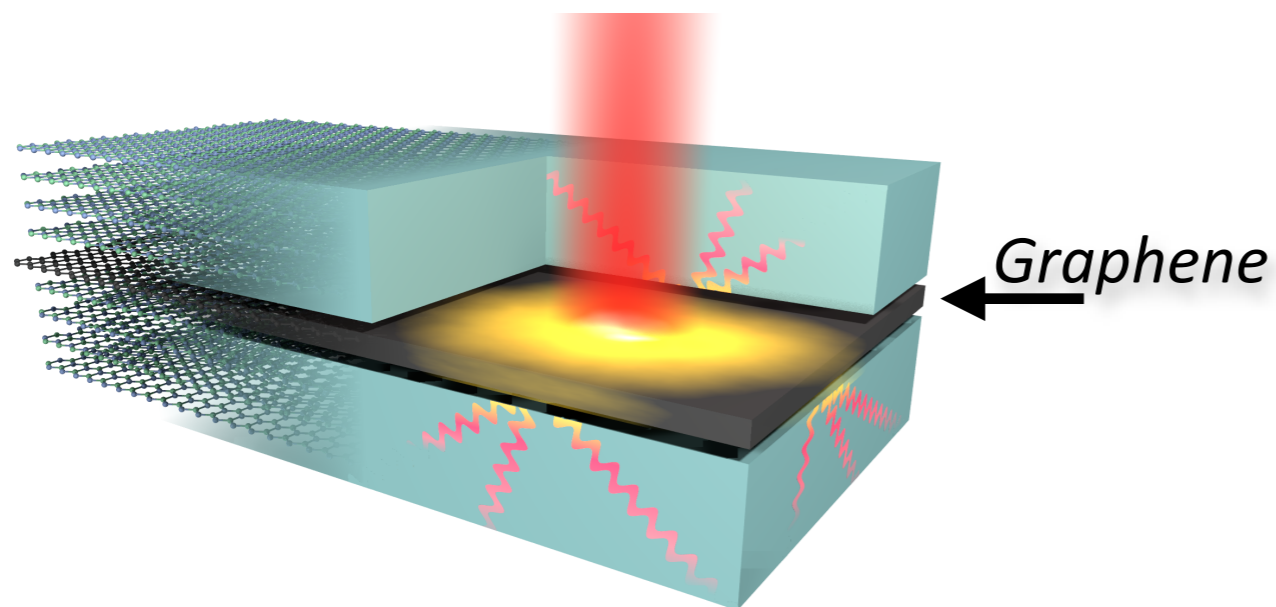
$$k < \omega/c$$

Very inefficient!

=> Cooling to graphene phonons dominates
(Governed by deformation potential)

Bistritzer and MacDonald, *PRL* (2009)
Song et al. *PRL* (2012)
Graham et al. *Nature Phys.* (2013)
Betz et al. *Nature Phys.* (2013)

Graphene: Hot electrons



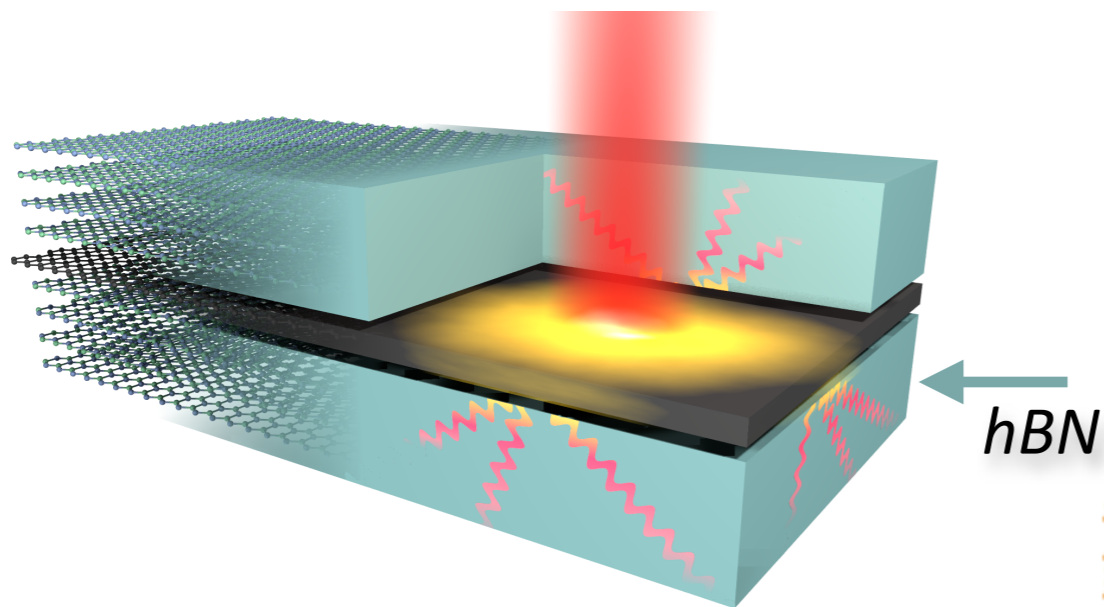
Planck radiation: coupling to *far-field* light in vacuum

$$k < \omega/c$$

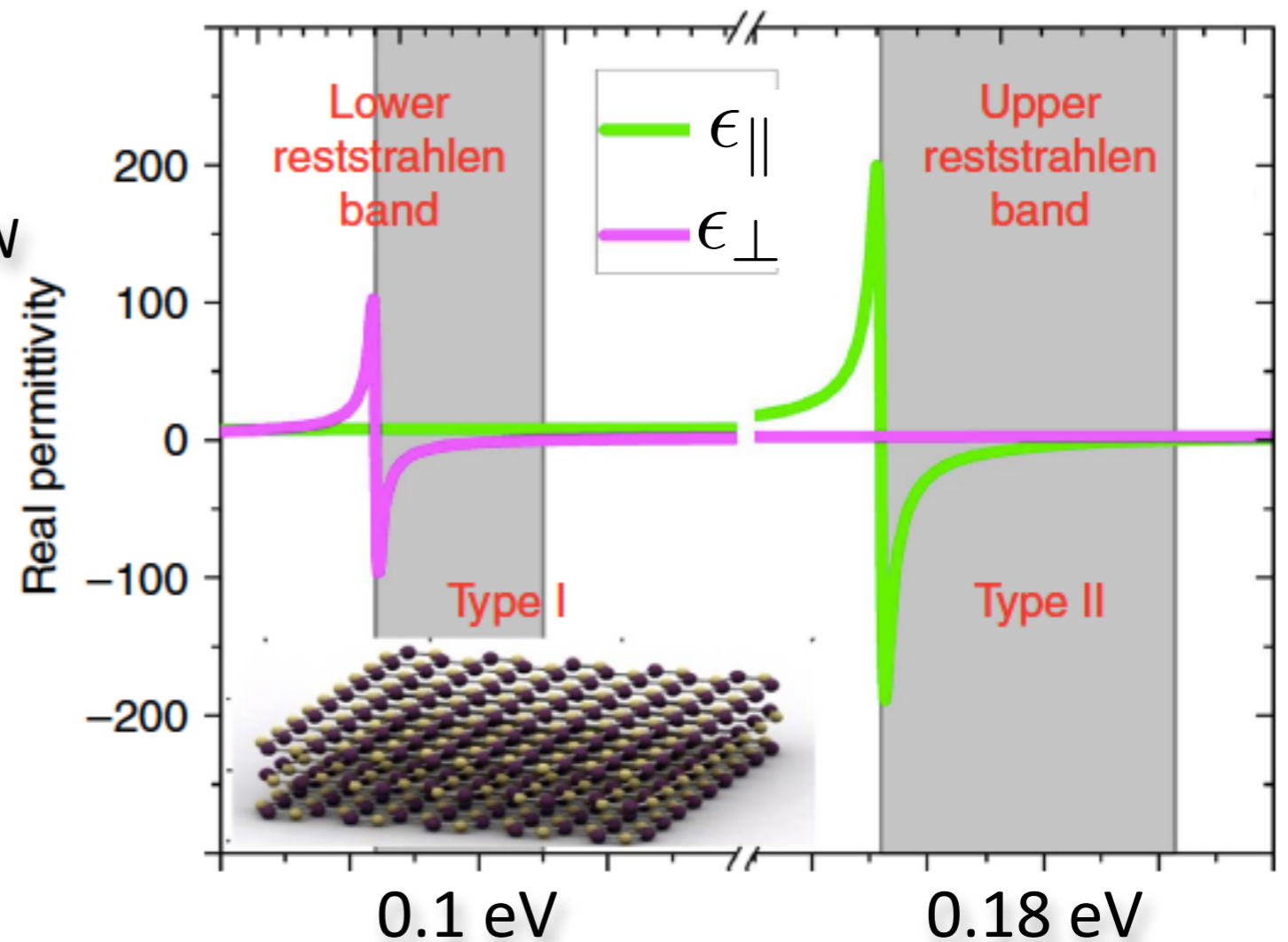
Very inefficient!

=> What about *near-field* radiation to encapsulant?

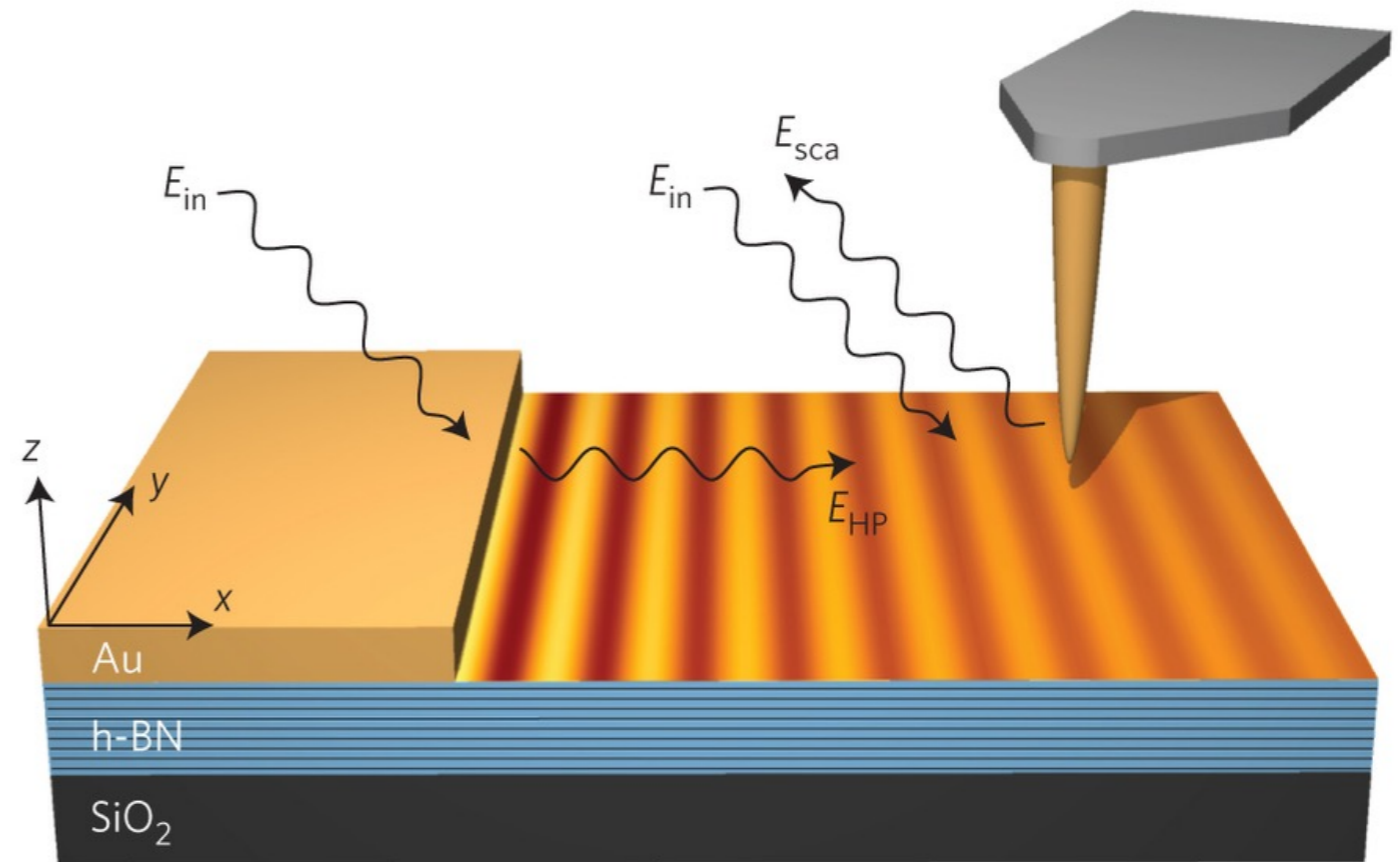
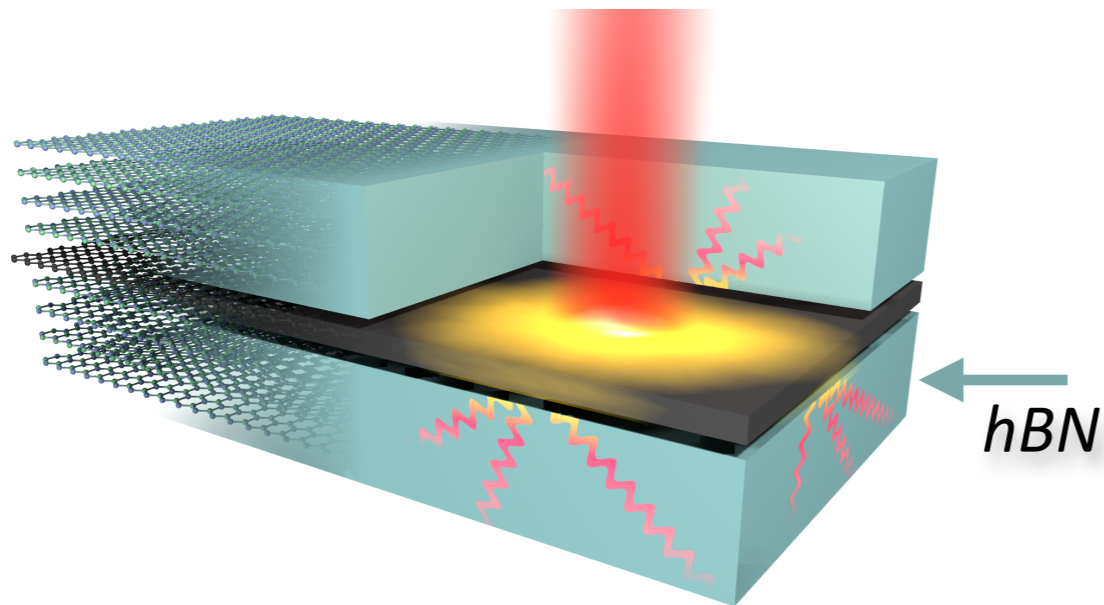
hBN: Hyperbolic phonons



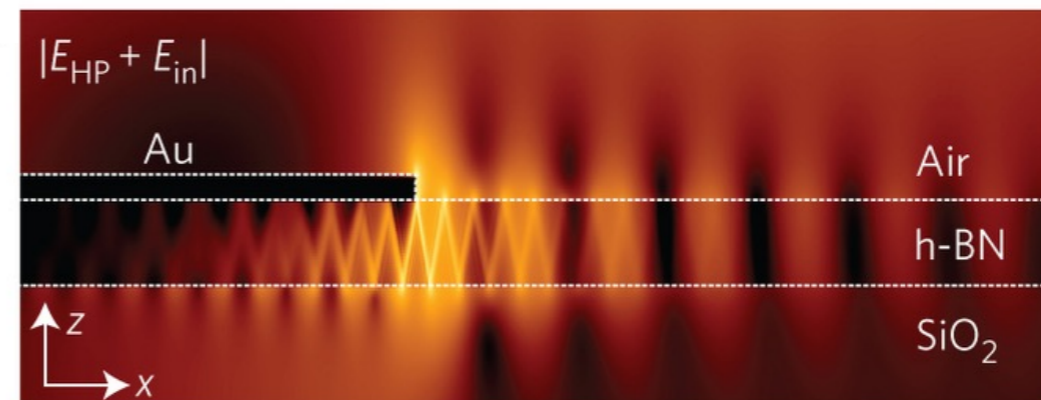
Hyperbolic modes:
 $\text{sgn}(\epsilon_{\perp}) \neq \text{sgn}(\epsilon_{\parallel})$



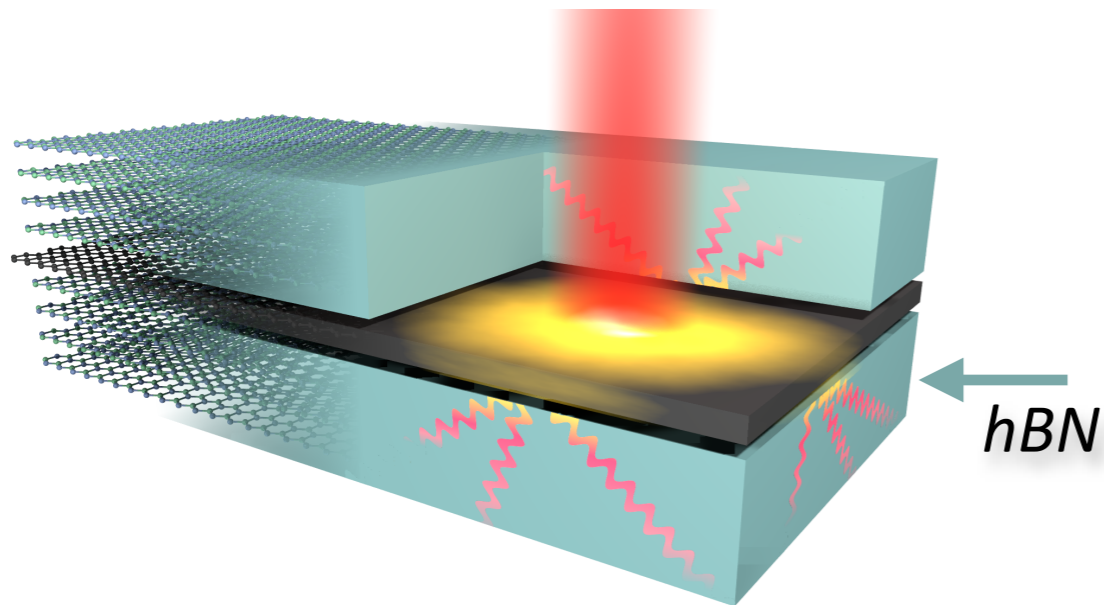
hBN: Hyperbolic phonons



Hyperbolic modes:
 $\text{sgn}(\epsilon_{\perp}) \neq \text{sgn}(\epsilon_{\parallel})$

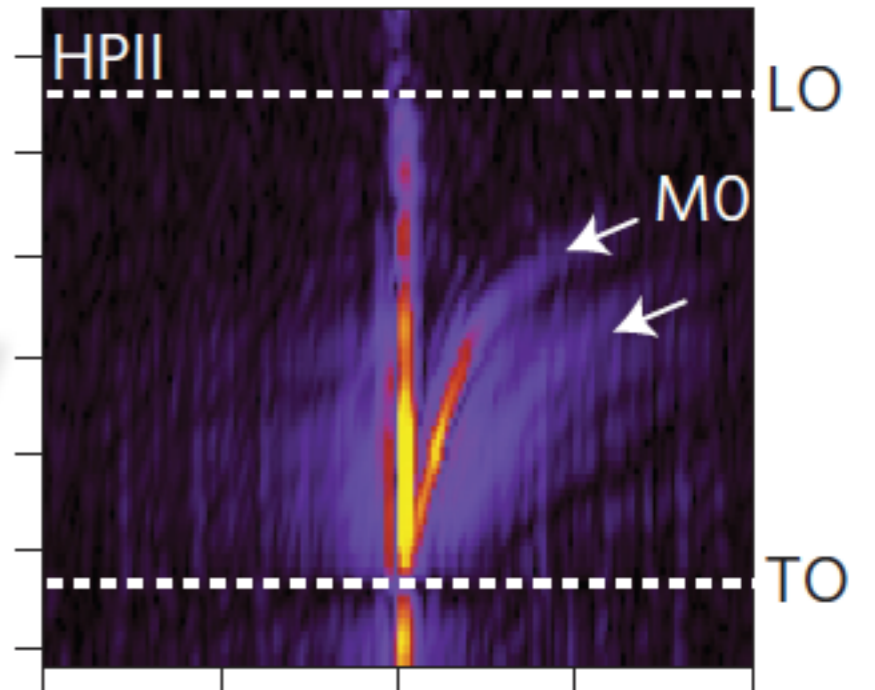


hBN: Hyperbolic phonons

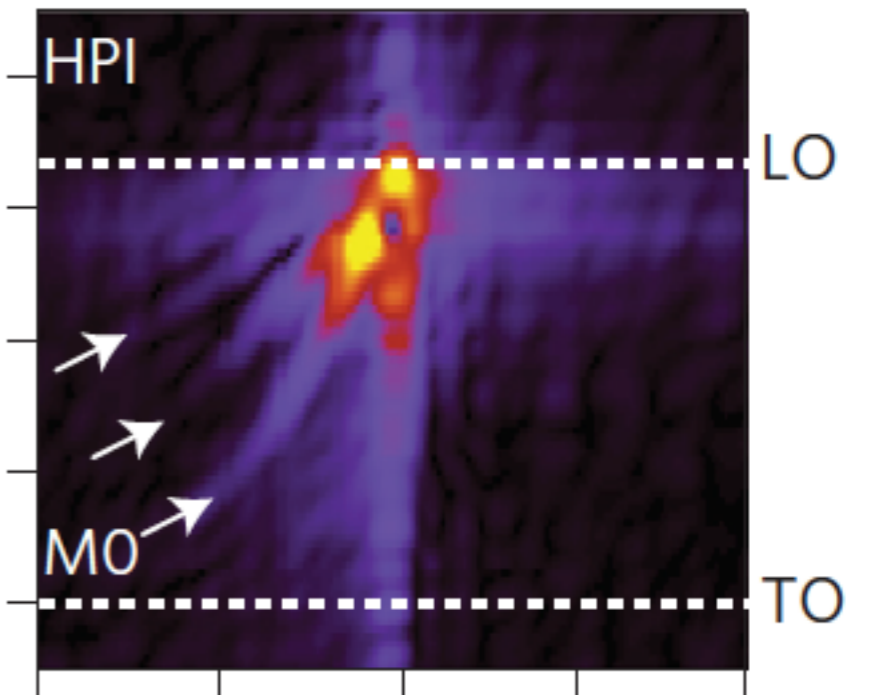


Hyperbolic modes:
 $\text{sgn}(\epsilon_{\perp}) \neq \text{sgn}(\epsilon_{\parallel})$

$E = 0.18 \text{ eV}$

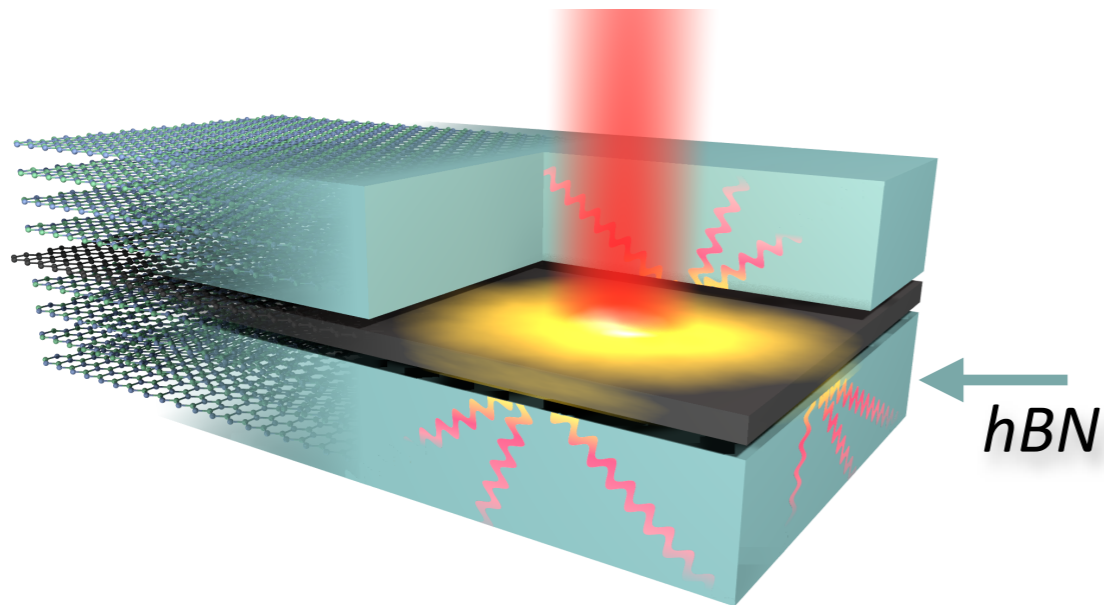


$E = 0.1 \text{ eV}$



$k = 0$

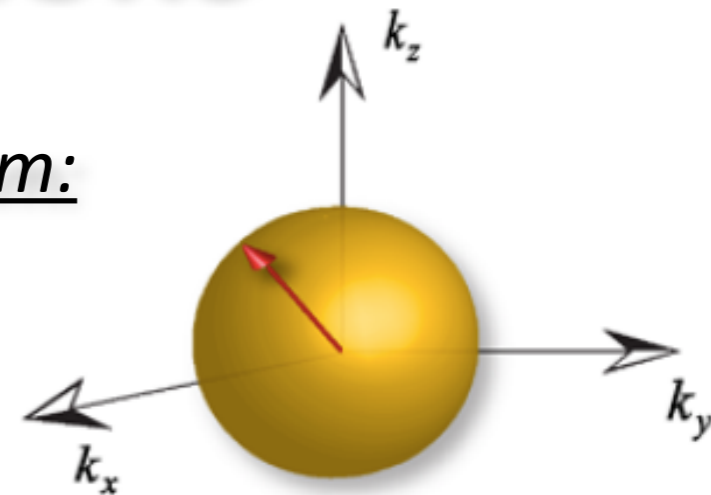
hBN: Hyperbolic phonons



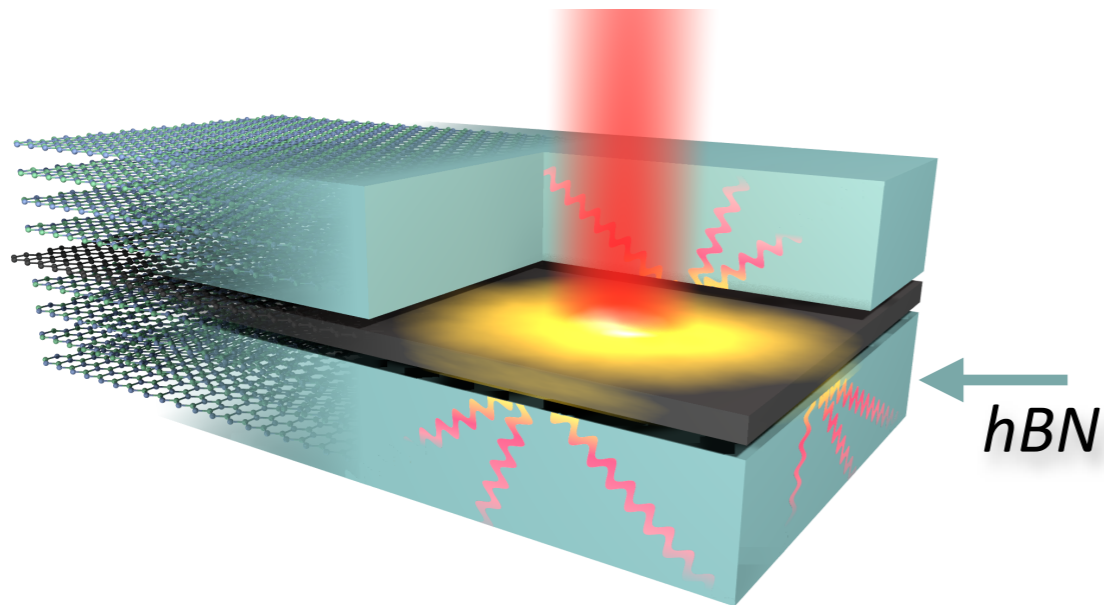
Isotropic medium:

$$\epsilon_{\perp} = \epsilon_{\parallel}$$

$$k = \omega/c$$



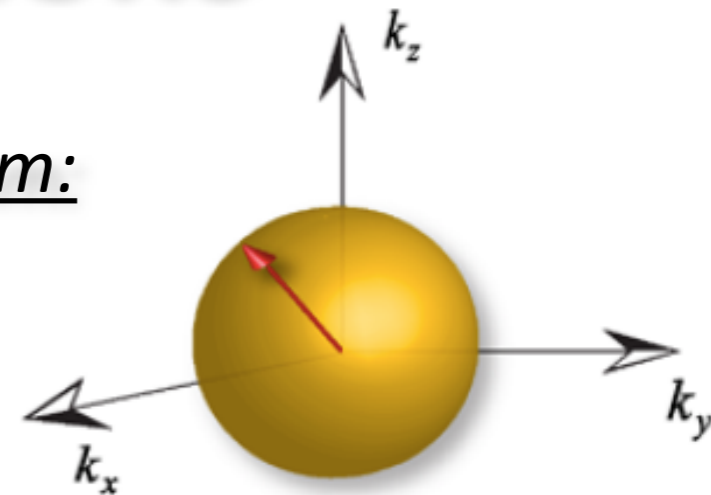
hBN: Hyperbolic phonons



Isotropic medium:

$$\epsilon_{\perp} = \epsilon_{\parallel}$$

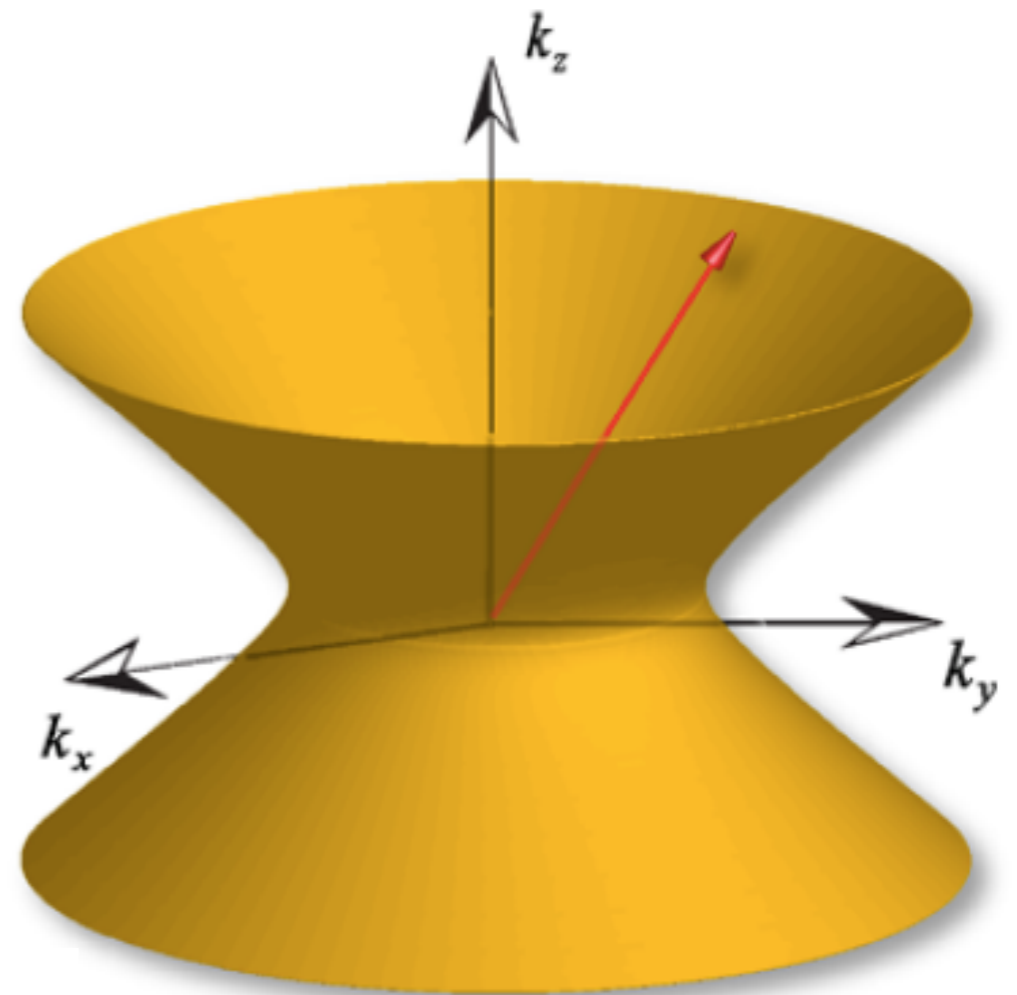
$$k = \omega/c$$



Hyperbolic mode (Type II):

$$\text{sgn}(\epsilon_{\perp}) \neq \text{sgn}(\epsilon_{\parallel})$$

$$k \gg \omega/c$$

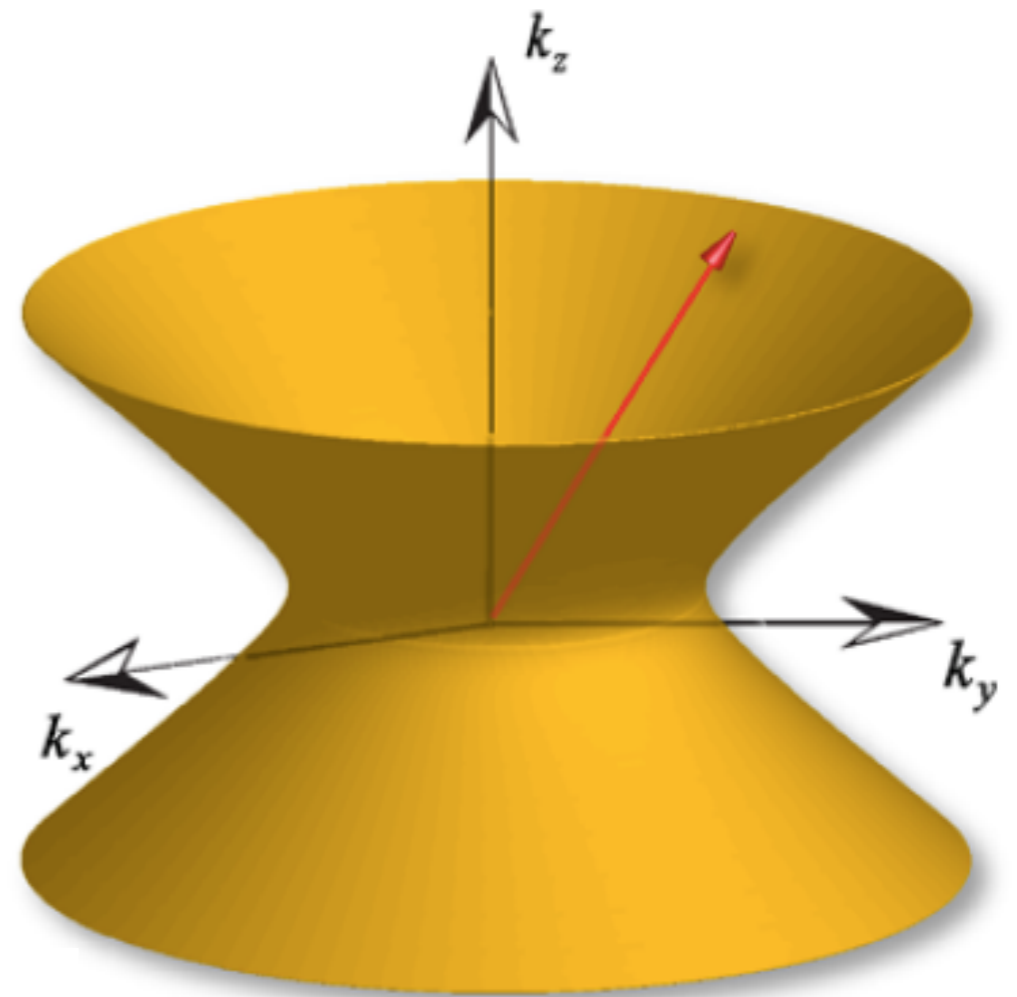
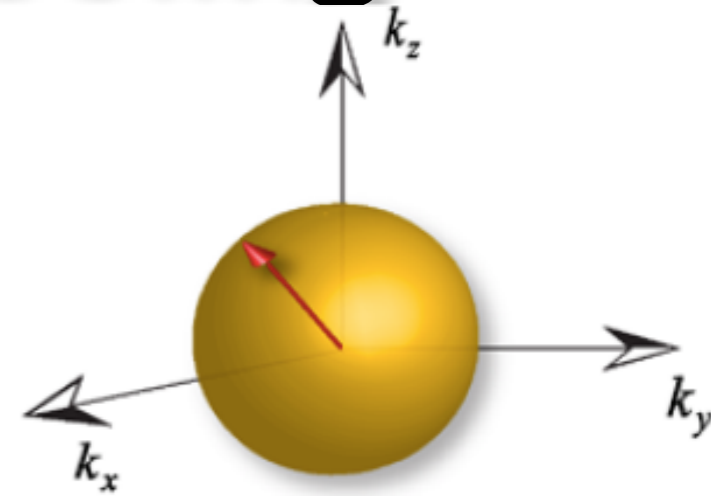


Near-field, hyperbolic cooling

Graphene in vacuum

- Light cone with restricted k -vectors
- *Low thermal energy density*

➔ **Blackbody Planck radiation (inefficient)**

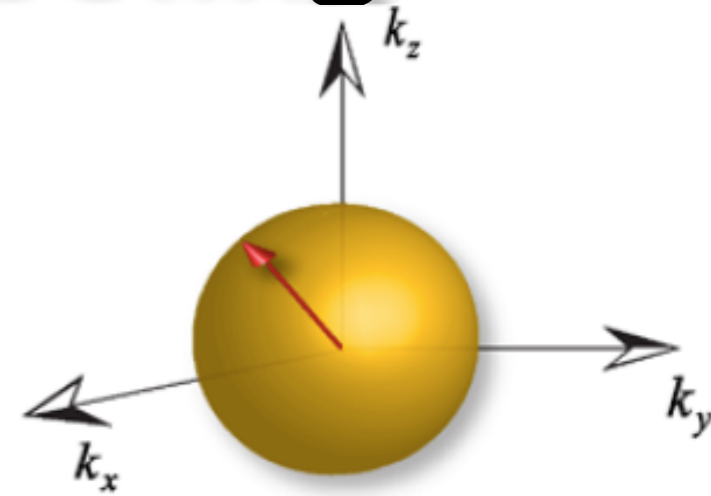


Near-field, hyperbolic cooling

Graphene in vacuum

- Light cone with restricted k -vectors
- *Low thermal energy density*

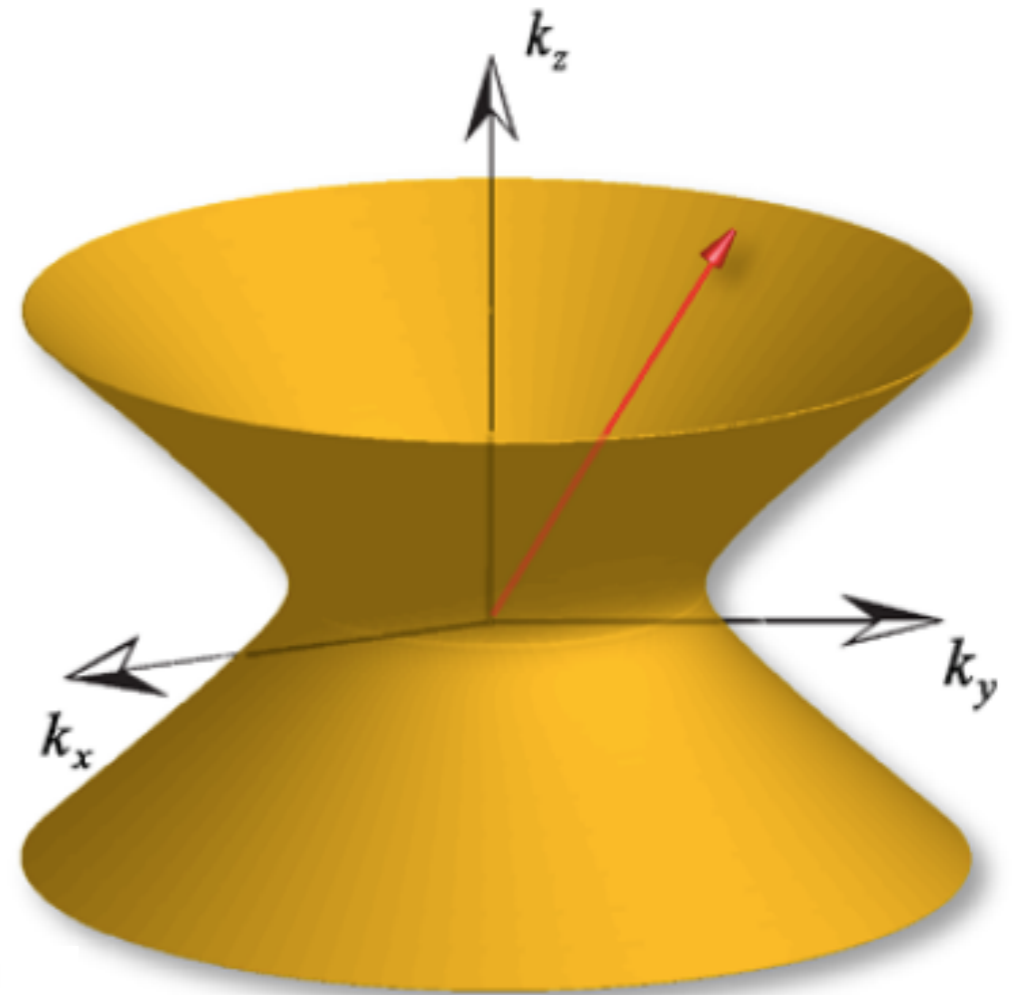
➔ **Blackbody Planck radiation (inefficient)**



hBN-encapsulated graphene

- Hyperbolic modes with near-infinite range of k -vectors
- *High thermal energy density*

➔ **Super-Planckian radiation (very efficient)**



More efficient than graphene phonon cooling?

Experiment

Hot graphene electrons

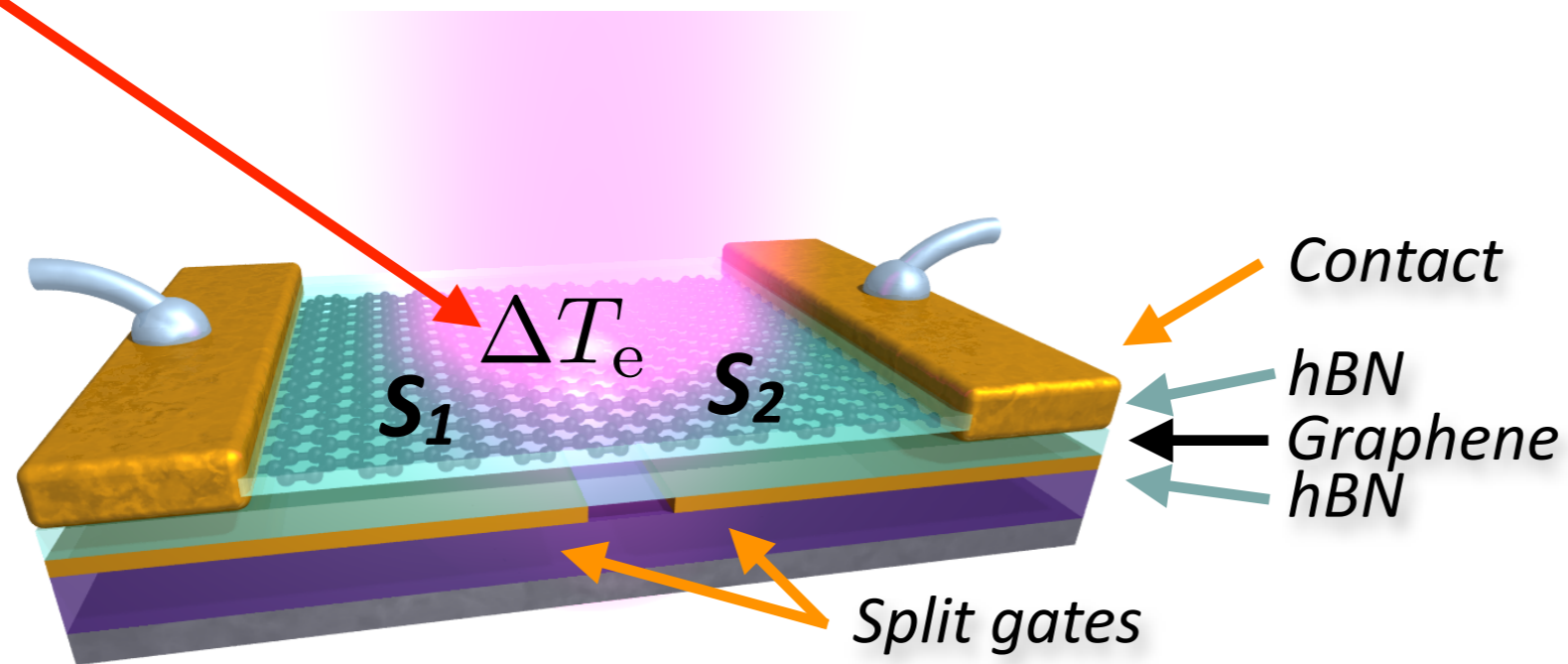
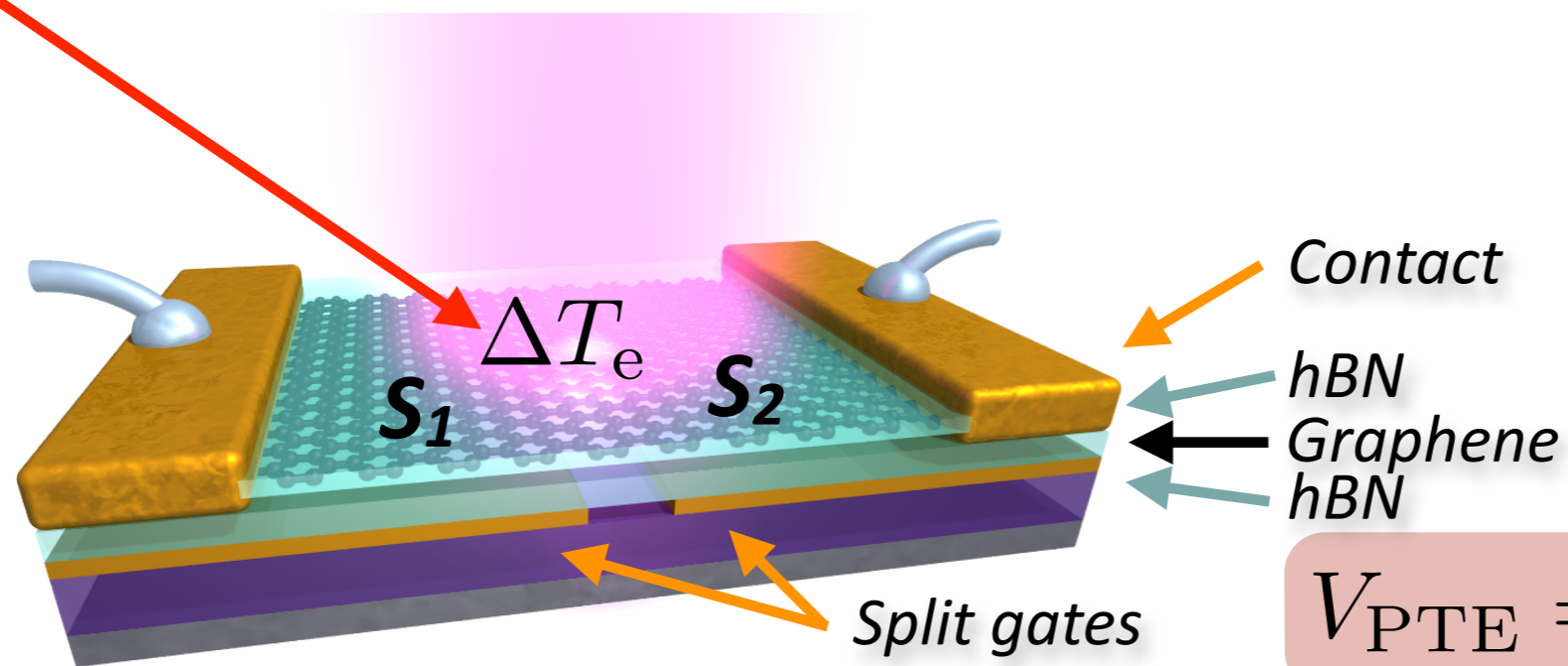


Photo-thermoelectric (PTE) detector

Experiment

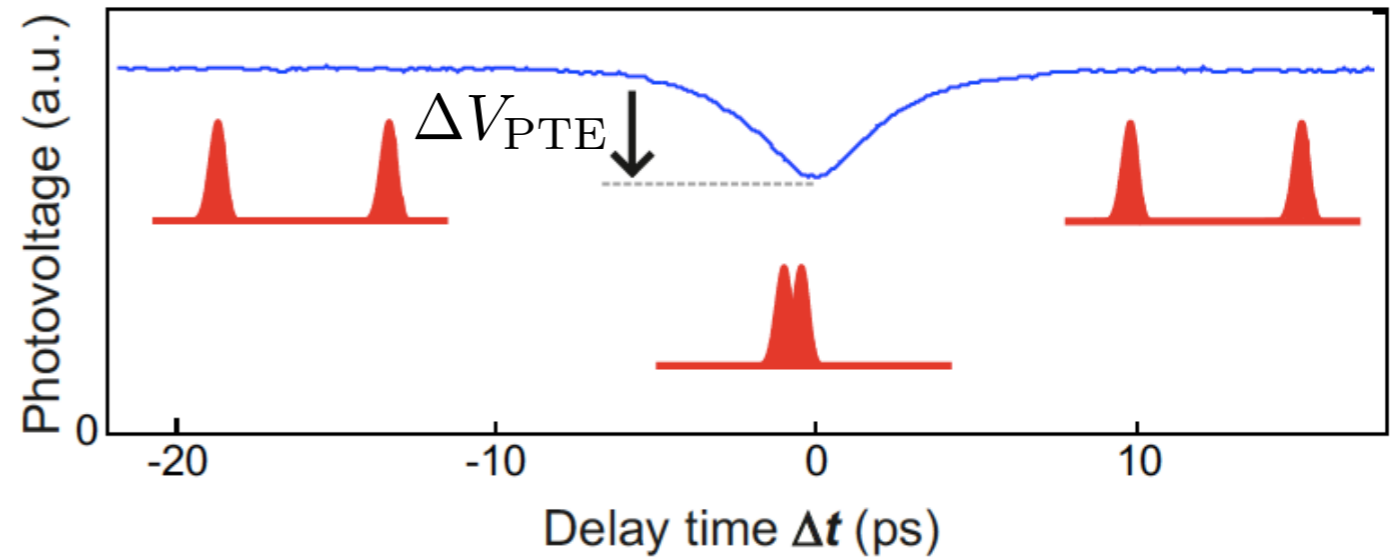
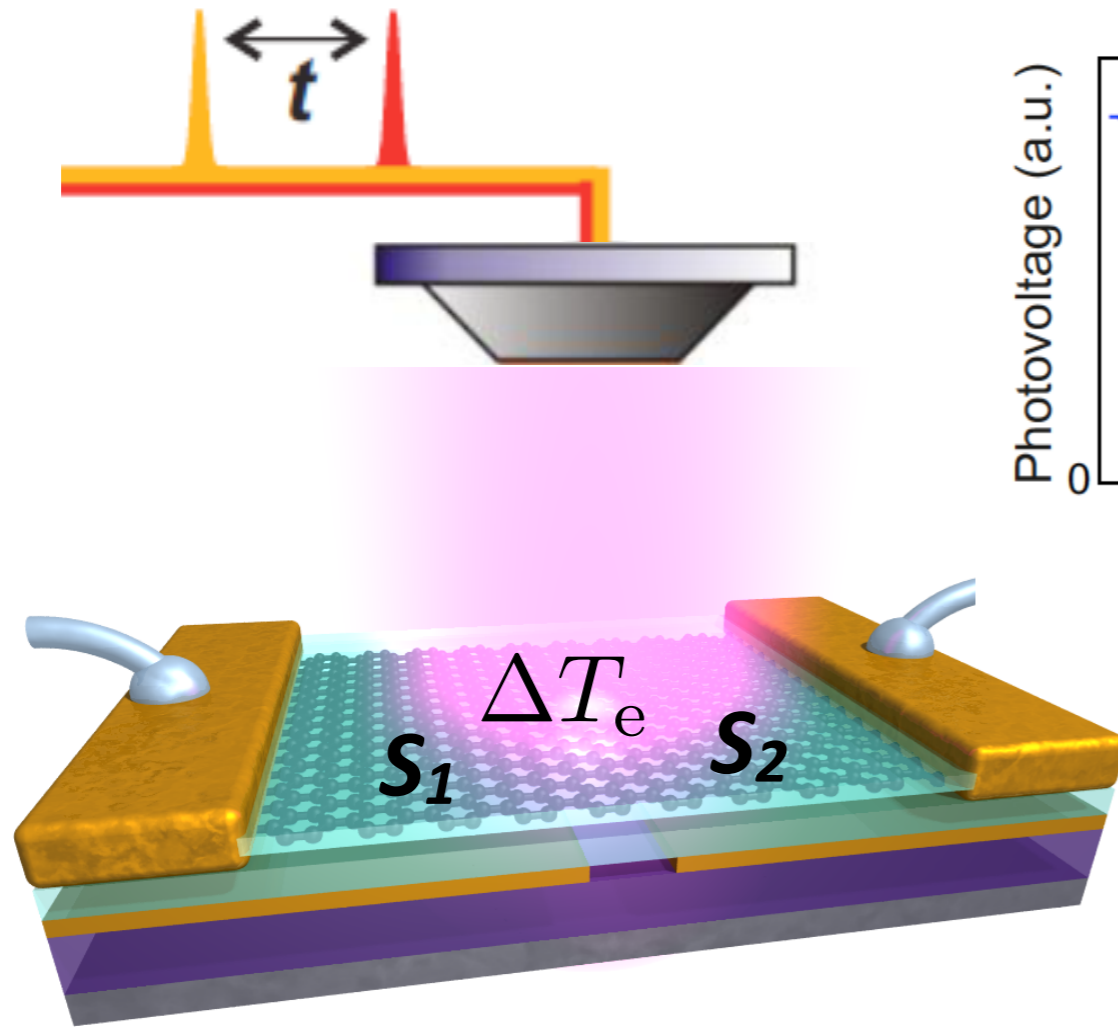
Hot graphene electrons



$$V_{\text{PTE}} = (S_2 - S_1) \Delta T_e$$

Photo-thermoelectric (PTE) detector

Experiment

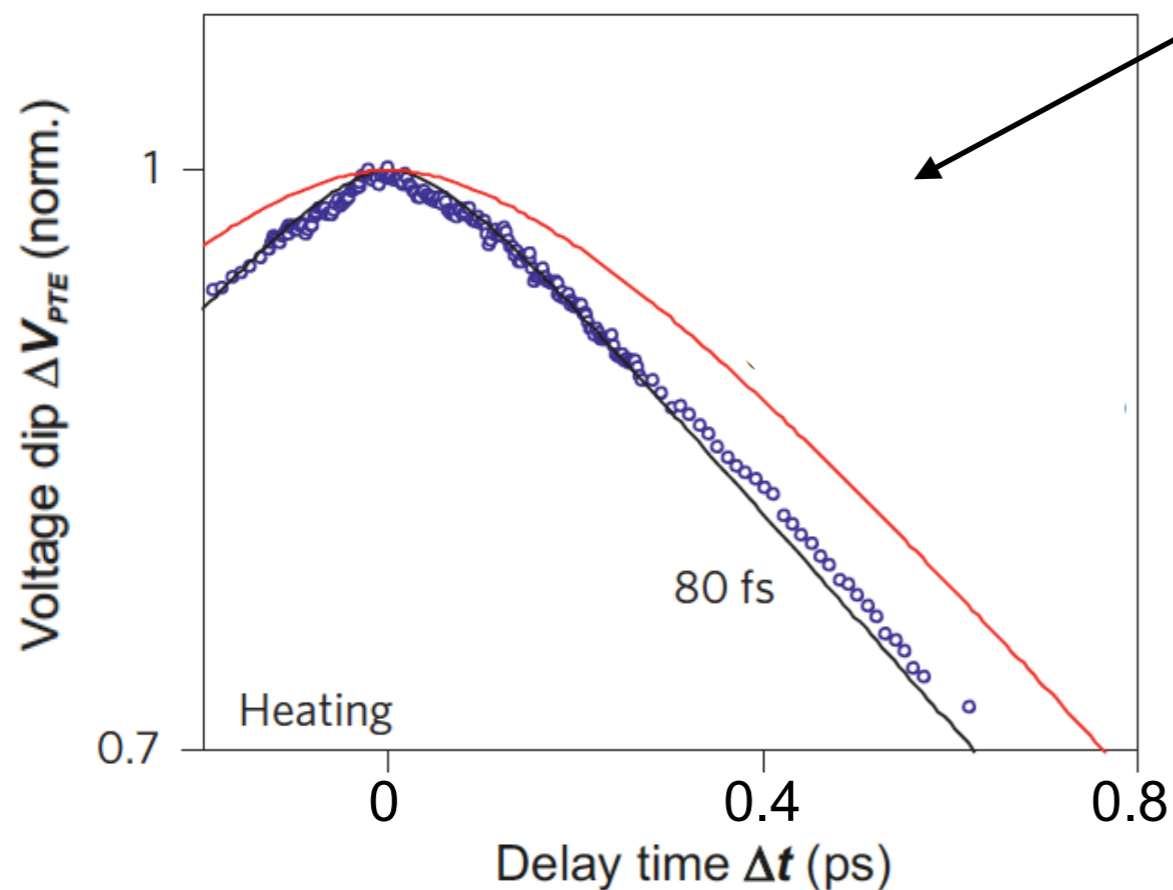
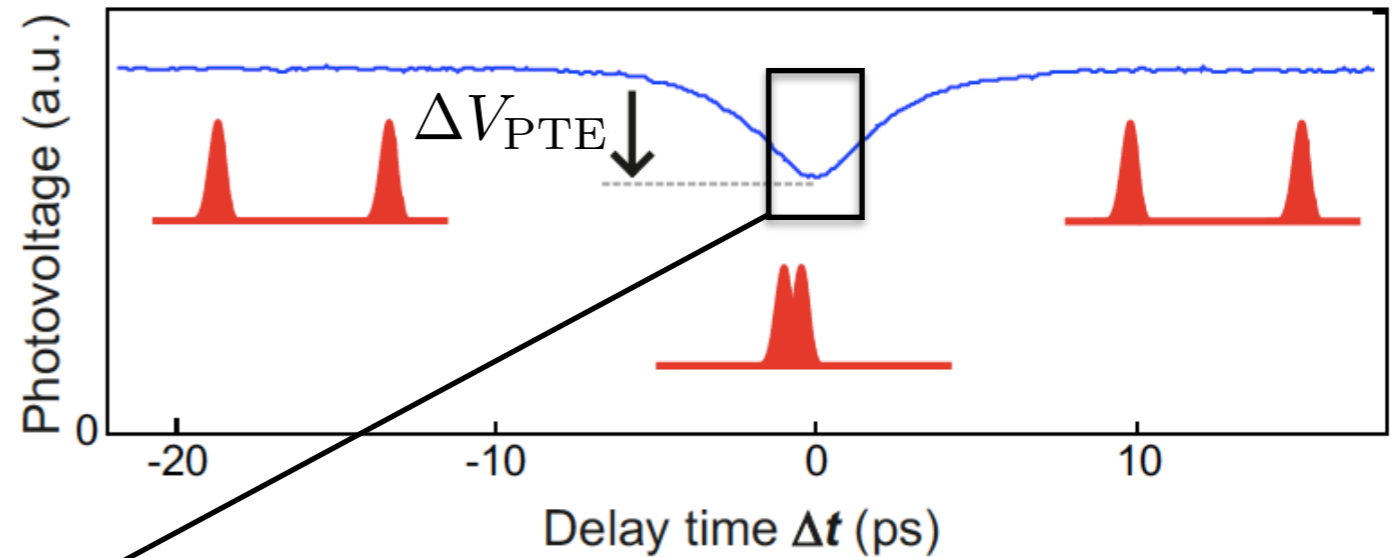


$$V_{\text{PTE}} = (S_2 - S_1) \Delta T_e$$

Access to temperature dynamics!

$$\Delta V_{\text{PTE}}(\Delta t) \sim \Delta T_e(\Delta t)$$

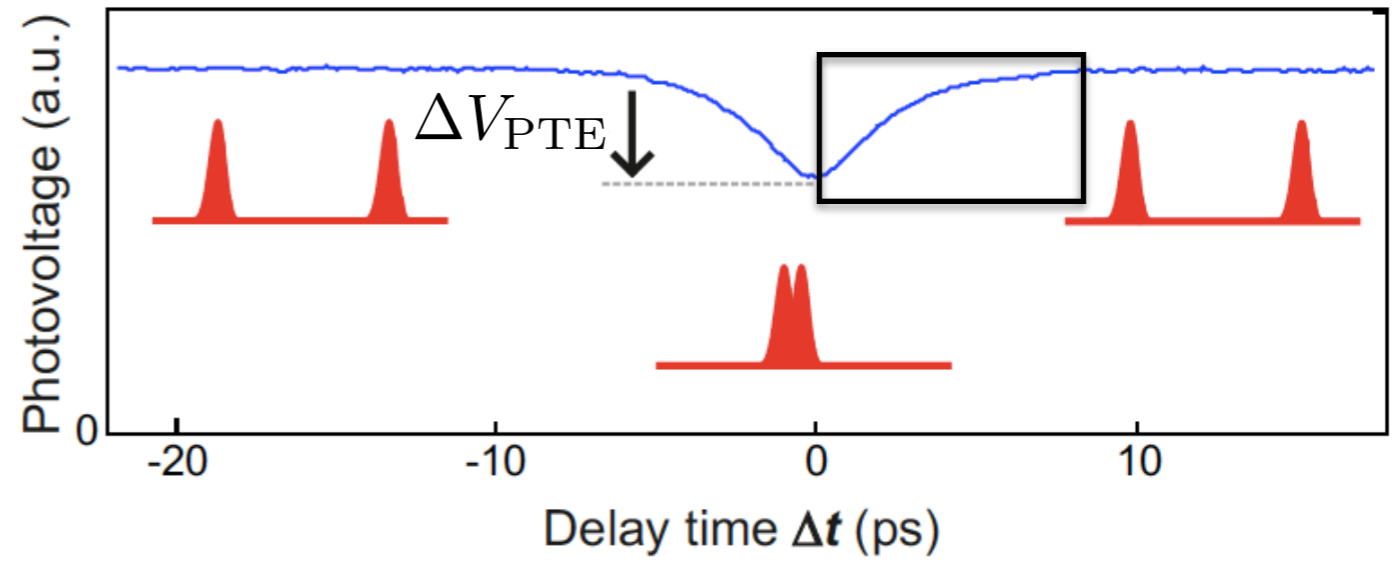
Ultrafast heating



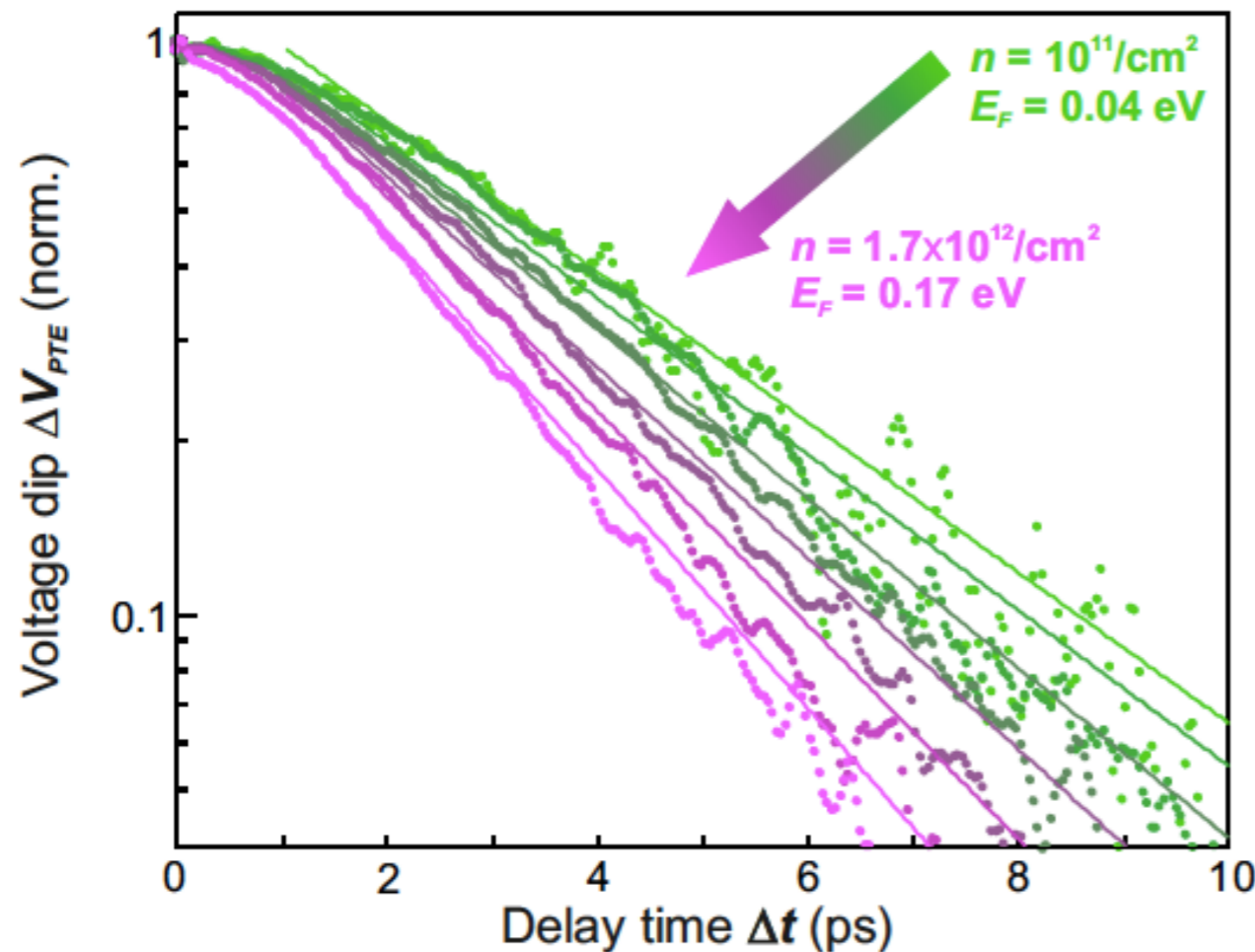
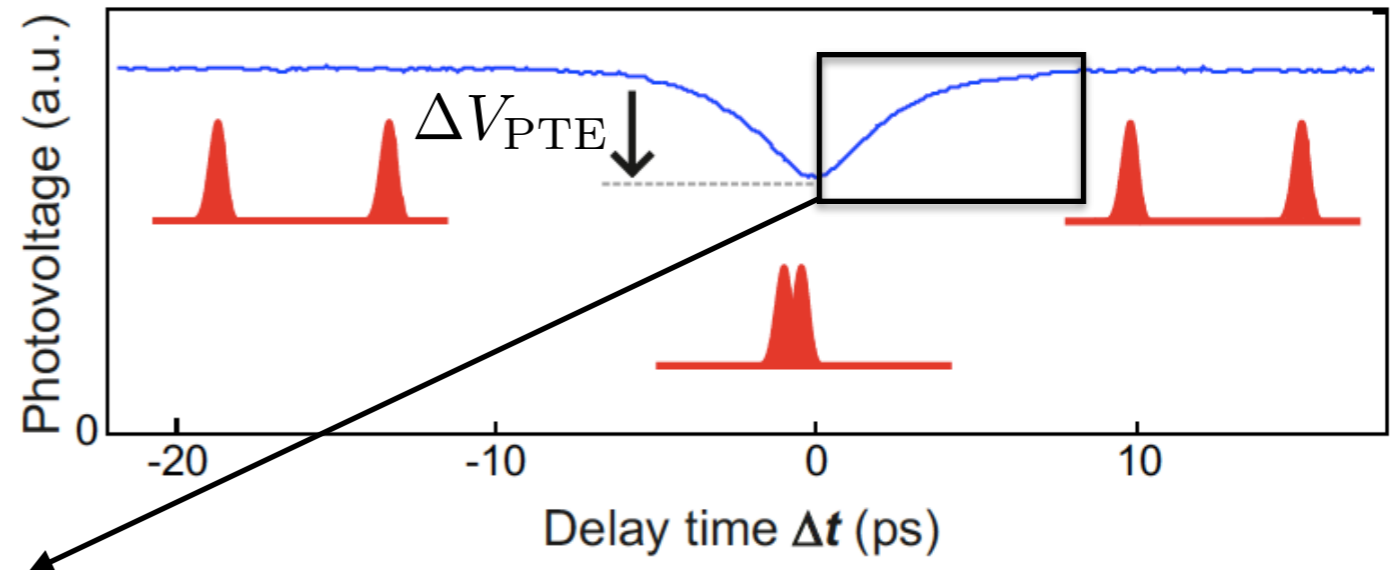
- Ultrafast response function of photodetector
- Ultrafast generation of hot electrons

→ Ultrafast generation of local photovoltage: <80 fs

Cooling: varying carrier density



Cooling: varying carrier density



Cooling time $\sim 2-3$ ps



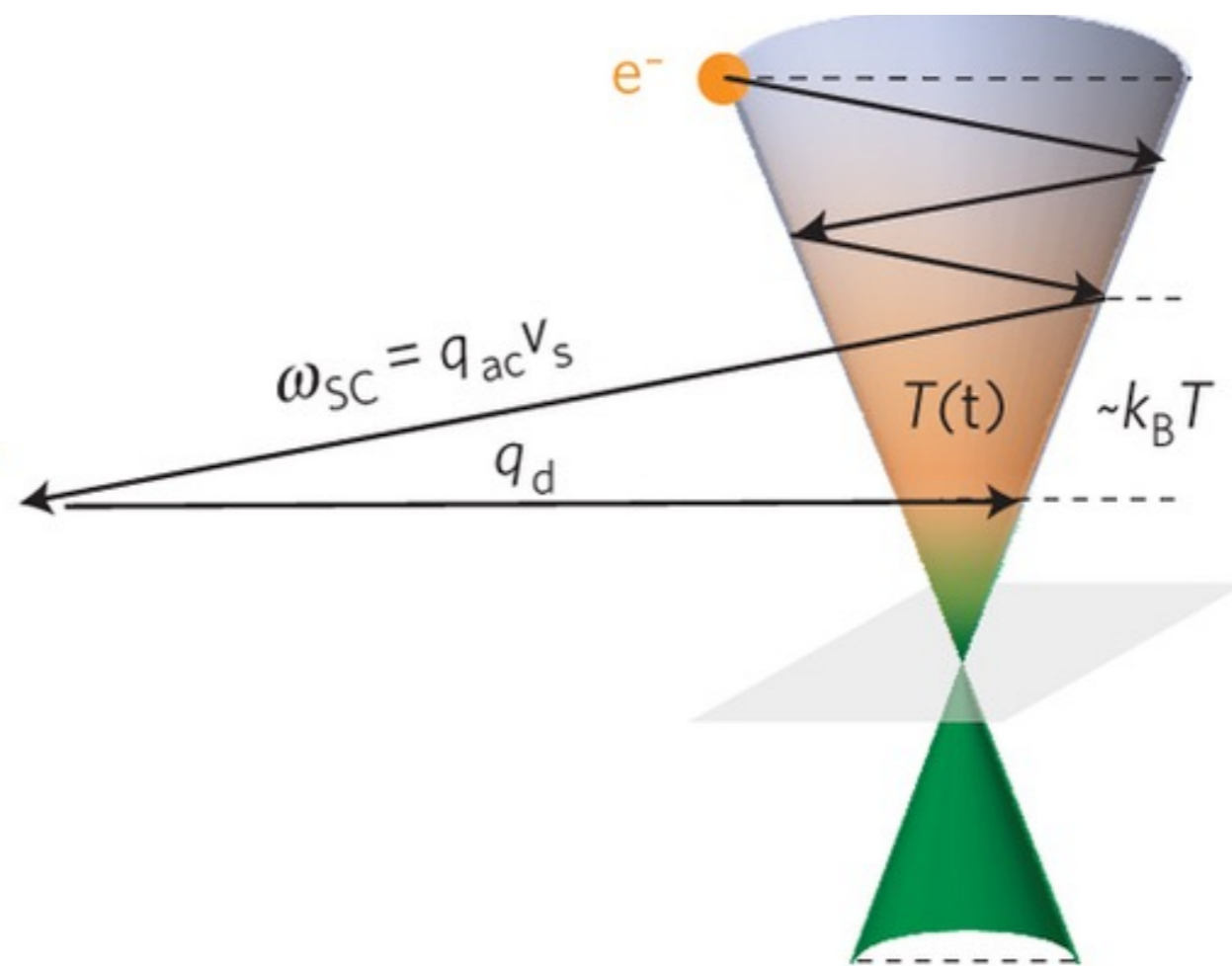
Faster cooling for *higher* density

Super-collision cooling?

Disorder-assisted scattering with acoustic graphene phonons:

- Deformation potential
- Disorder density

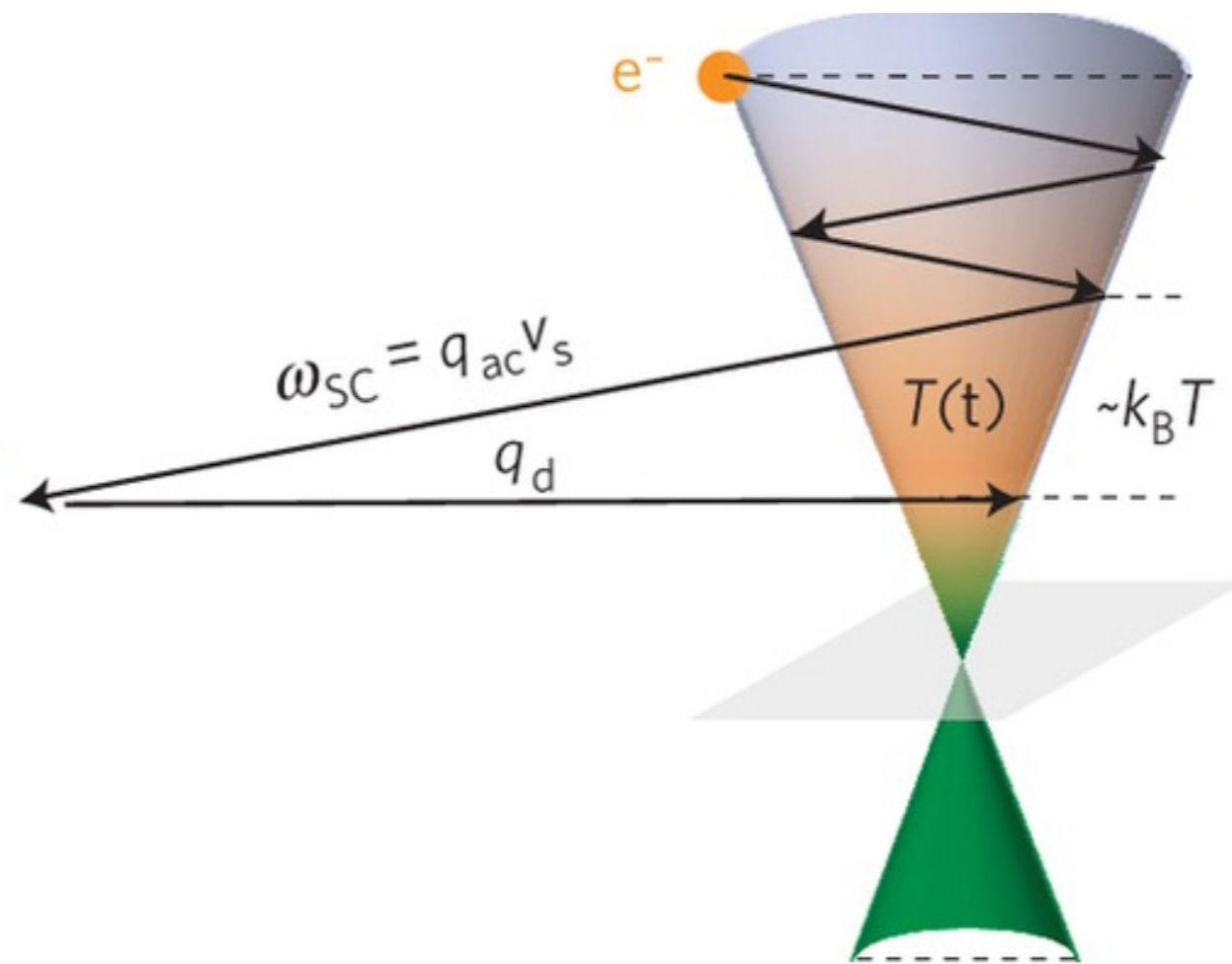
Graham et al. *Nature Phys* (2013)
Song et al. *PRL* (2012)



Super-collision cooling?

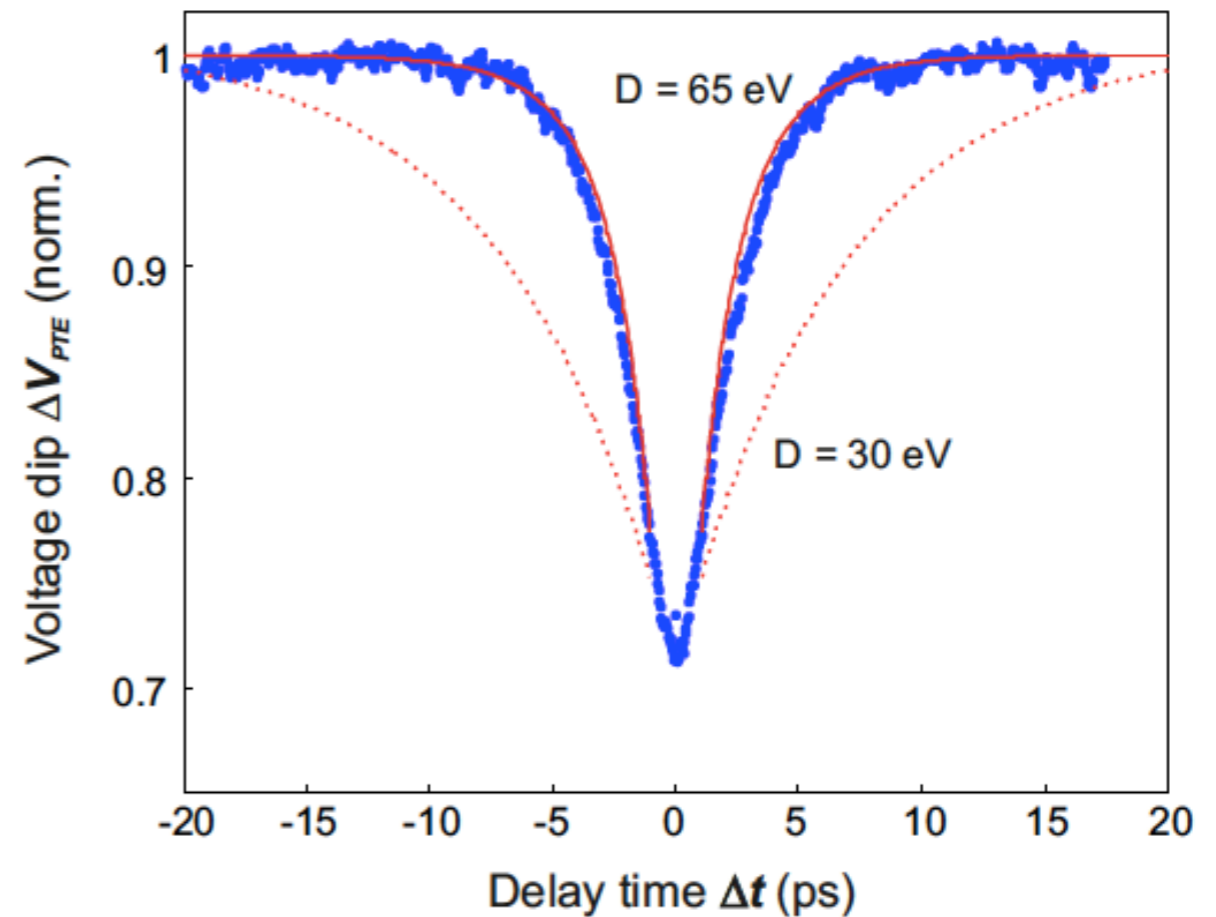
- Super-collision cooling is faster for *lower* carrier density

Graham et al. *Nature Phys* (2013)



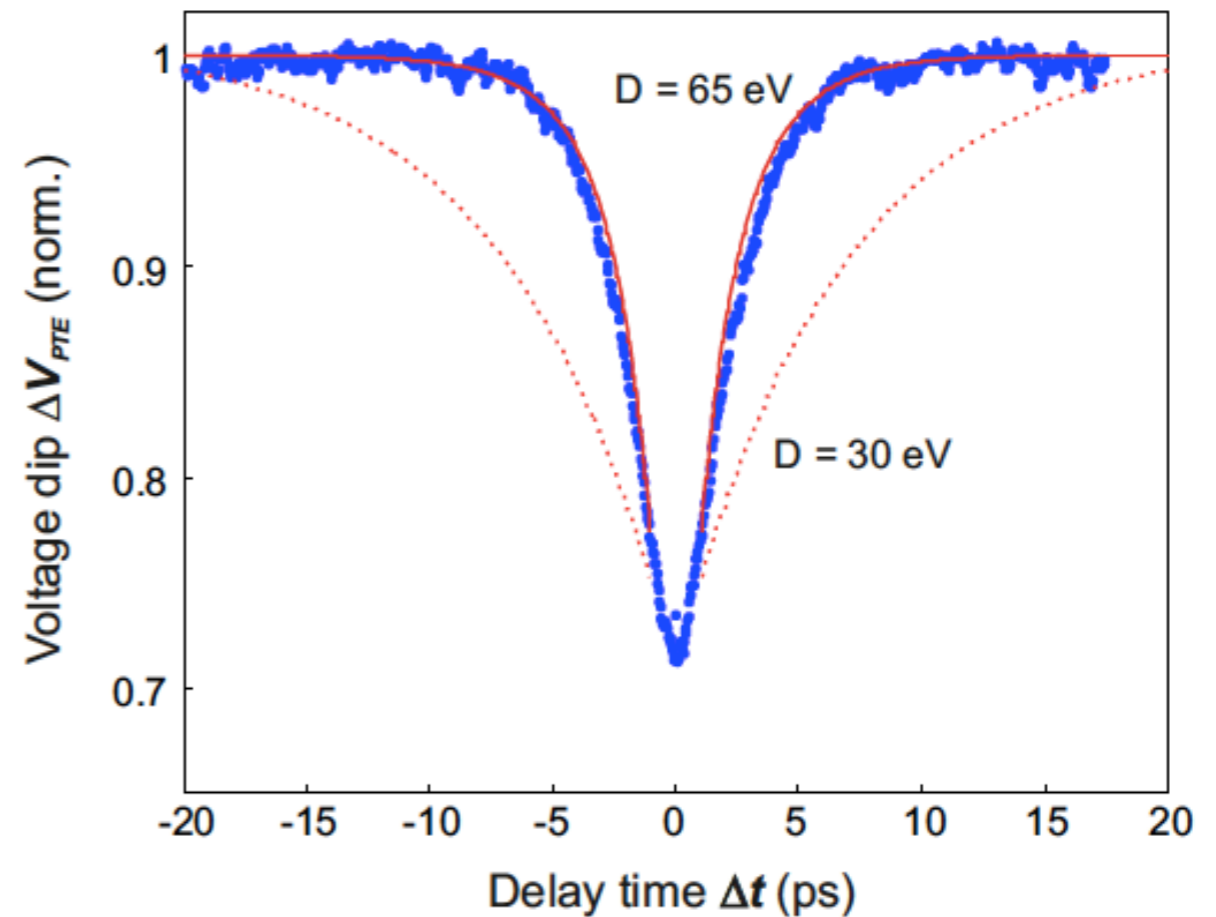
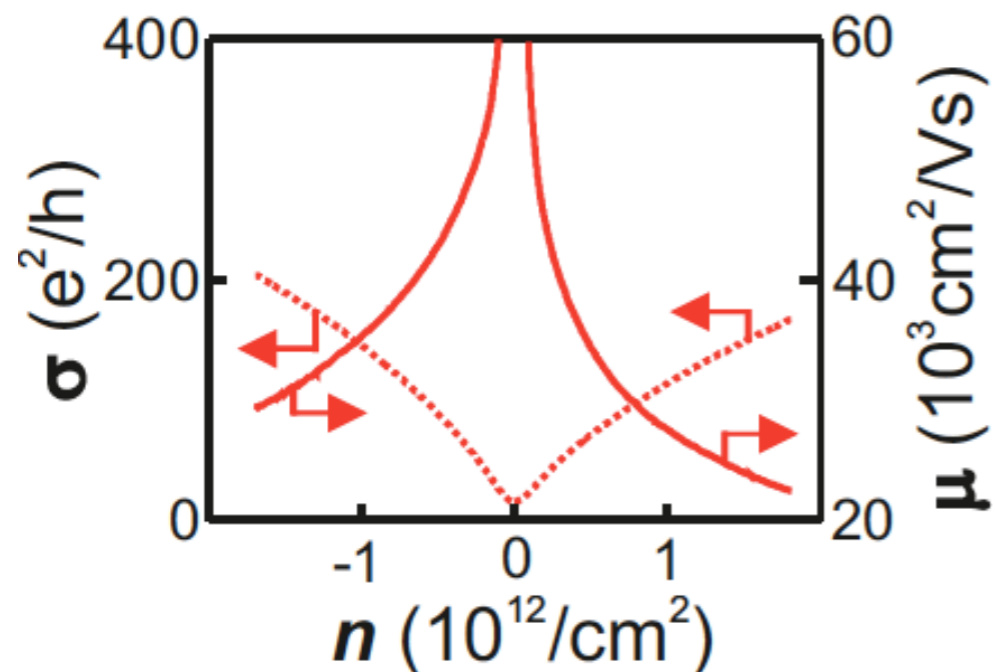
Super-collision cooling?

- Super-collision cooling is faster for *lower* carrier density
- Super-collision cooling requires an unrealistic deformation potential of **65 eV**

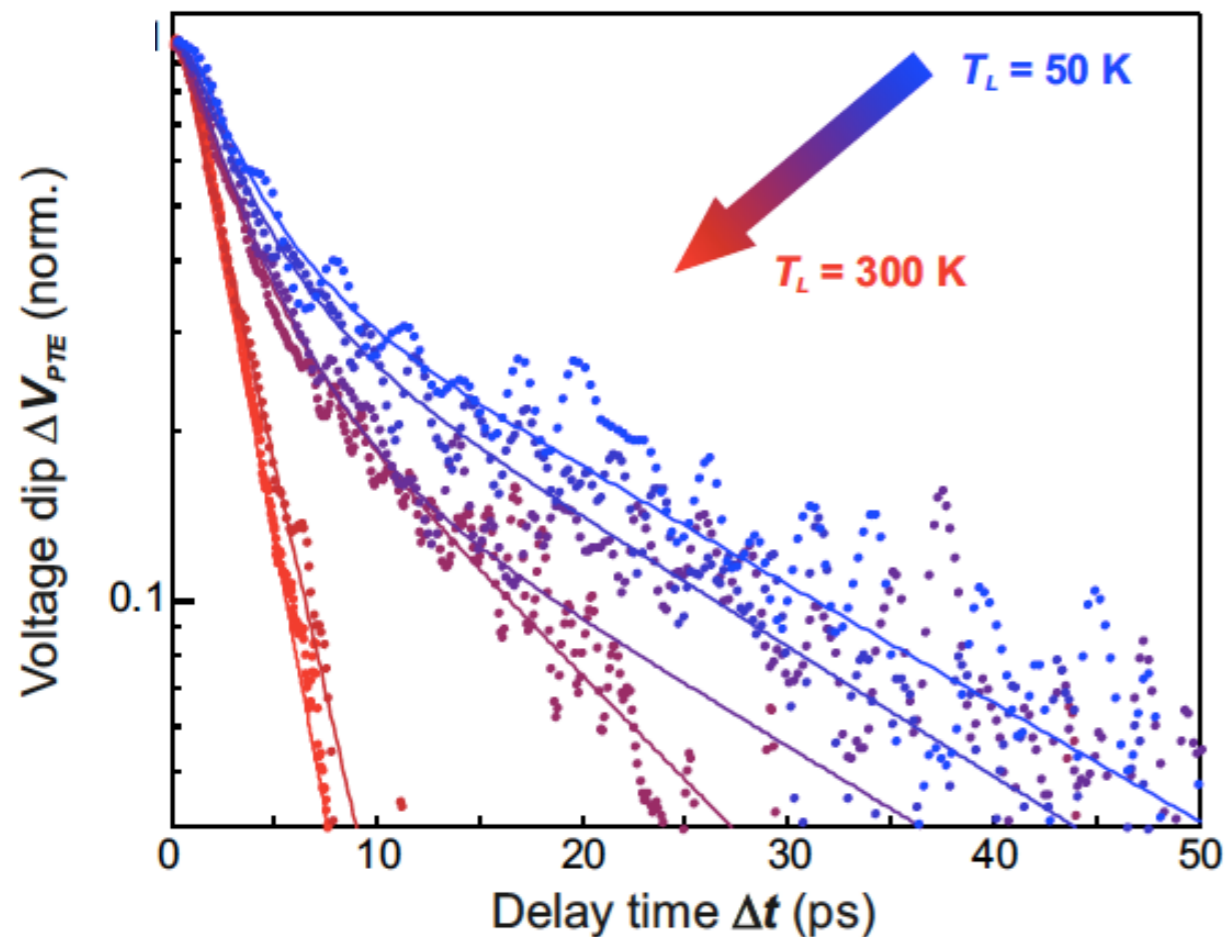
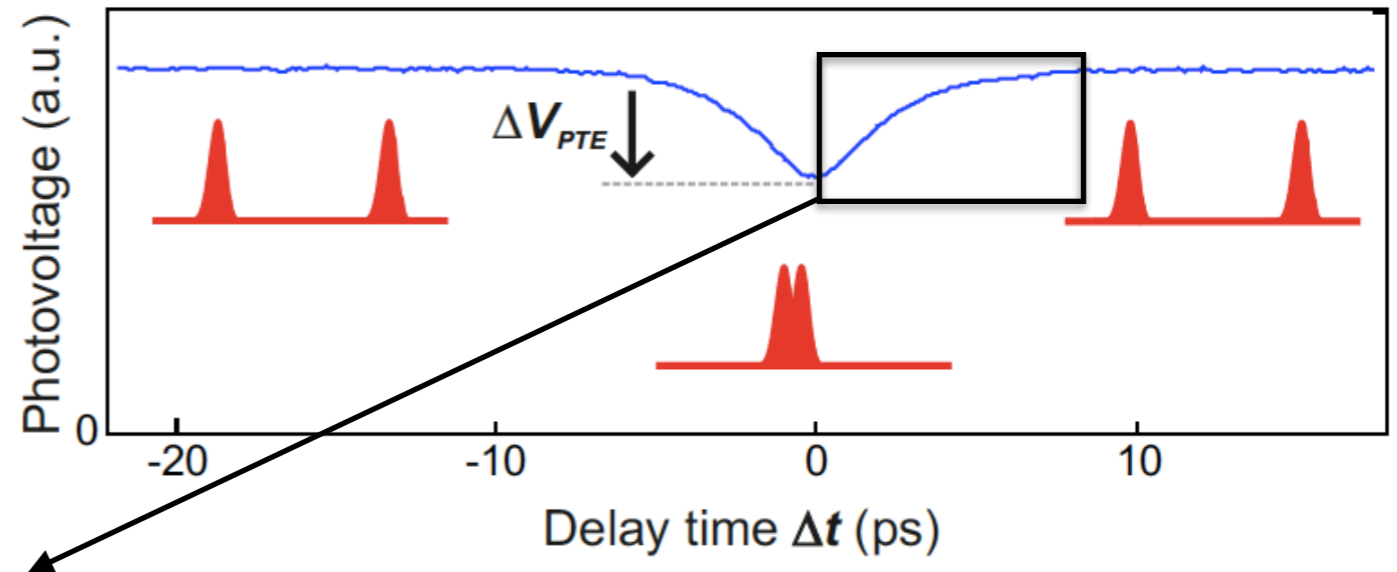


~~Super-collision cooling?~~

- Super-collision cooling is faster for *lower* carrier density
- Super-collision cooling requires an unrealistic deformation potential of **65 eV**
- Our device has a deformation potential **<35 eV**



Cooling: varying lattice temperature



Faster cooling for *higher* lattice temperature

Normal collision cooling?

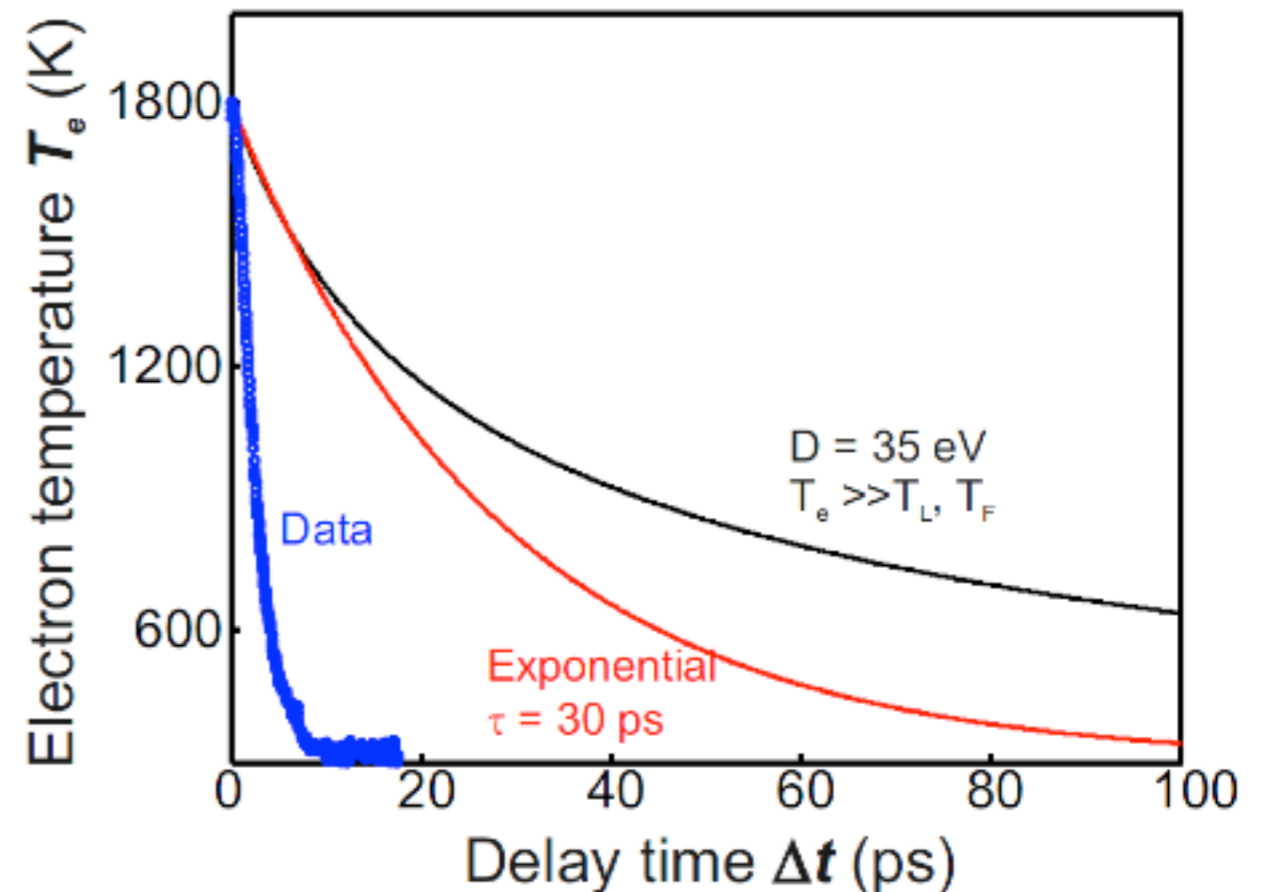
- Normal collision cooling (in overheating) is not dependent on lattice temperature

Bistritzer and MacDonald *PRL* 102, 206410 (2009)

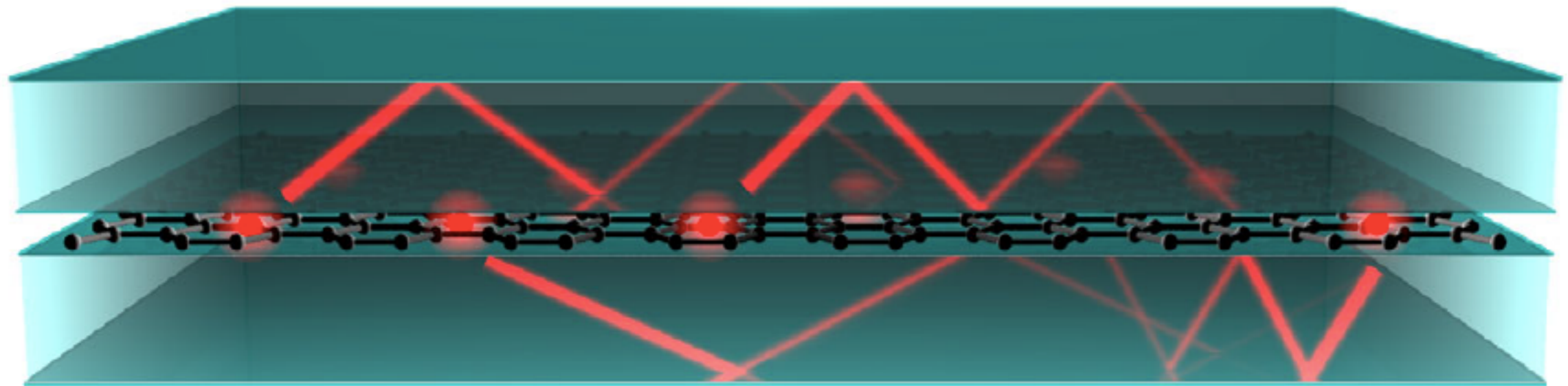
~~Normal collision cooling?~~

- Normal collision cooling (in overheating) is not dependent on lattice temperature
- Normal collision cooling gives non-exponential cooling with a timescale >30 ps at RT

Bistritzer and MacDonald *PRL* 102, 206410 (2009)

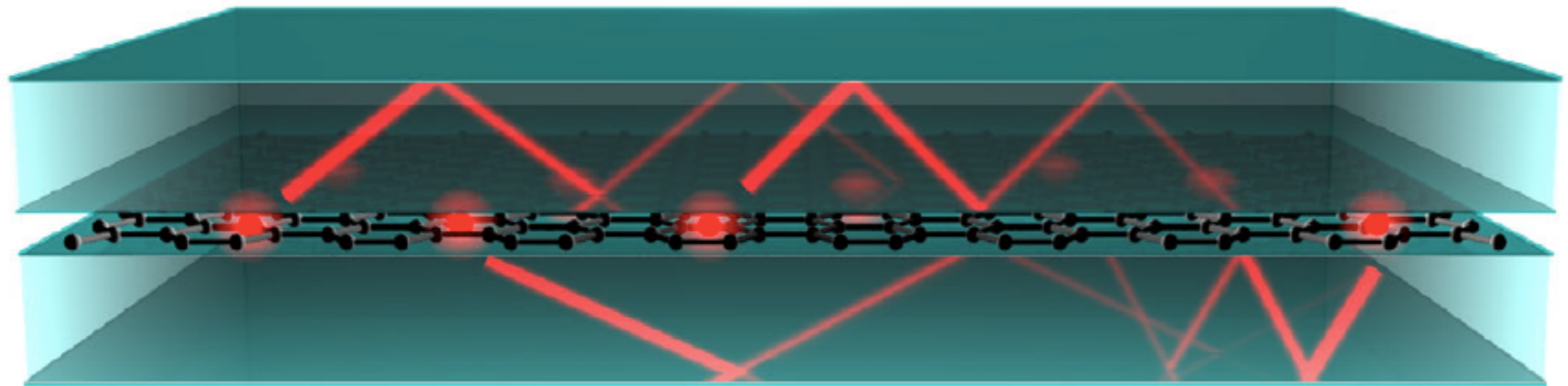


Tielrooij et al, *Arxiv*:1702.03766 (2017)



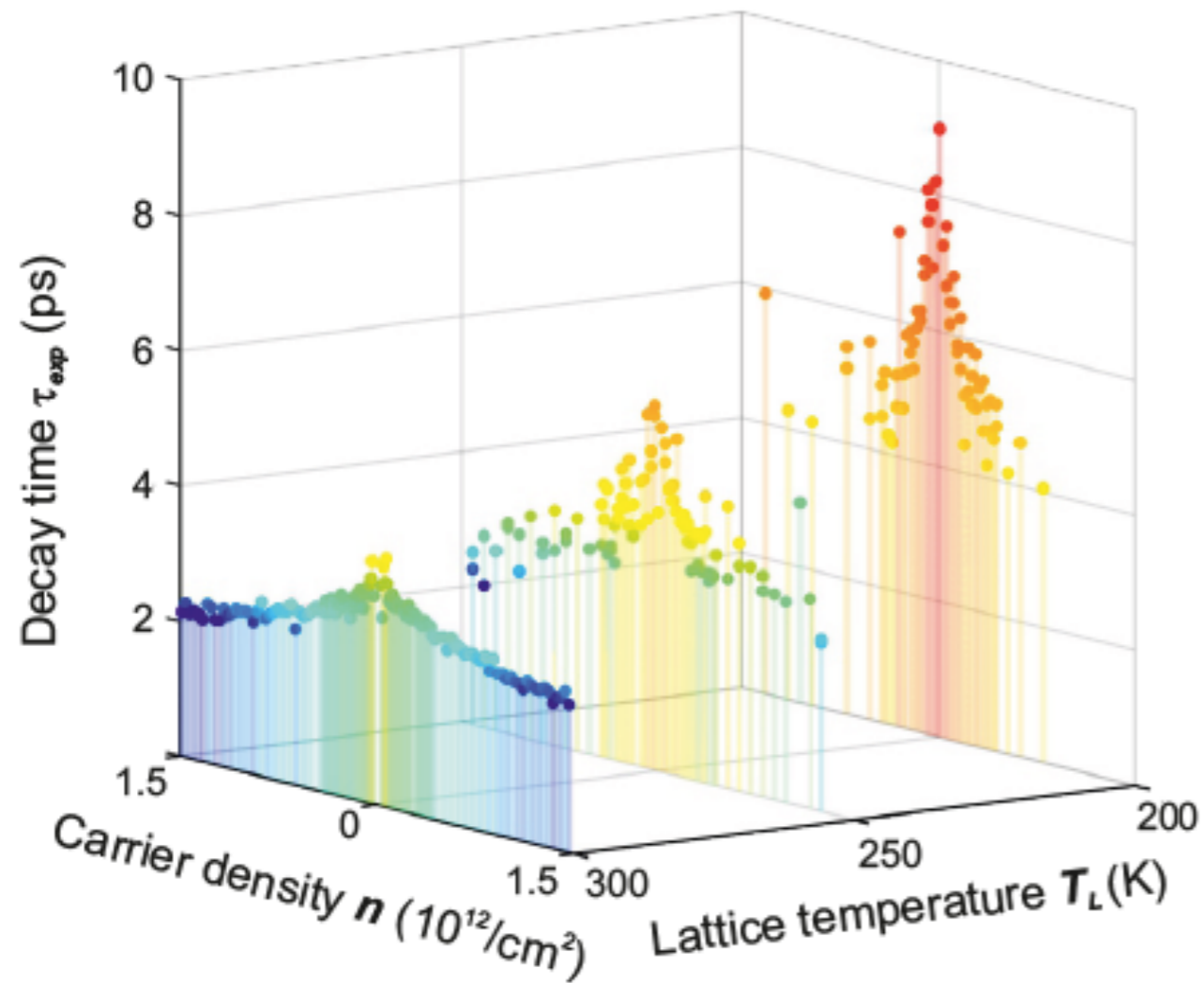
➔ In-plane cooling mechanisms are not consistent with data

Out-of-plane transport!

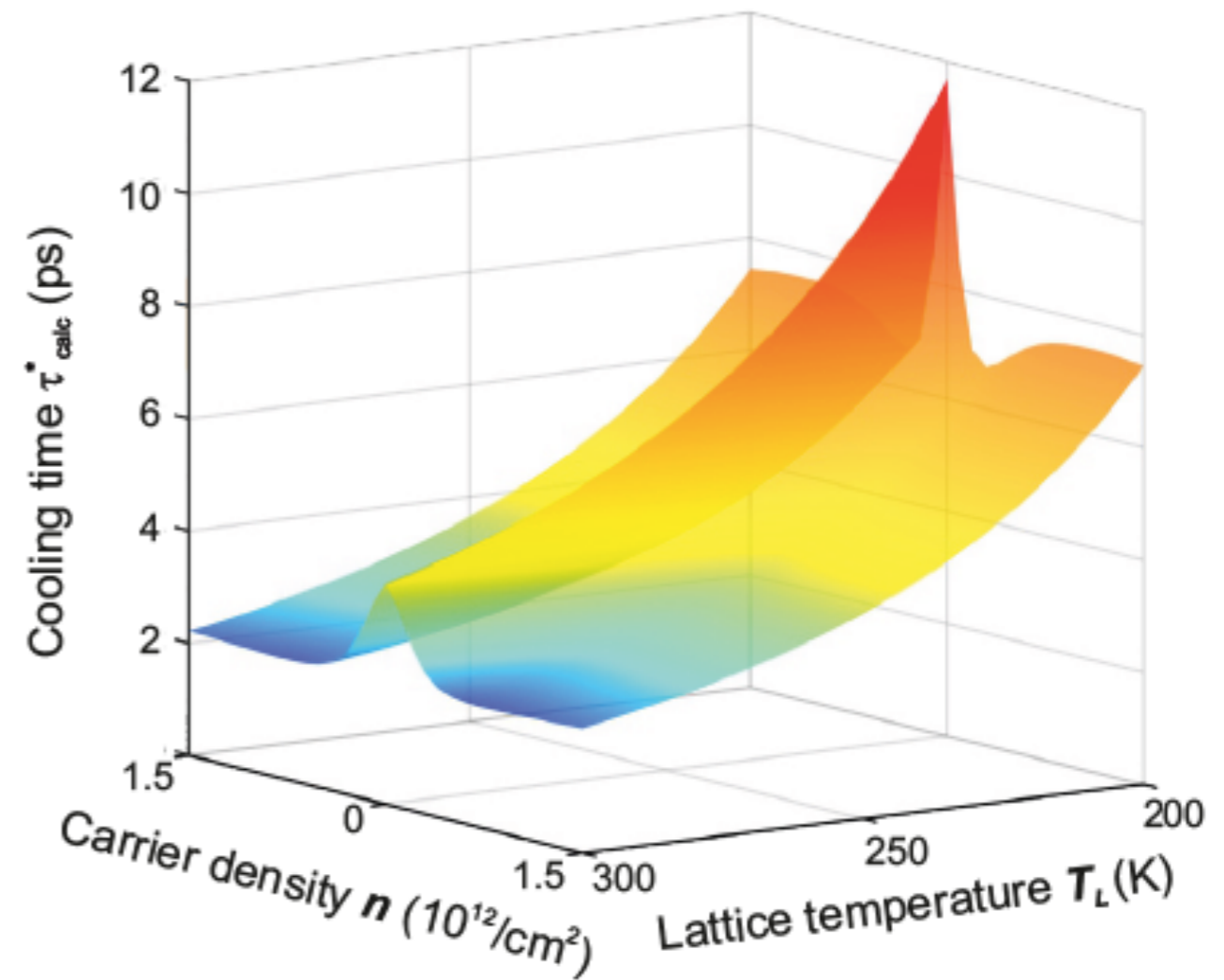
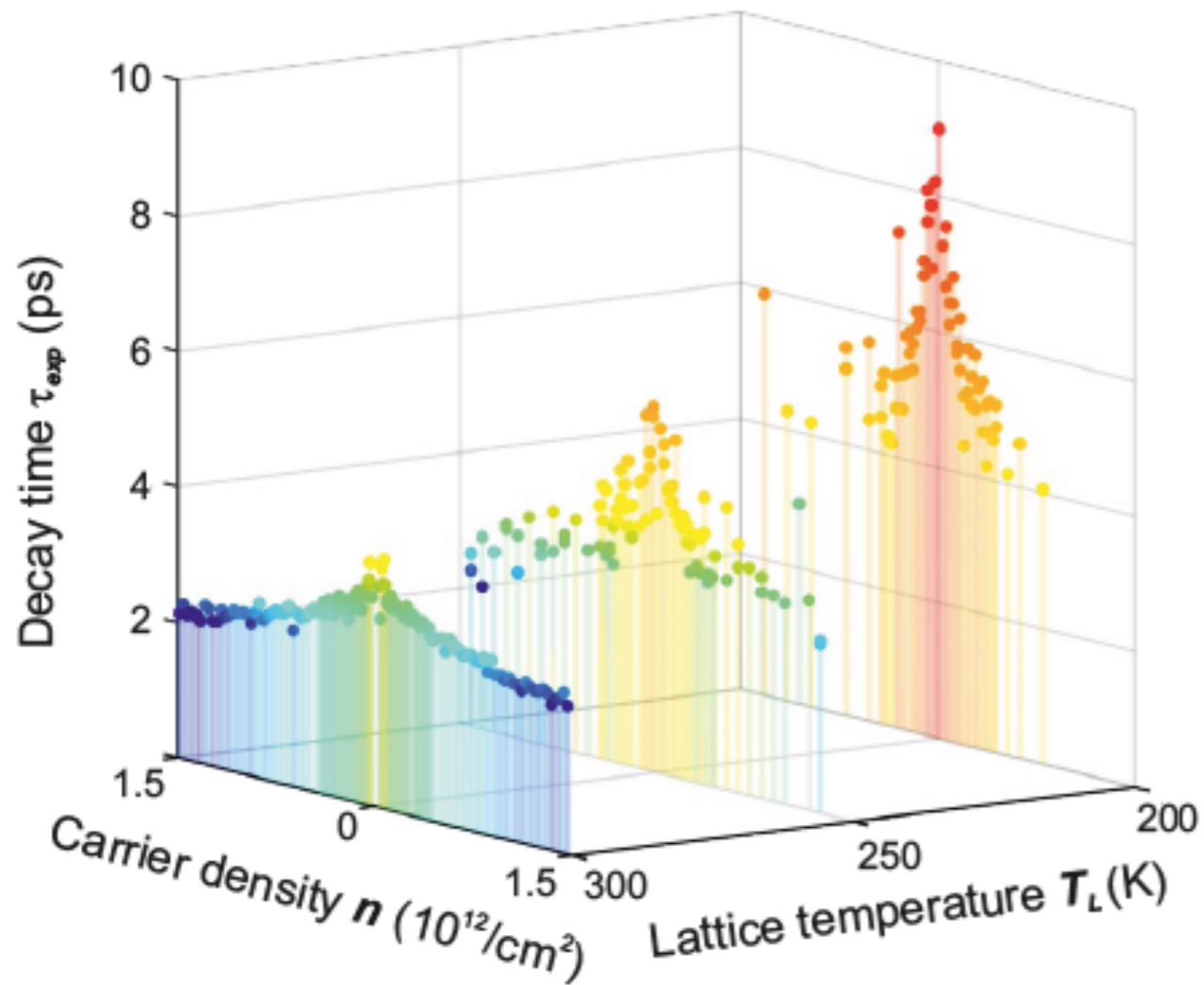


➔ In-plane cooling mechanisms are not consistent with data

Compare with hyperbolic cooling



Compare with hyperbolic cooling



➔ Cooling to hyperbolic hBN phonon polaritons reproduces the trends

Hyperbolic cooling

$$Q = \iiint_{-\infty}^{\infty} \frac{d\omega dk_x dk_y}{(2\pi)^3} [n_B(\omega, T_e) - n_B(\omega, T_L)] M(\omega, k)$$

Energy transfer rate



Marco Polini



Mark Lundeborg



Alessandro Principi

Principi et al, *PRL* 118, 126804 (2017)

Hyperbolic cooling

$$Q = \iiint_{-\infty}^{\infty} \frac{d\omega dk_x dk_y}{(2\pi)^3} [n_B(\omega, T_e) - n_B(\omega, T_L)] M(\omega, k)$$

Energy transfer rate

$$M(\omega, k) = 4 \frac{\mathcal{R}\{Y(\omega, k)\} \mathcal{R}\{\sigma(\omega, k)\}}{|Y(\omega, k) + \sigma(\omega, k)|^2}$$

Impedance matching function
between graphene electrons and
hBN phonon polaritons

➔ No adjustable fit parameters



Marco Polini



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$$\Gamma_{\text{cool}} = \left. \frac{\partial Q}{\partial T_e} \right|_{T_e=T_L}$$

Interfacial heat conductivity

$$\tau_{\text{calc}}^* = C_n / \Gamma_{\text{cool}}$$

Near-equilibrium cooling time



Marco Polini



Mark Lundeberg



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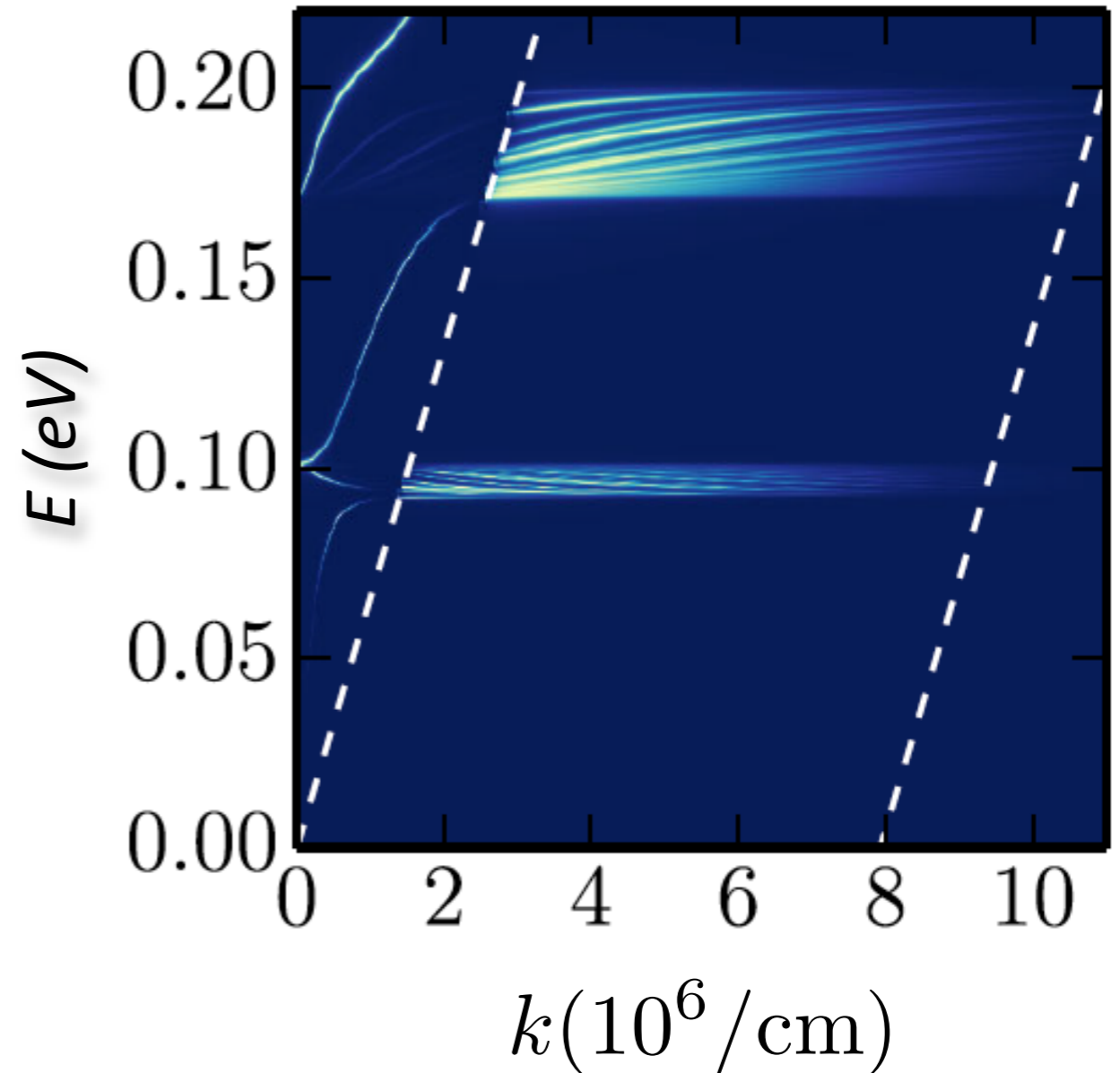
Principi et al, *PRL* 118, 126804 (2017)

Hyperbolic cooling

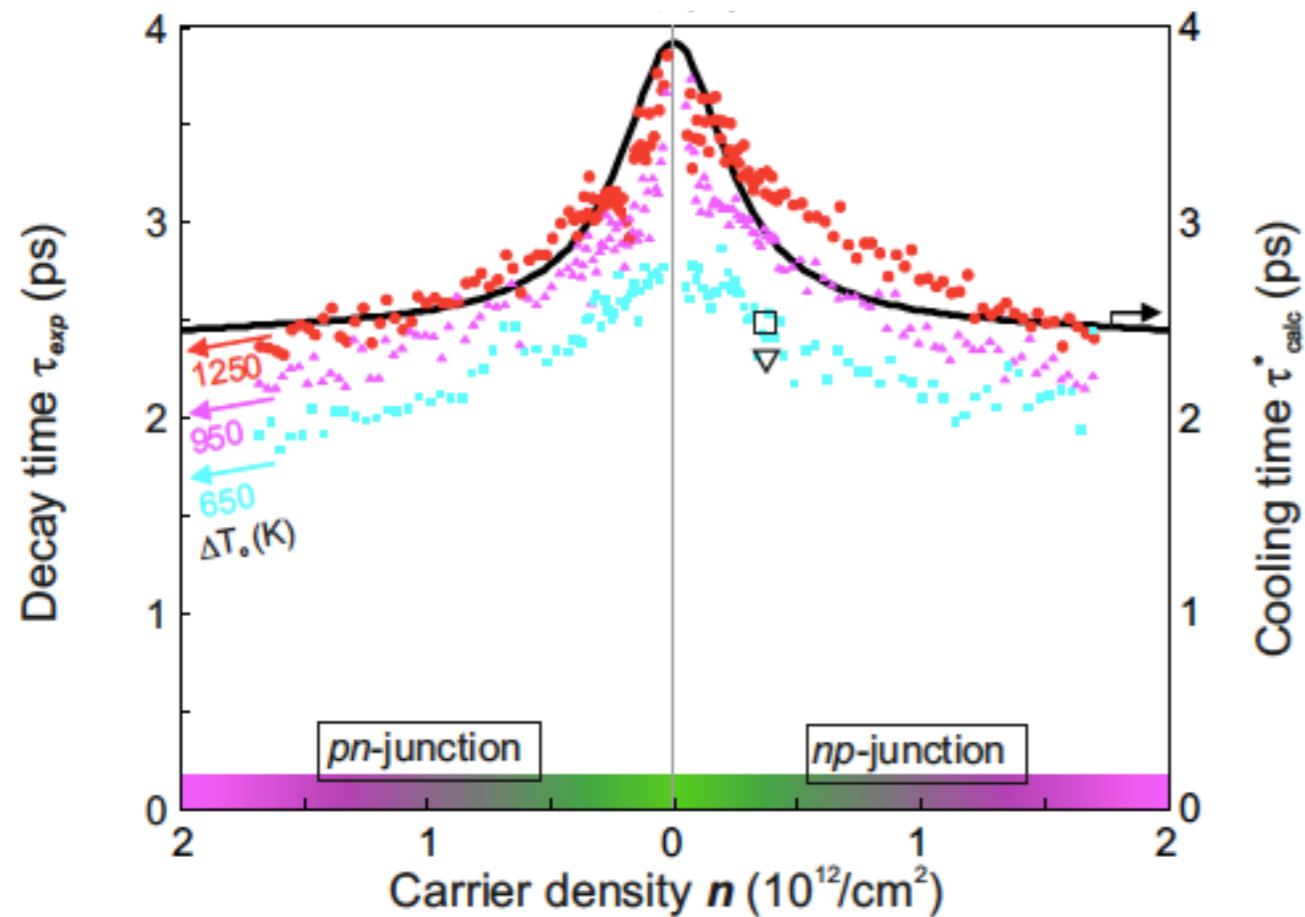
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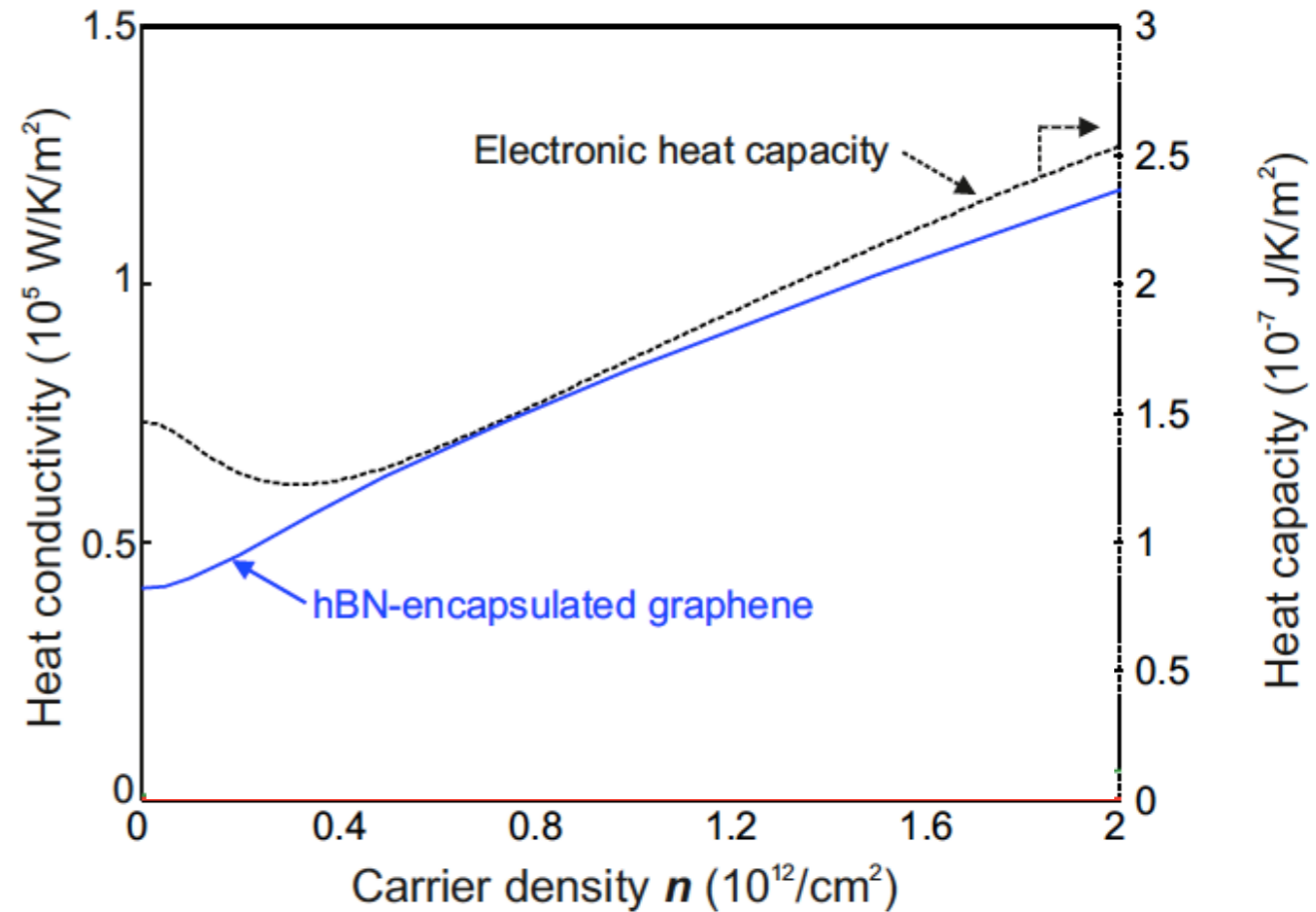
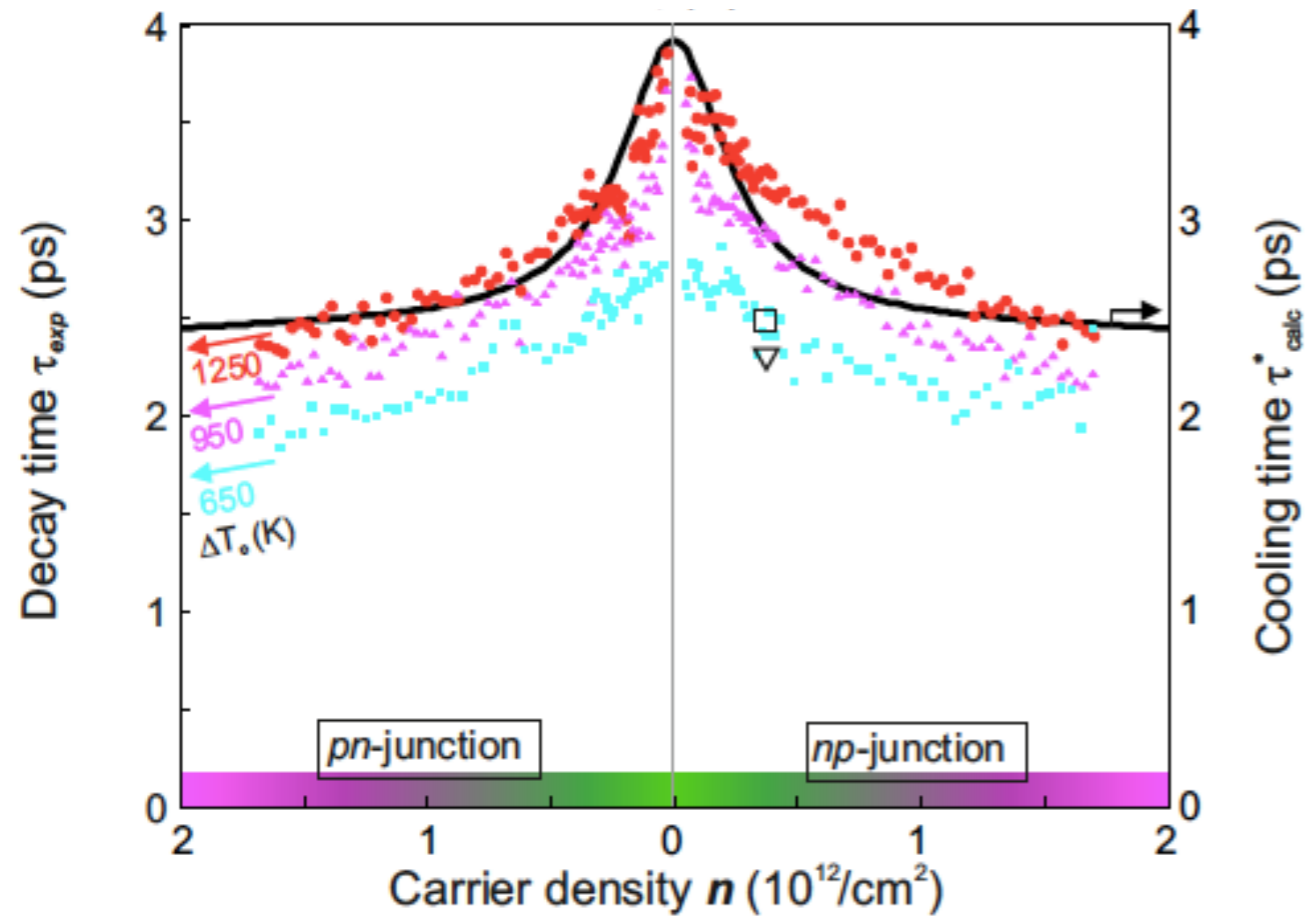


Quantitative comparison



- Origin of the low-density peak?
- Effect of laser power?

Quantitative comparison



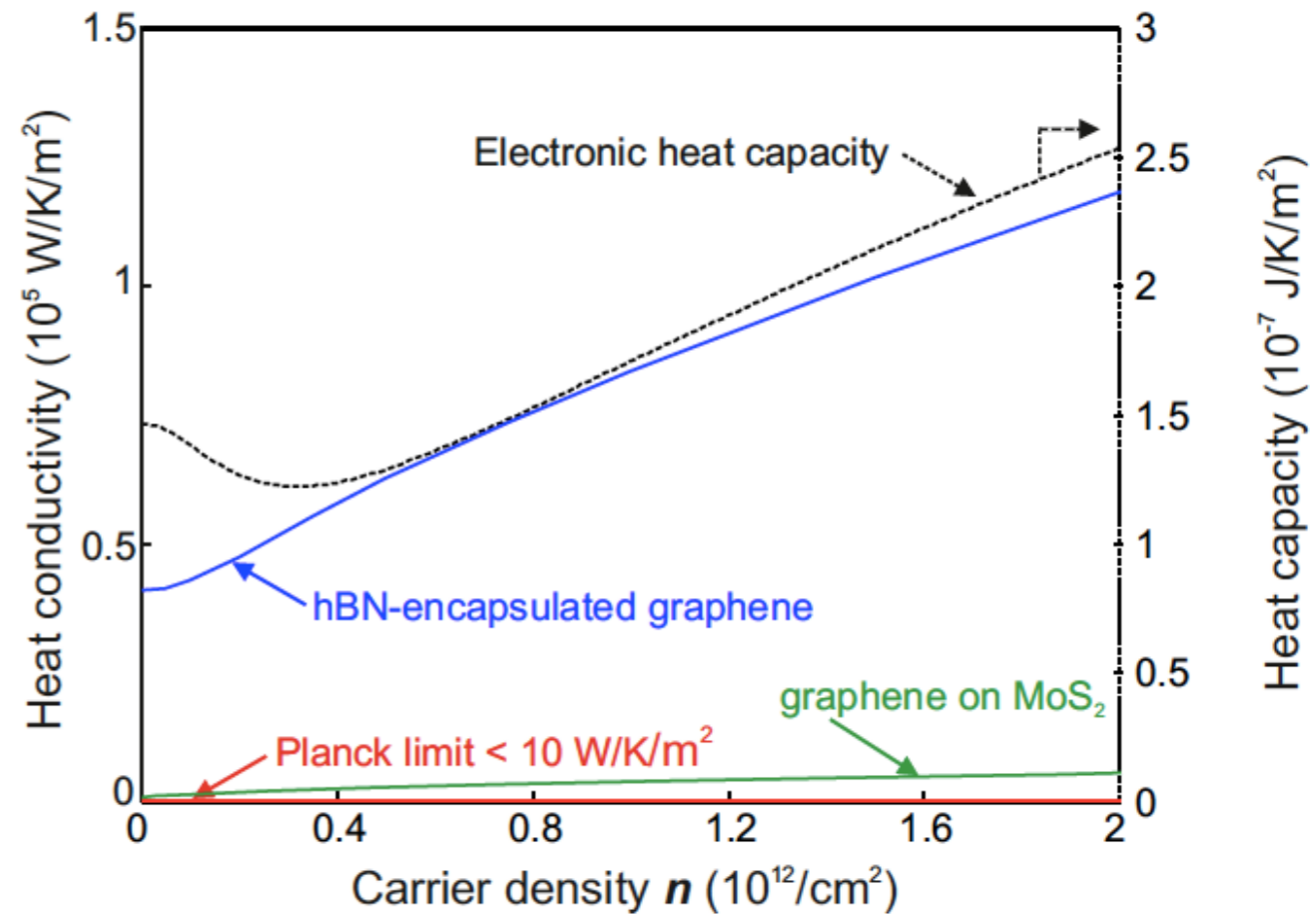
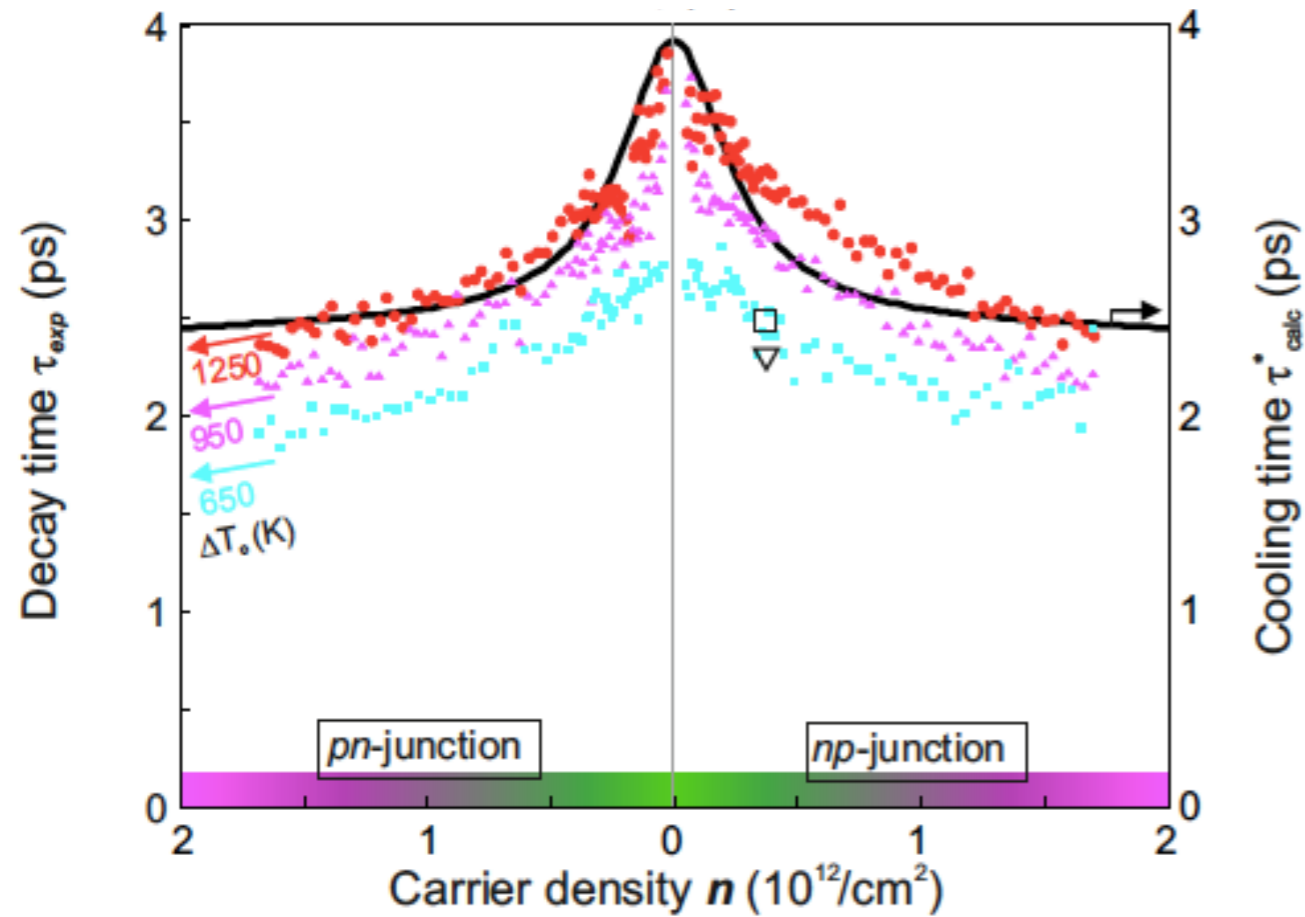
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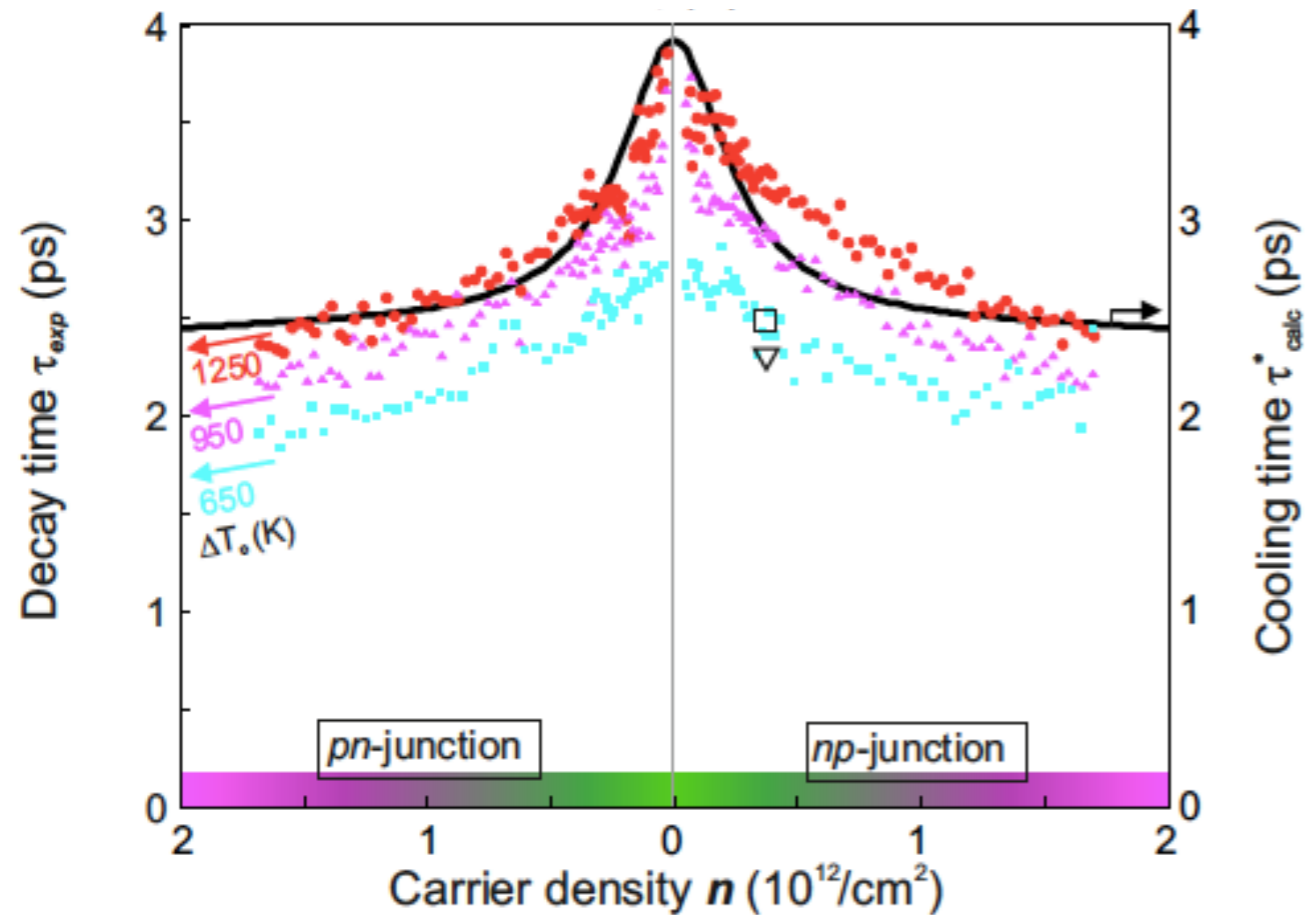
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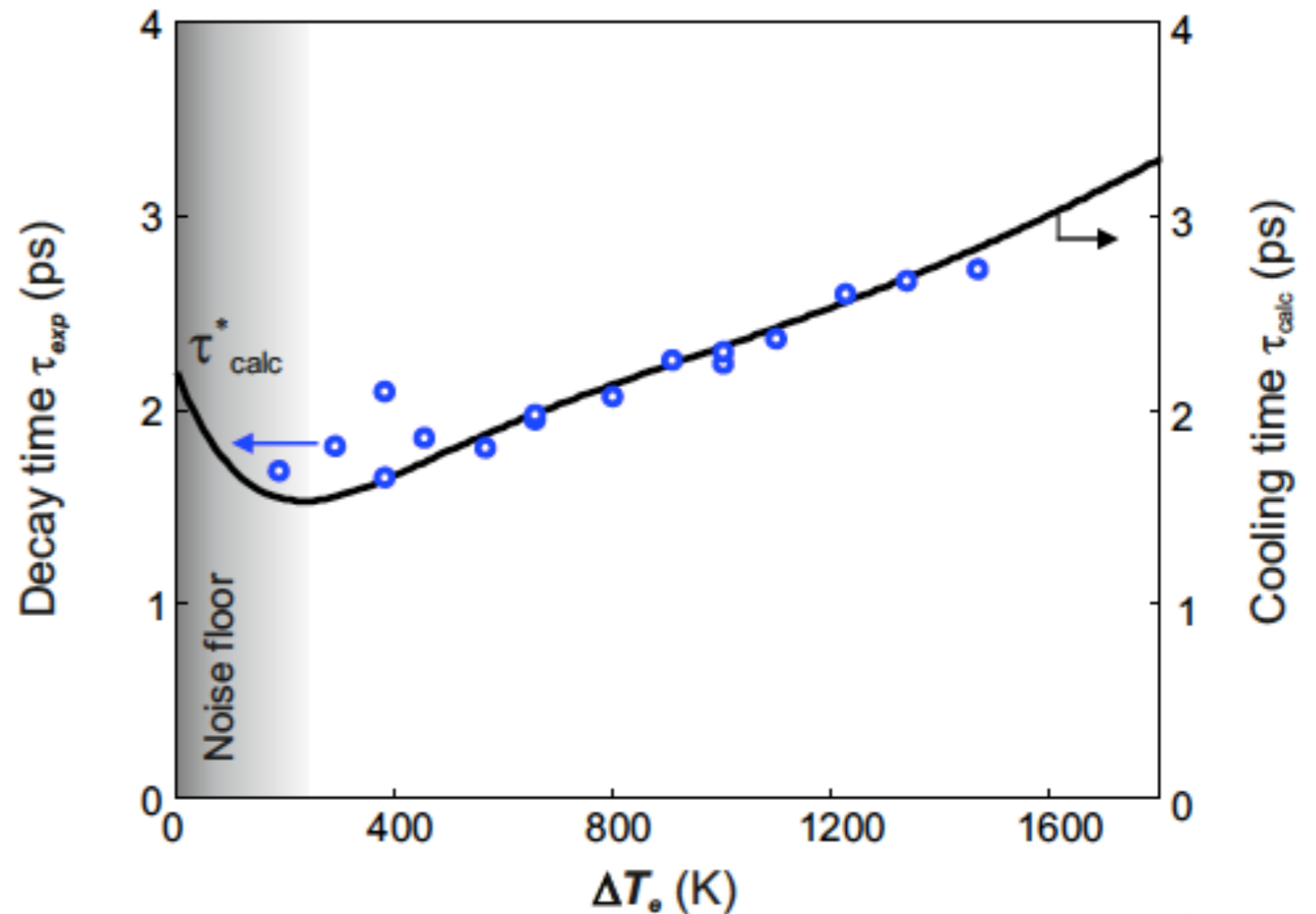
- Origin of the low-density peak?
- **Effect of laser power?**

Quantitative comparison

$$\tau_{\text{calc}}(T_e, T_L) = C_n \frac{T_e - T_L}{Q}$$

Cooling time in overheating regime

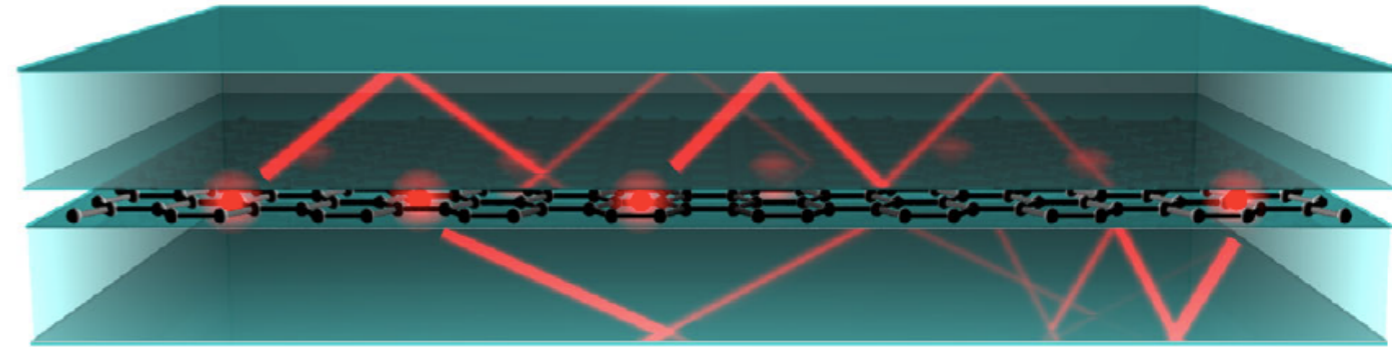
Principi et al, *PRL* 118, 126804 (2017)



- ➔
- Longer cooling time with increasing laser power
 - Consistent with hyperbolic phonon cooling

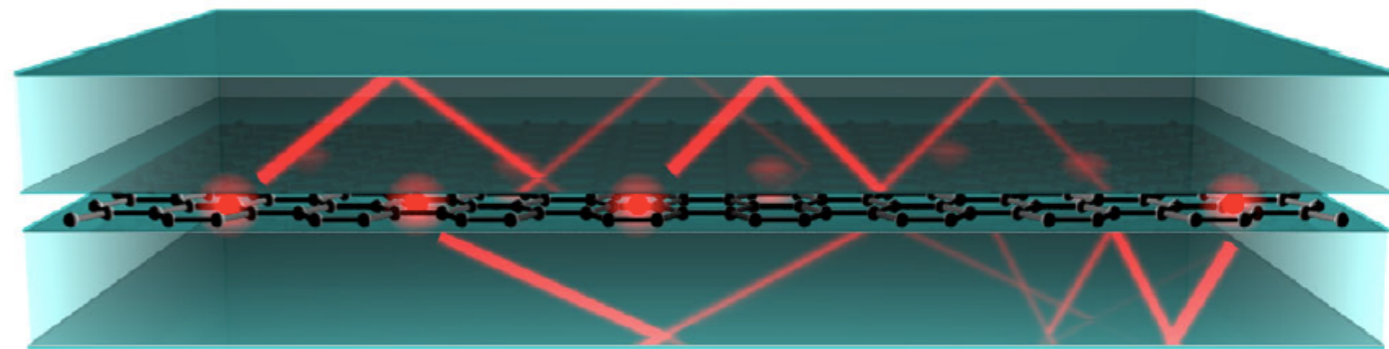
Summary

Graphene encapsulated by hBN:
Cooling of **hot graphene carriers**
through **out-of-plane heat transfer**
to **hBN hyperbolic phonons**

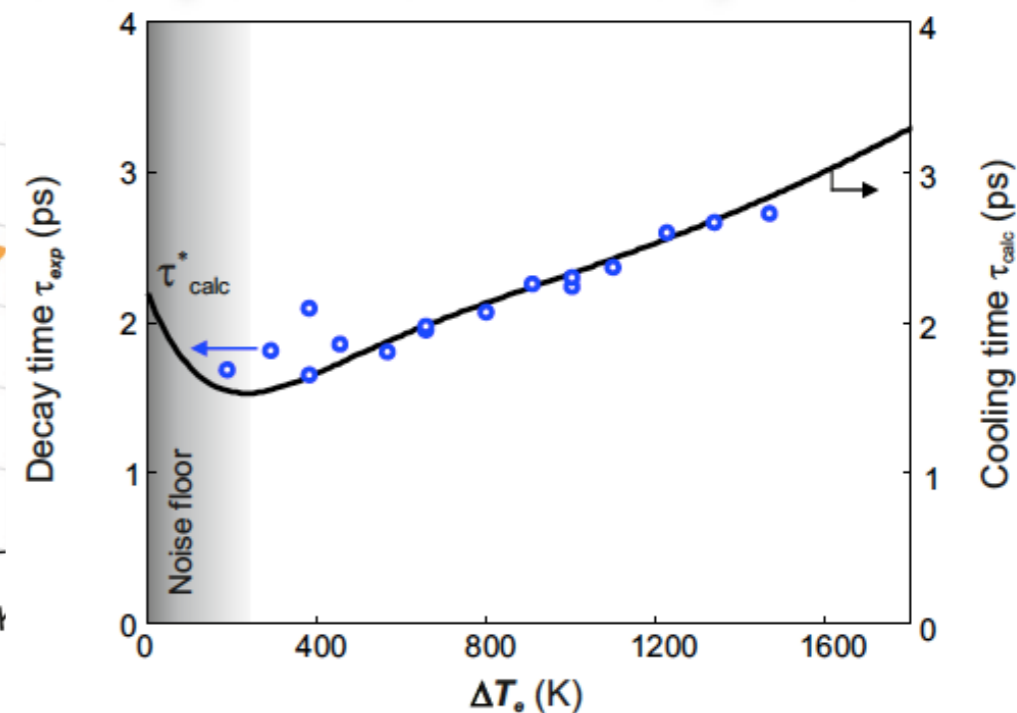
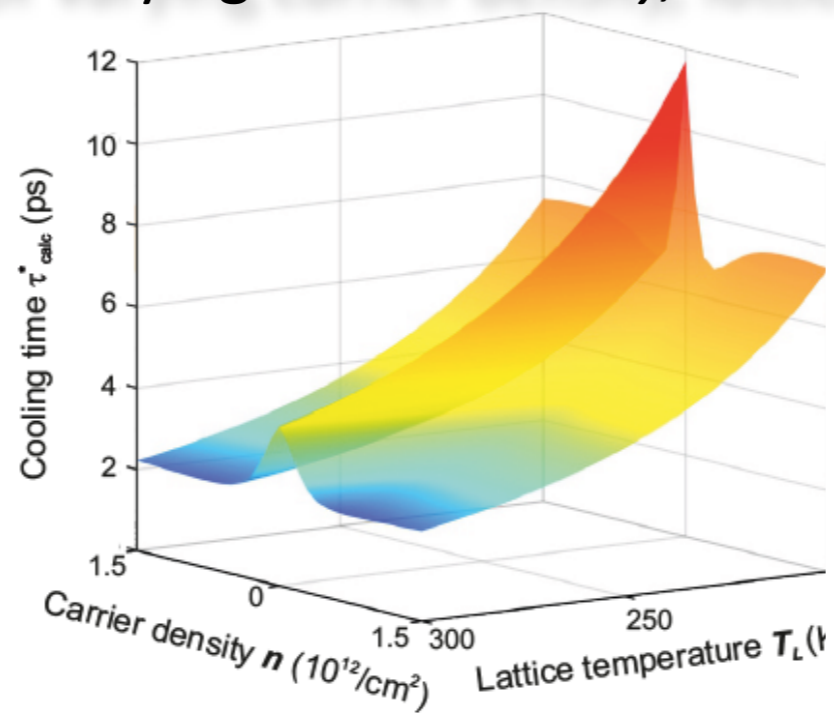
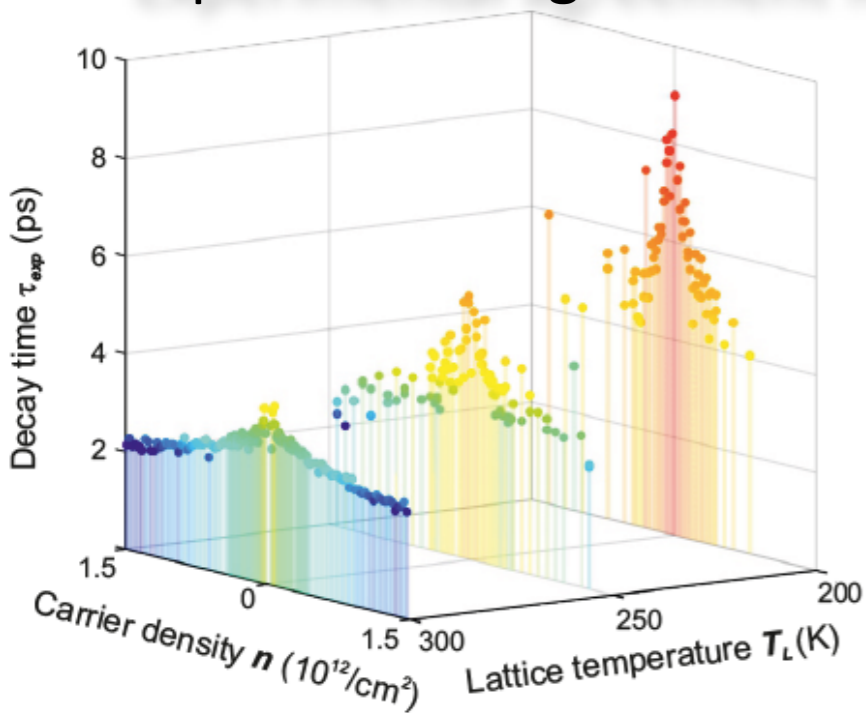


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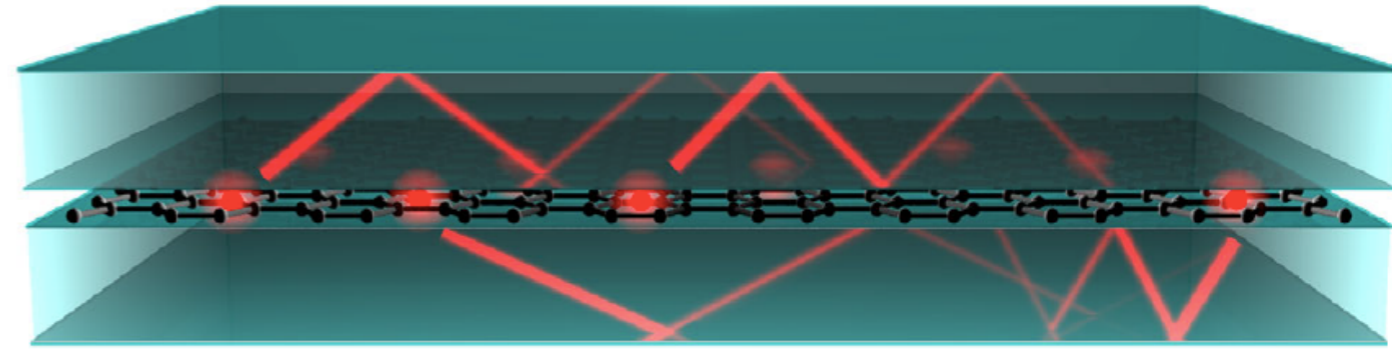


Experimental agreement for varying *carrier density, lattice temperature and laser power*



Outlook

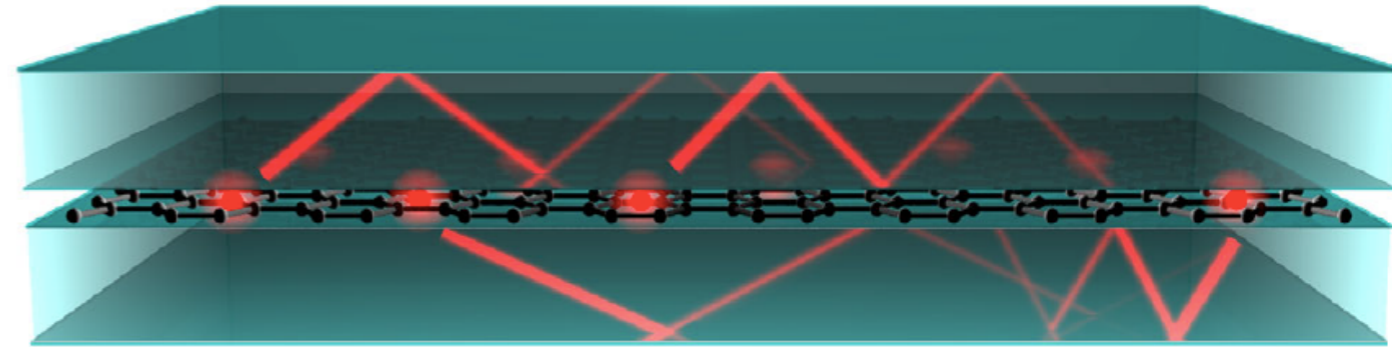
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➔ **Thermal management: ideal substrate = heat sink!**

Outlook

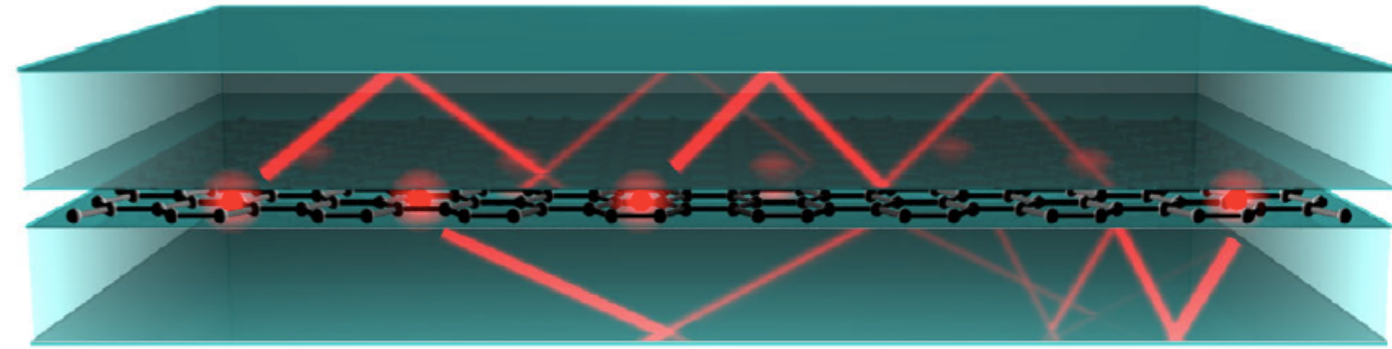
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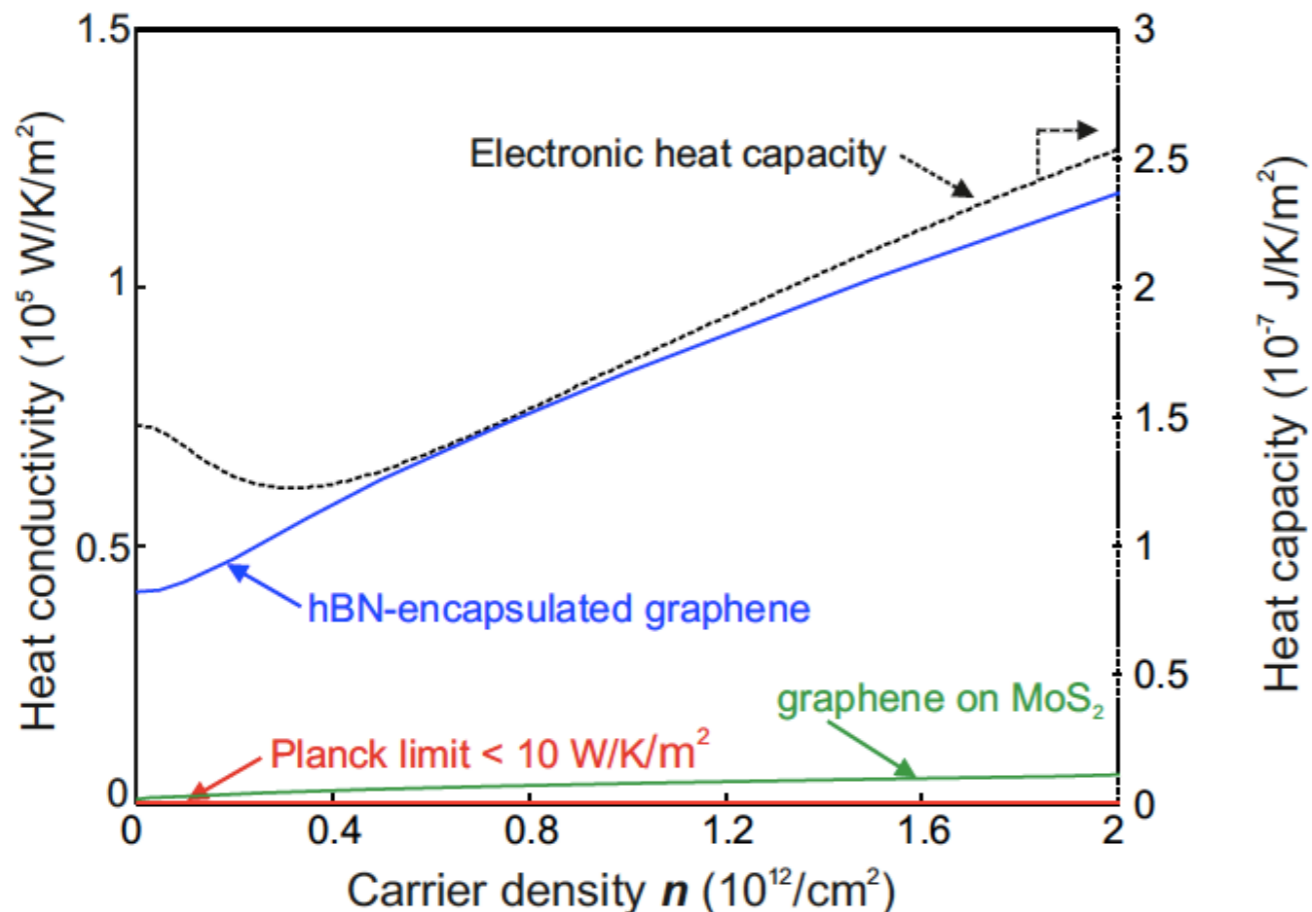
➔ **Photodetectors: electron cooling?**

Outlook

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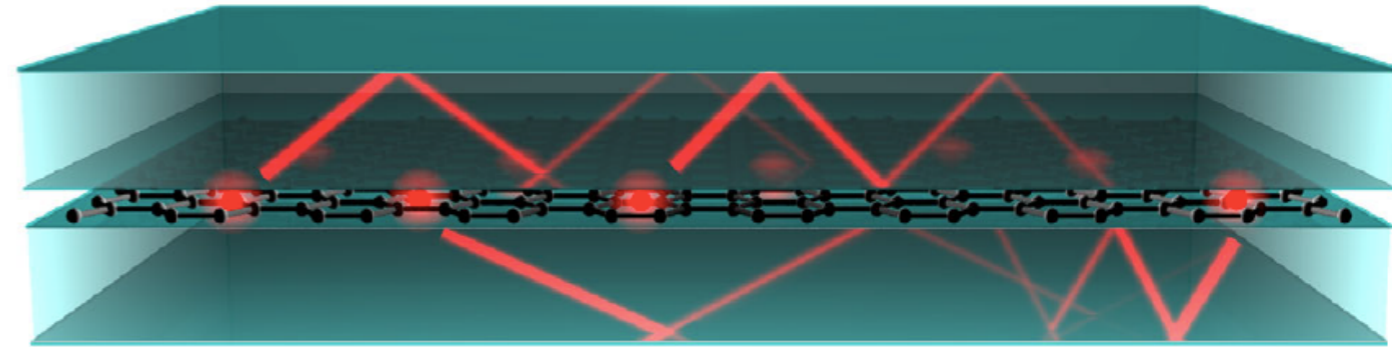


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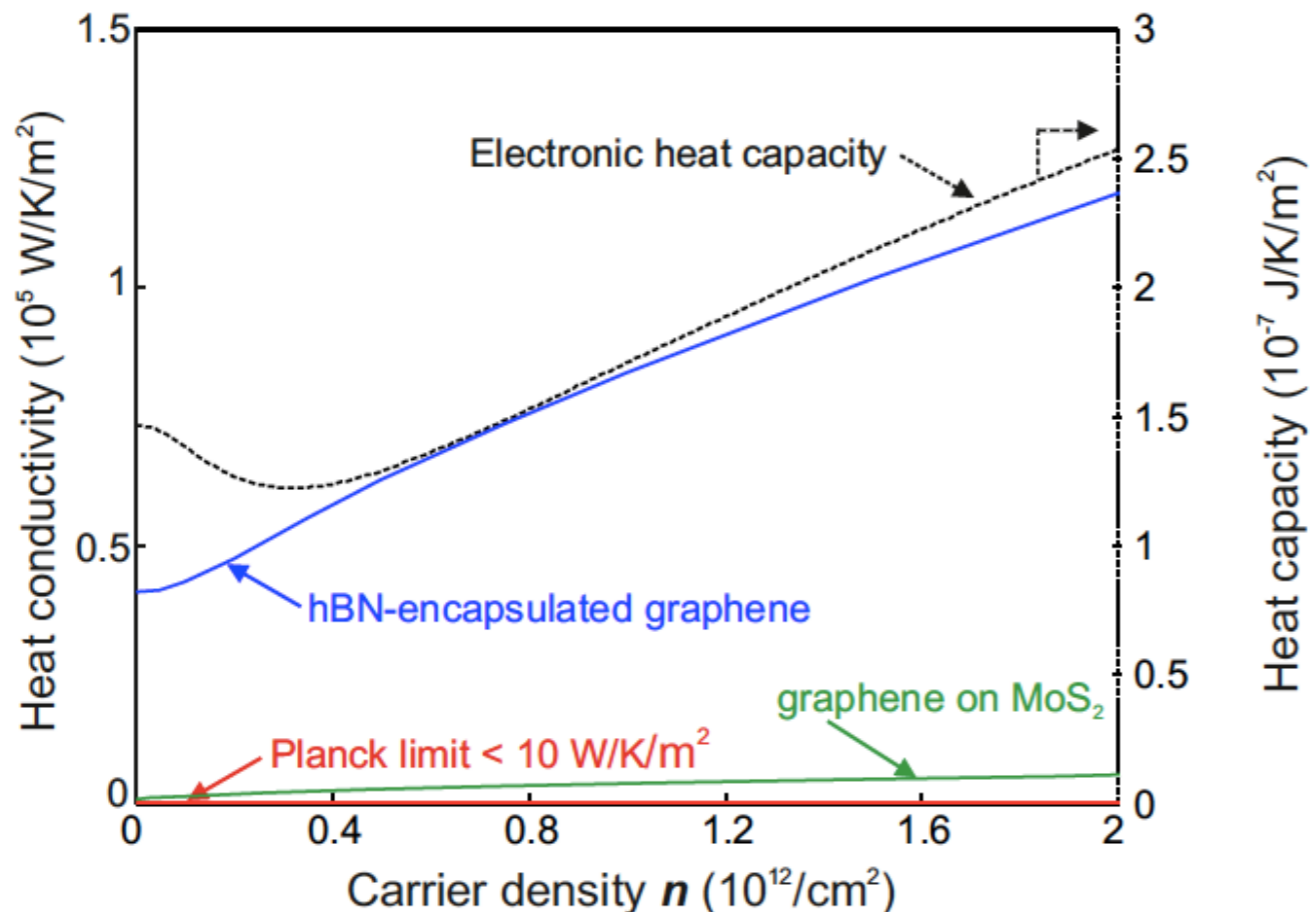


Outlook

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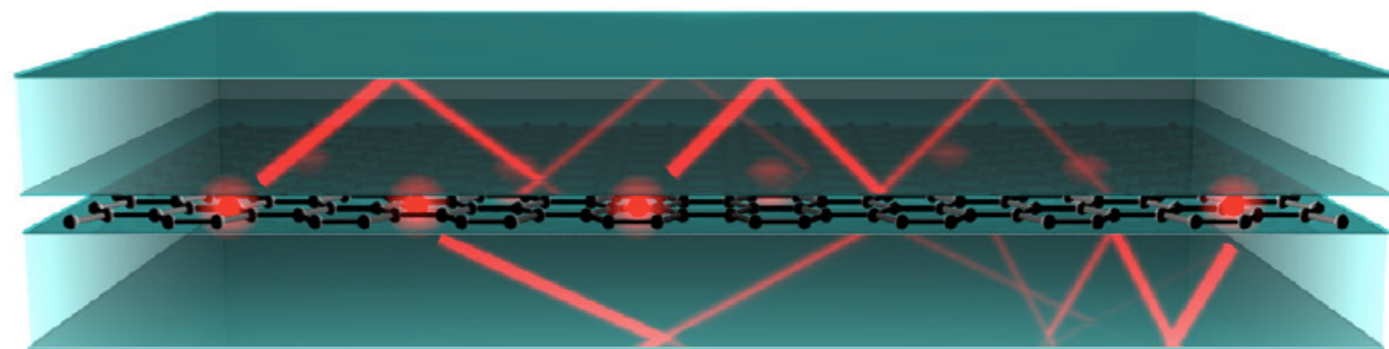
➔ **Photodetectors: electron cooling?**



➔ **Different encapsulant!**

Summary

Graphene encapsulated by hBN:
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Experimental agreement for varying *carrier density, lattice temperature and laser power*

