

# Multiferroic Orders in Two-dimensional Materials

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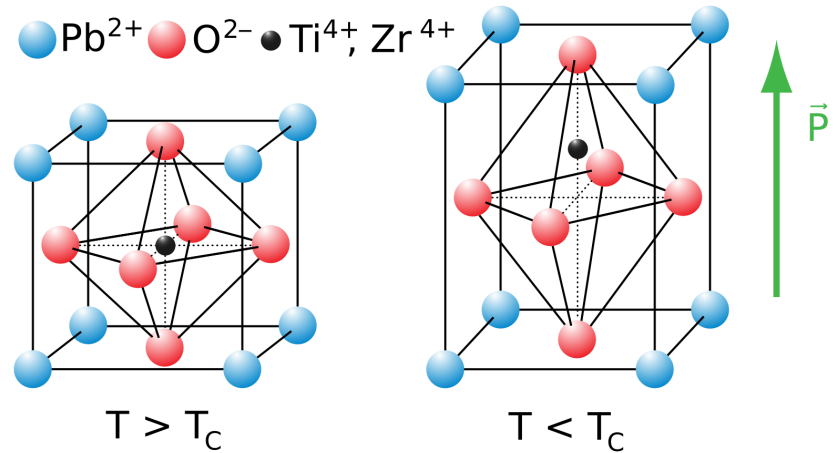
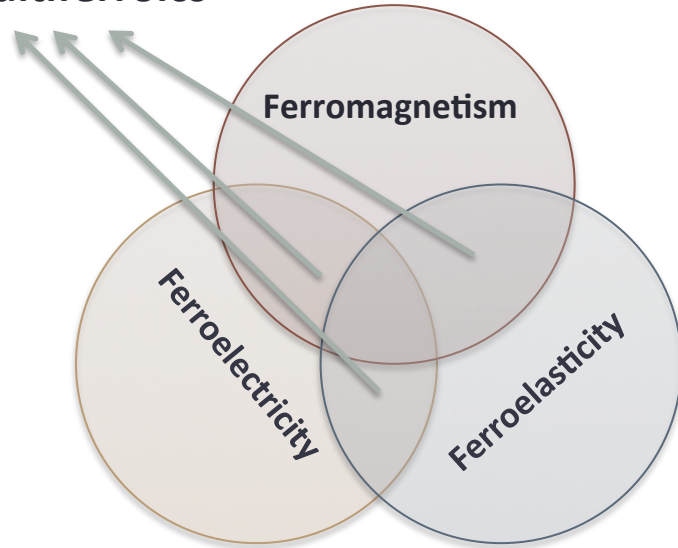
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# Multiferroics

Multiferroics



Perovskite

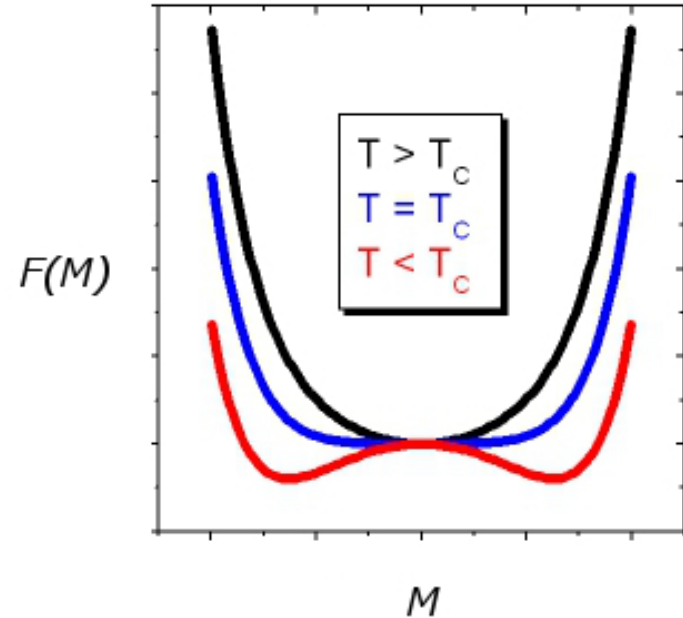
# Landau theory

$$F(\mathcal{M}) = \alpha(T)\mathcal{M}^2 + \beta\mathcal{M}^4$$

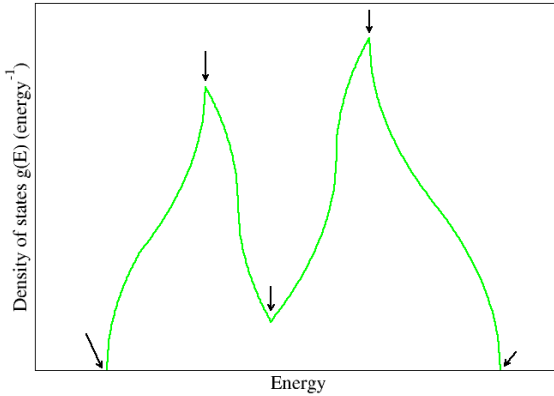
$$\frac{\partial F}{\partial \mathcal{M}} = 0 \Rightarrow \alpha(T)\mathcal{M} + 2\beta\mathcal{M}^3 = 0$$

$$\mathcal{M} = 0, \quad \mathcal{M} = \pm \sqrt{-\frac{\alpha(T)}{2\beta}}$$

$$\alpha(T) = \alpha_0(T - T_C)$$

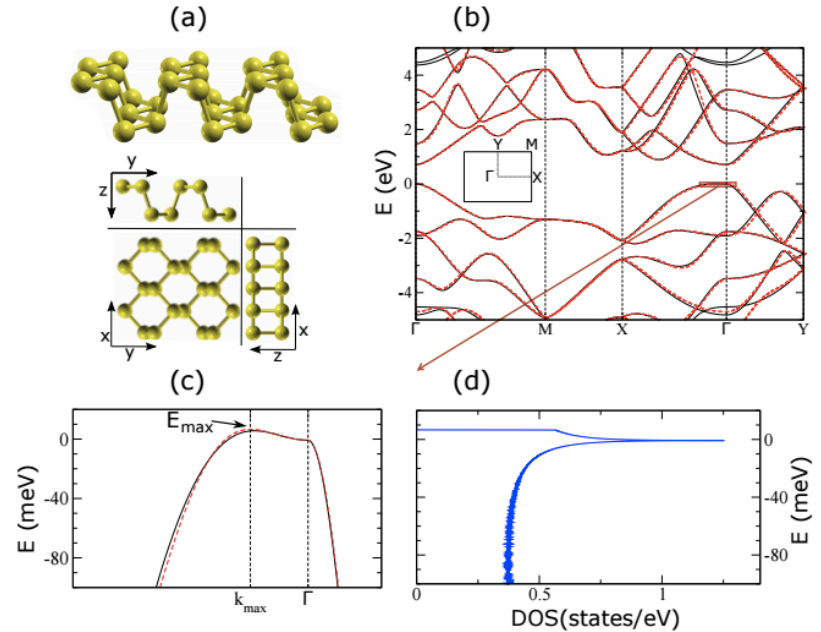


# van Hove singularities (VHS)



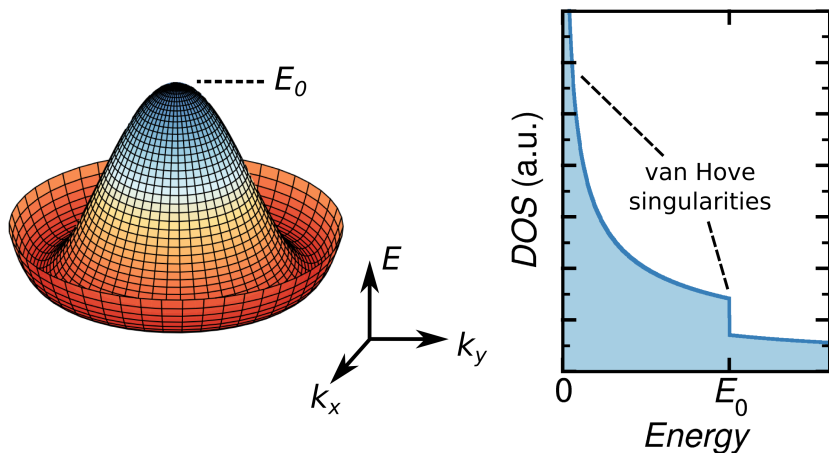
## Stoner criterion

$$DOS(E_F)U > 1$$



A. Ziletti *et al.* Phys. Rev. B **92**, 085423 (2015)

# Mexican-hat band edge (MHBE)



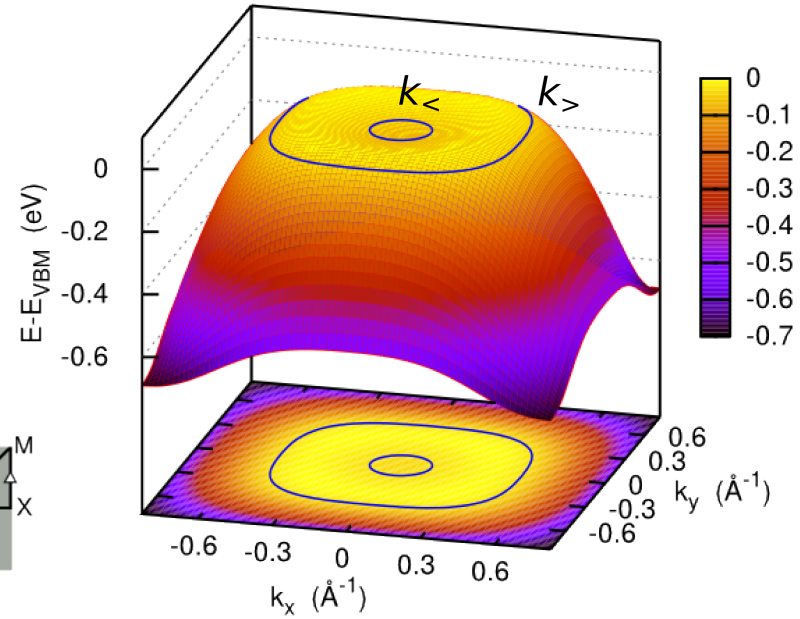
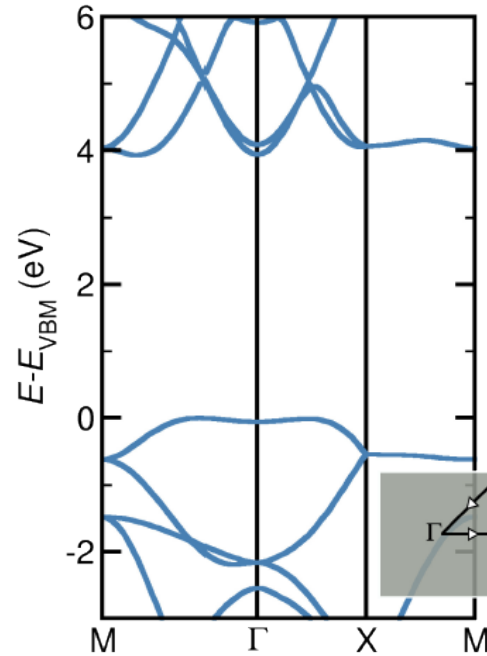
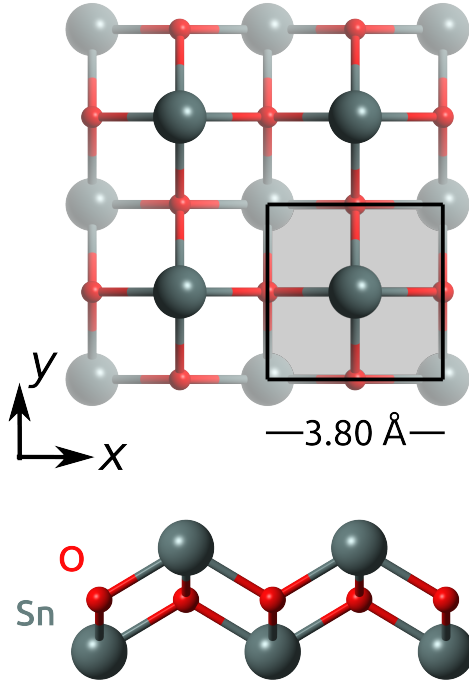
**Band edge**

$$E(k) = Ak^4 + Bk^2 + E_0,$$

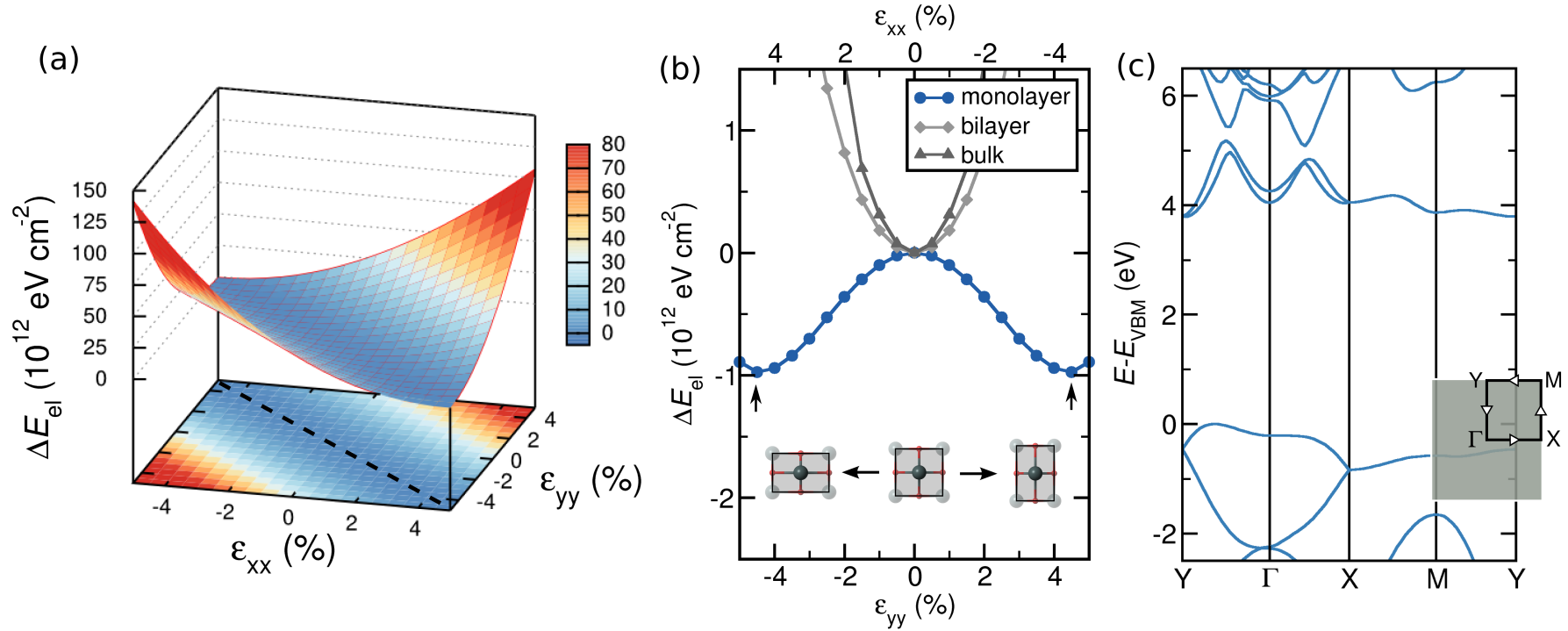
**Density of states**

$$DOS(E) = \frac{1}{4\pi\sqrt{A}} \frac{1}{\sqrt{E}} \left[ 1 - \frac{\Theta(E - E_0)}{2} \right]$$

# $\alpha$ -SnO



# Ferroelasticity in $\alpha$ -SnO



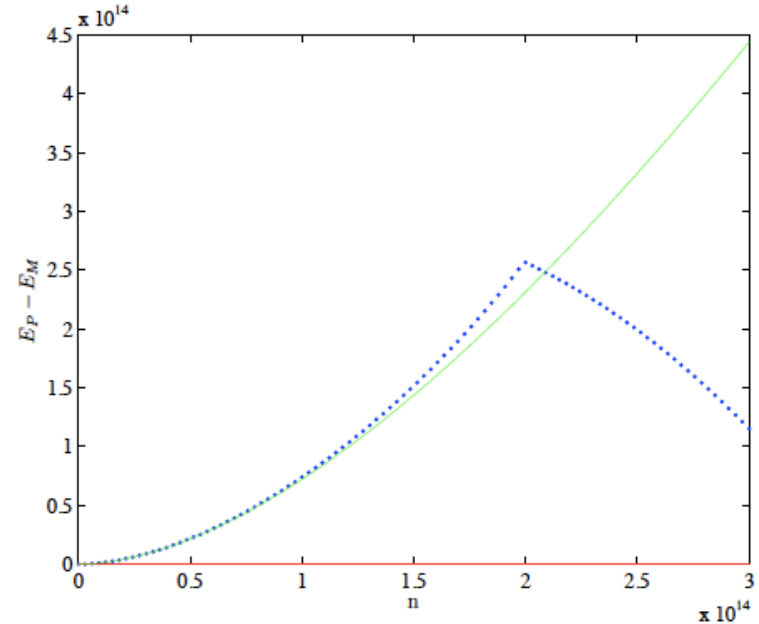
# Ferromagnetism (Analytical model)

Magnetic system

$$\mathcal{E}_{\text{system}}^{\text{M}}(n) \approx n^2 \left\{ \frac{4\pi^2 A}{3} n - e^2 \left( 3 + 2 \ln \left( \frac{2B}{An\pi} \right) \right) \sqrt{\frac{A}{2B}} \right\}$$

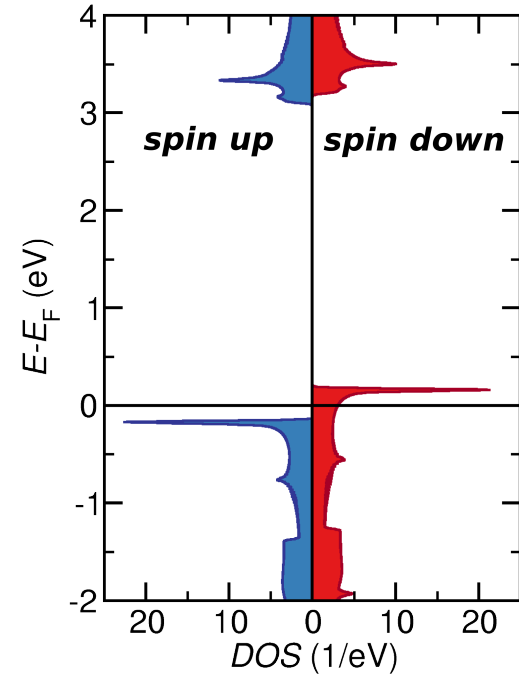
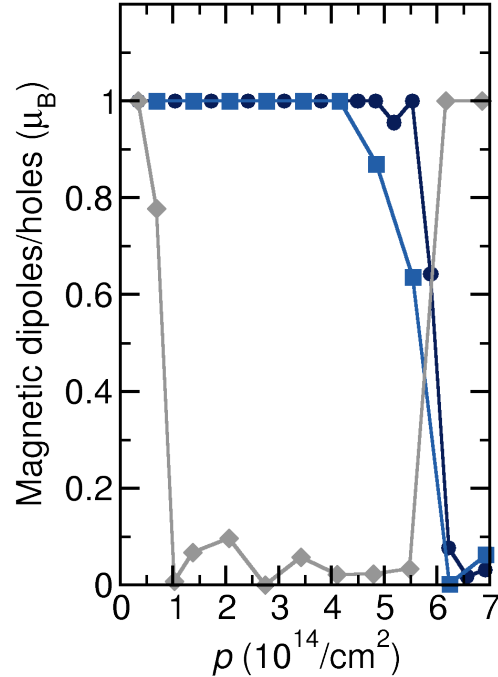
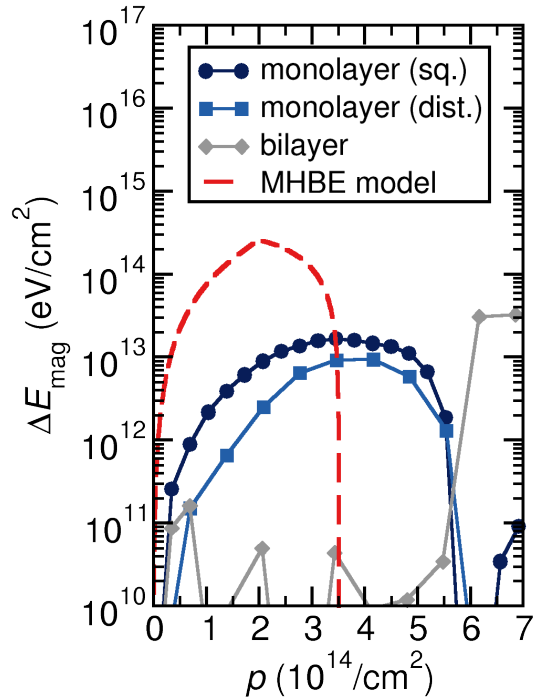
Non-magnetic system

$$\mathcal{E}_{\text{system}}^{\text{U}}(n) \approx 2 \left[ \left( \frac{n}{2} \right)^2 \left\{ \frac{2\pi^2 A}{3} n - e^2 \left( 3 + 2 \ln \left( \frac{4B}{An\pi} \right) \right) \sqrt{\frac{A}{2B}} \right\} \right]$$

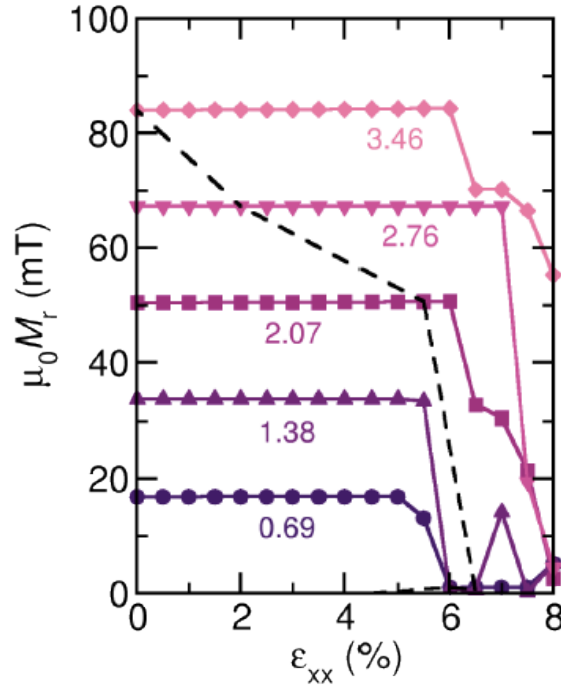
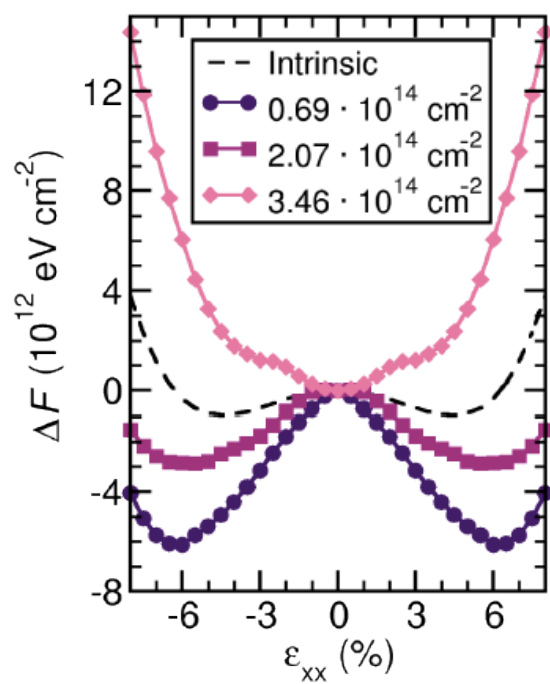




# Ferromagnetism in $\alpha$ -SnO



# Multiferroicity in $\alpha$ -SnO



**Ferroelasticity  
+  
Ferromagnetism**

# Landau theory of $\alpha$ -SnO

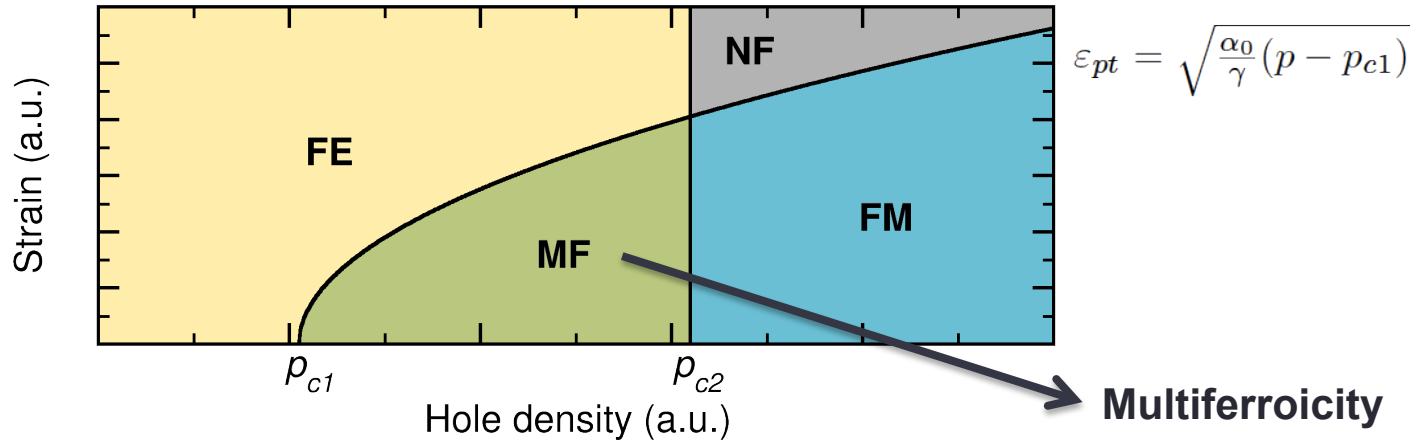
Ferromagnetic

Ferroelastic

$$F(\mathcal{M}, \varepsilon) = \alpha(p)\mathcal{M}^2 + \beta\mathcal{M}^4 + \gamma\varepsilon^2\mathcal{M}^2 + \eta(p)\varepsilon^2 + \lambda\varepsilon^4$$

$$\alpha(p) = \alpha_0(p_{c1} - p)$$

$$\eta(p) = \eta_0(p - p_{c2})$$



# Summary

- 2D materials with Mexican-hat band edge can become ferromagnetic with free carrier densities;
- $\alpha$ -SnO is ferroelastic for monolayer;
- $\alpha$ -SnO can be multiferroic for  $p$ -type doped material.
- **$\alpha$ -SnO monolayer is the first 2D material multiferroic with ferromagnetism and ferroelasticity.**

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## Thank you!