#### Spin Hall Effect and Origins of Nonlocal Resistance in Adatom-Decorated Graphene

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#### Introduction

### Nonlocal resistance and spin Hall angle in multiterminal graphene

**3** Scaling of spin Hall angle and nonlocal resistance with adatom concentration

(4) Six-terminal graphene geometry for isolating the SHE contribution to  $R_{\rm NL}$ 





#### **Motivation**



Over the past decade, the spin Hall effect (SHE) has become the standard pure spin-current generator (a) and detector (b).



#### Six-terminal graphene device



$$\begin{aligned} \mathscr{H} &= - \gamma_0 \sum_{\langle ij \rangle} c_i^{\dagger} c_j + \frac{2i}{\sqrt{3}} V_I \sum_{\langle \langle ij \rangle \rangle \in \mathscr{R}} c_i^{\dagger} \vec{s} \cdot (\vec{d}_{kj} \times \vec{d}_{ik}) c_j \\ &+ i V_R \sum_{\langle ij \rangle \in \mathscr{R}} c_i^{\dagger} \vec{z} \cdot (\vec{s} \times \vec{d}_{ij}) c_j - \mu \sum_{i \in \mathscr{R}} c_i^{\dagger} c_i. \end{aligned}$$

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# Definition of Spin Hall angle and Nonlocal resistance



 $\frac{\text{Spin Hall angle}}{\theta_{\text{sH}} = l_5^{S_z}/l_1}$ 

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Nonlocal resistance  $R_{\rm NL} = V_{\rm NL}/I_1 = (V_3 - V_4)/I_1$ 

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# Nonlocal resistance and spin Hall angle in multiterminal graphene



We calculate the total charge  $I_p$  and spin  $I_p^{S_z}$  currents and voltages  $V_p$  in leads p = 2-6 in response to injected charge current  $I_1$  using the multiterminal Landauer-Büttiker formula, as implemented in KWANT (http://kwant-project.org/).

# Nonlocal resistance and spin Hall angle in multiterminal graphene

Nonzero  $R_{\rm NL}$  even when all SOC terms are switched off ( $V_R = V_I = 0$ ), while keeping random on-site potential  $\mu \neq 0$  due to Au adatoms.

Complex sign change of  $R_{\rm NL}$ .

 $R_{\rm NL} = R_{\rm NL}^{\rm SHE} + R_{\rm NL}^{\rm Ohm} + R_{\rm NL}^{\rm qb} + R_{\rm NL}^{\rm pd}$ 



## Additive contributions to Nonlocal resistance

$R_{\rm NL}^{ m SHE}$	positive	combined direct and inverse SHE.
$R_{\rm NL}^{\rm Ohm}$	positive	classical diffusive charge transport
$R_{ m NL}^{ m qb}$	negative	quasiballistic contribution due to $T_{32} eq 0$
$R_{ m NL}^{ m pd}$	positive	pseudodiffusive transport in Dirac materials

For devices with W>L, the positive sign of  $R_{\rm NL}$  is dominated by  $R_{\rm NL}^{\rm pd}$ .

For devices with L > W,  $R_{\rm NL}^{\rm Ohm}$  can be neglected; then, the main competition is between  $R_{\rm NL}^{\rm Qb}$  and  $R_{\rm NL}^{\rm SHE}$ .



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# Scaling of the pseudodiffusive contribution to $R_{NL}$



In pristine graphene, this positive nonlocal signal around the CNP is specific to Dirac electron systems.

This mechanism provides background contribution  $R_{\rm NL}^{\rm pd}$ of positive sign to total  $R_{\rm NL}$ , as long as W > L.

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### Spin Hall angle as a function of the concentration of randomly scattered Au adatoms



The values of  $\theta_{sH}$  are averaged over the Fermi energy interval [-0.01%, 0.01%].

 $\theta_{\rm sH}$  increases with the adatom concentration in the limit of low  $n_i$ .

# Nonlocal resistance for a uniform distribution of gold adatoms



The large value of the nonlocal signal and  $\theta_{\rm sH}$  is away from CNP due to doping of graphene by  $\mu = 0.3\gamma_0$ , viewing the central region as a single large cluster.



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# Six-terminal graphene device for isolating the SHE contribution to *R*<sub>NL</sub>



We remove adatoms in the channel for isolating  $R_{\rm NL}^{\rm SHE}$ . For a sufficiently long channel,  $R_{\rm NL}^{\rm pd} = 0$  due to L > W and  $R_{\rm NL}^{\rm qb}$ ,  $R_{\rm NL}^{\rm Ohm} \to 0$  due to the absence of adatom-induced scattering in the channel.

# Six-terminal graphene device for isolating the SHE contribution to $R_{\rm NL}$



 $R_{\rm NL}$  and  $\theta_{\rm sH}$  exhibit a sharp peak at about the same Fermi energy located very close to the CNP, which demonstrates one-toone correspondence between directly measurable charge transport quantity  $R_{\rm NL}$  and indirectly inferred spin transport quantity  $\theta_{\rm sH}$ .

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### Summary

- By using the multiterminal LB formula, we obtained  $\theta_{\rm sH} \sim 0.1-0.3$  in Au-decorated graphene with large Au-adatom concentration  $n_i = 15\%$ .
  - +  $\theta_{sH}$  significantly decreases with temperature and adatom clustering.
- The SHE contribution to R<sub>NL</sub> was isolated in a special configuration with an impurity-free channel and L > W.
  - There is a one-to-one correspondence between directly measurable  $R_{\rm NL}$  and indirectly inferred  $\theta_{\rm sH}$ .

